

# **Self-similar model of Relativistic Astrophysical Jet**

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# Outline

- **Motivations**
- **Self-similar model**
- **Modeling of extragalactic jet**
- **Classification FRI/FRII**
- **Conclusion**

# **Jet in Active galactic nuclei**

## **Spin jet**

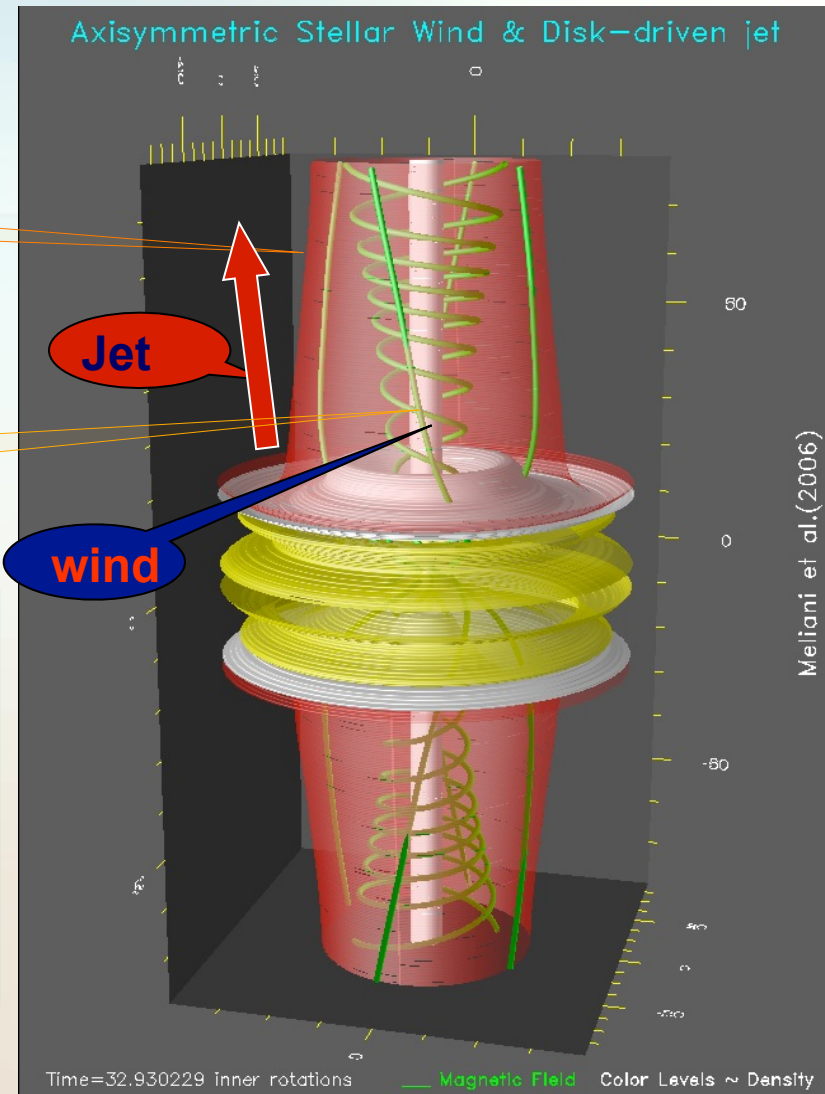
# Jet launching

✓ Ejection from disk

✓ Ejection from inner corona

Results

The energy and angular  
Momentum is extract by jet and  
wind



Meliani, Casse, Sauty, 2006

# Self-similar model of relativistic jet (Schwarzschild metric)

## • Self-similar method

$\alpha$ : magnetic flux

$\alpha$ : function of the radius  $R$  and the angle  $\theta$

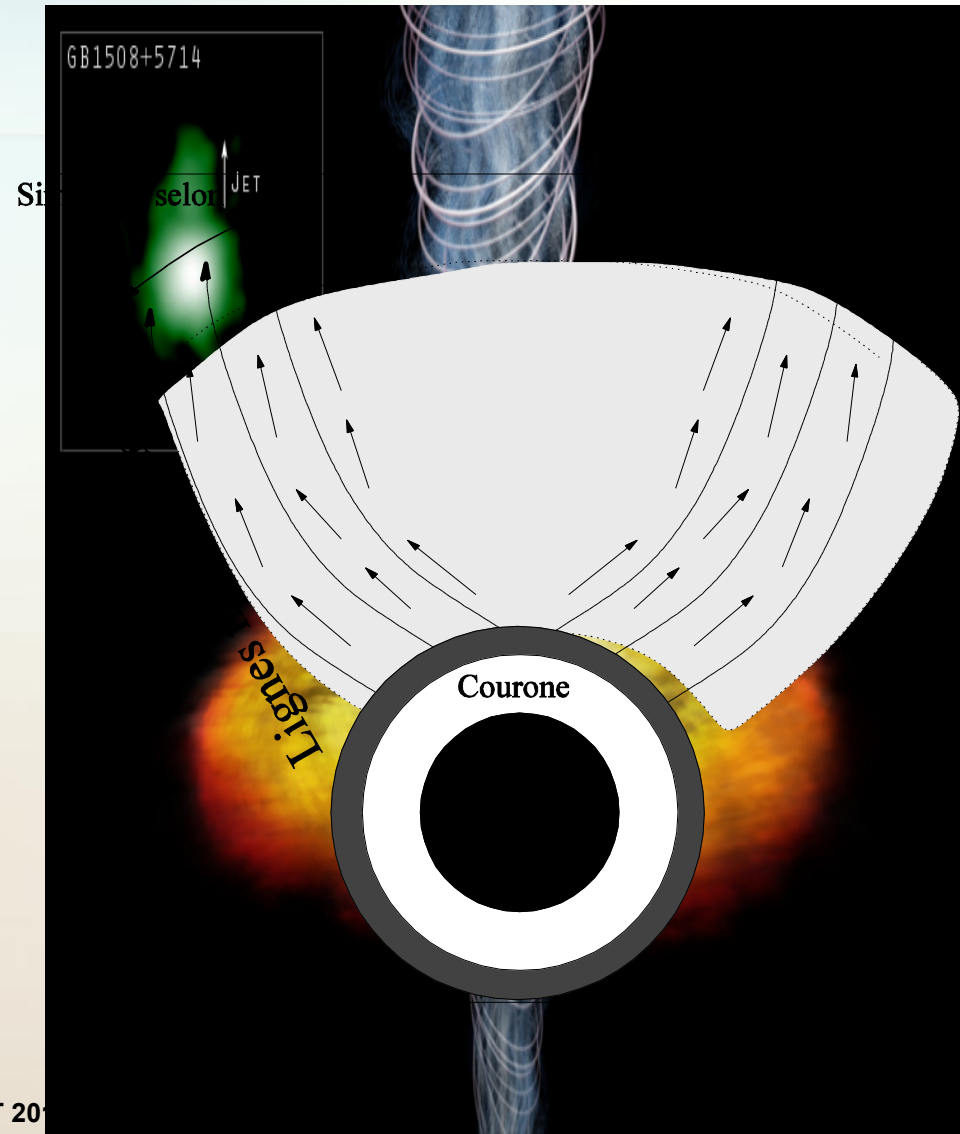
$$\alpha = f(r) \sin^2(\theta)$$

First ordre in  $\alpha$

