



Quantum Black Holes

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Semi-classical Black Holes and Quantum Black Holes

Model of low scale quantum gravity:

Formation of small black holes (BH) at elementary particle colliders

Semi-Classical BH

- thermal object
- decay via Hawking radiation into many particle final state
- formation unlikely since $M_{\text{BH}} \gg M_{\text{P}}$
- geometrical cross section:

$$\sigma = \pi r_s^2$$

QBH

- non-thermal object
- decay into only a few particles
- interpretation as short-lived state
- cross section from semi-classical case

Effective Operators for QBHs

How to model these states in particle physics processes?

→ suitable Effective Field Theory

QBH

- e.g. spinless QBH is represented by scalar field
- charges in accordance with gauge quantum numbers of Standard Model

Interaction

- defined by EFT
 - matching of cross section with geometrical one
- conservation of gauge symmetries
- no equal assumption for global symmetries

Effective Operators for QBHs

Lagrangian

$$\mathcal{L} = \frac{c}{M_P^2} \square \phi \bar{\psi} \psi + h.c.$$

- ϕ : neutral scalar field \rightarrow QBH
- ψ : fermion field
- c : adjustable parameter to match cross section, depending on CoM energy and relevant masses

Matching of Cross Sections

Cross section for production of scalar field

$$\sigma(2\psi \rightarrow \phi) = \frac{\pi}{s} |\mathcal{A}|^2 \delta(s - M_{BH}^2)$$

$$\text{amplitude: } |\mathcal{A}(2\psi \rightarrow \phi)|^2 = s^2 \frac{c^2}{\bar{M}_P^4} \left[s - (m_1 + m_2)^2 \right]$$

Geometrical Cross Section

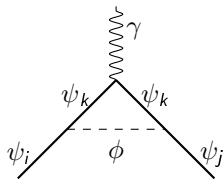
$$\sigma \sim \pi r_s^2, \quad 4d : r_s = \frac{\sqrt{s}}{4\pi \bar{M}_P^2}$$

$$\text{thus: } c^2 = \frac{1}{4\pi \left[s - (m_1 + m_2)^2 \right]} \frac{\sqrt{s} \left[(\sqrt{s} - M_{BH})^2 + \frac{\Gamma^2}{4} \right]}{\Gamma}$$

Low energy contributions

Effective Lagrangian

$$L_{\text{eff}} = \sum_{ij} \frac{1}{\bar{M}_P} \bar{\psi}_i (A_{ij} + B_{ij} \gamma_5) \sigma_{\mu\nu} \psi_j F^{\mu\nu}$$



- ① anomalous magnetic moment
 $\rightarrow \bar{M}_P > 2 \times 10^8 \text{ GeV}$
- ② “forbidden“ lepton family number violating processes, e.g. $\mu \rightarrow e \gamma$
 $\rightarrow \bar{M}_P > 7.2 \times 10^{12} \text{ GeV}$
- ③ CP violation \rightarrow EDM of leptons and quarks of SM, e.g. for neutron
 $\rightarrow \bar{M}_P > 4.5 \times 10^{16} \text{ GeV}$

Thanks

Thanks for your attention!