$P \sim (1 + \kappa \alpha) = (\text{pression})$

$n \sim (1 + \delta \alpha) = (\text{densité})$

$\Omega \sim \lambda / \sqrt{1 + \delta \alpha} = (\text{rotation})$



# GRMHD equations

## Stationnary GRMHD equations 3+1

$$\nabla \cdot (h\gamma n V) = 0.$$

$$\gamma n (V \cdot \nabla) \left( \frac{\gamma w V}{c^2} \right) = -\gamma^2 n w \nabla \ln h - \nabla P + \rho_e E + \frac{J_e \times B}{c},$$

$$n V \cdot \nabla w = V \cdot \nabla P.$$

$$\nabla \cdot E = 4\pi \rho_e,$$

$$\nabla \cdot B = 0,$$

$$\nabla \times (hE) = 0,$$

$$\nabla \times (hB) = \frac{4\pi h}{c} J_e,$$

$$E = -\frac{V \times B}{c}.$$

Pressure along the rotation axis

$$\frac{d\Pi}{dR} = -\frac{2}{h^2} \frac{1}{G^4} \left( \frac{dM^2}{dR} + \frac{F-2}{R} M^2 \right) - \frac{1}{h^4 R^2 M^2} \left( v^2 h_\star^4 - \mu \frac{M^4}{G^4} \right),$$

Alfven Number

$$\frac{dM^2}{dR} = \frac{\mathcal{N}_M}{\mathcal{D}},$$

Streamline expansion

$$\frac{dF}{dR} = \frac{\mathcal{N}_F}{\mathcal{D}},$$

ODE

Radial function

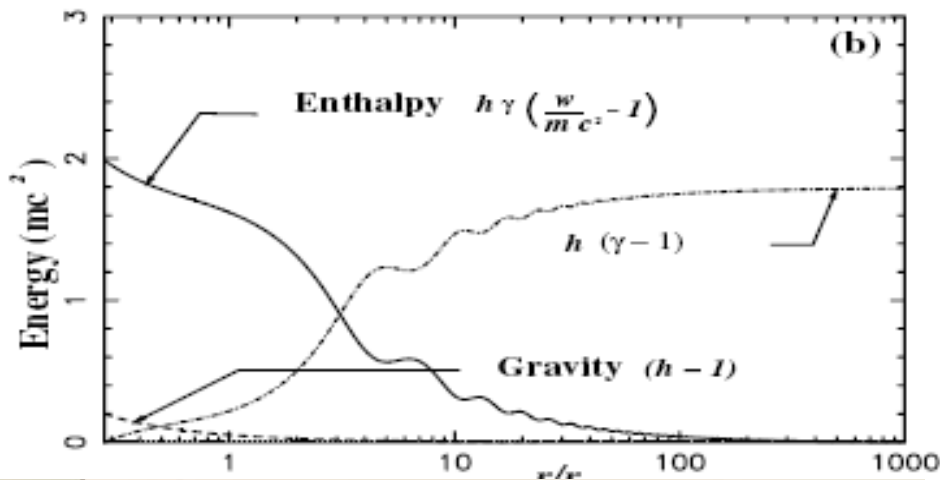
# Thermal and magnetic acceleration

Curvature function of the space-time

$$\mathcal{E} = h\gamma w - h \frac{\varpi \Omega}{\Psi_A} B_\varphi,$$

Enthalpy

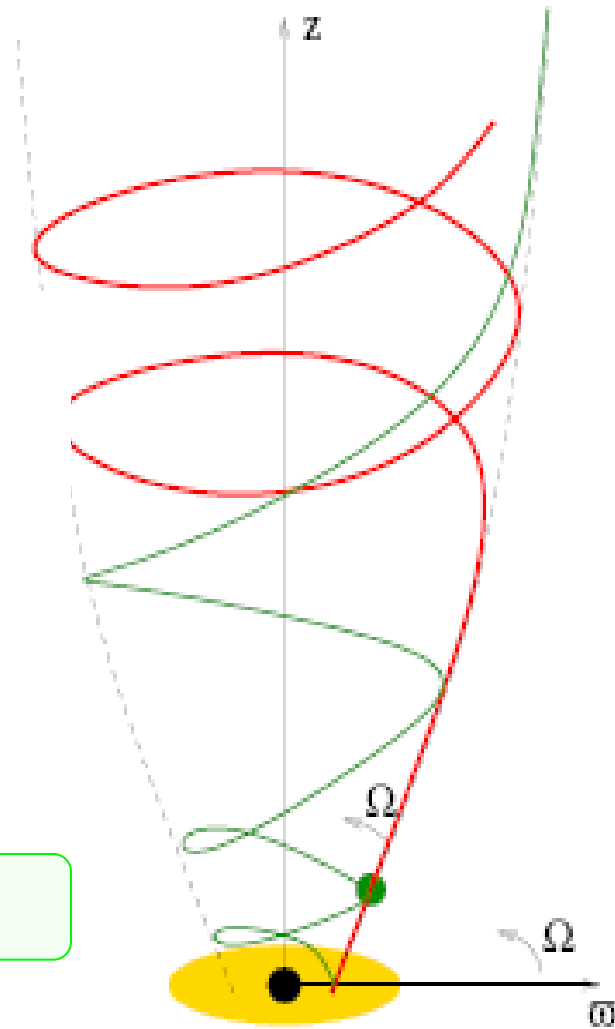
Poynting flux



Magnetic acceleration: Alfven Surface

After Alfven surface

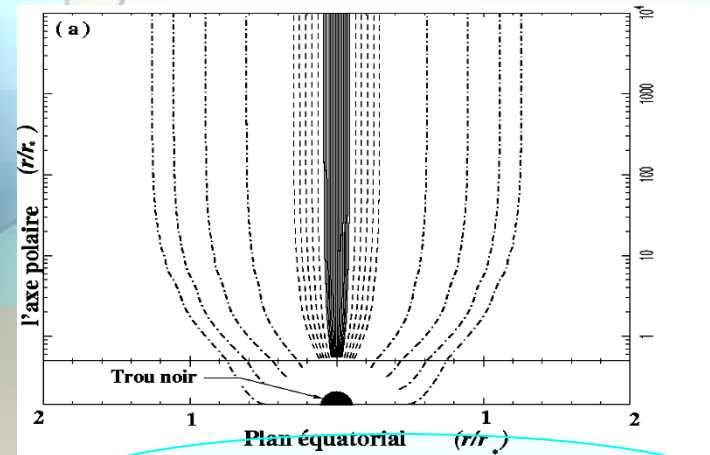
Thermal acceleration : heating



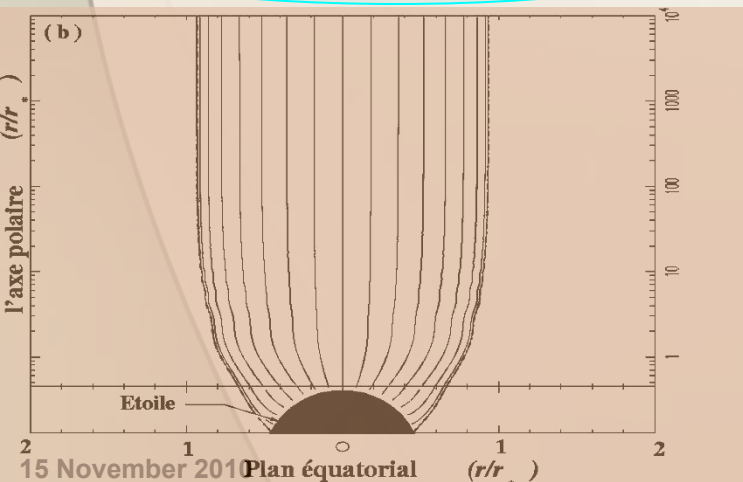
# AGN-YSO jet

- Formation and collimation the jet around schwarzschild BH

Jet- BH



Jet - YSO



Thermal acceleration  
 $\gamma \sim 20$  (heating)  
Magnetic/thermal  
collimation

Relativistic effects

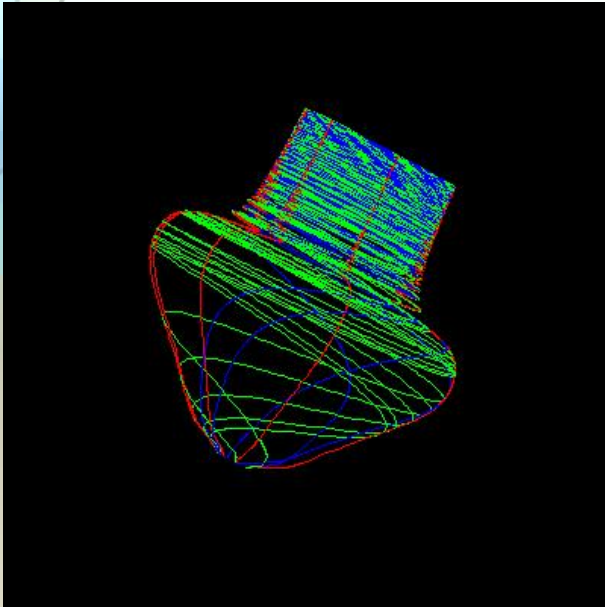
- Decrease of the magnetic collimation efficient
- Enhance the thermal acceleration



# Application

Fanaroff Riley galaxies (Radio galaxies)

Magnetic ligne in 3D



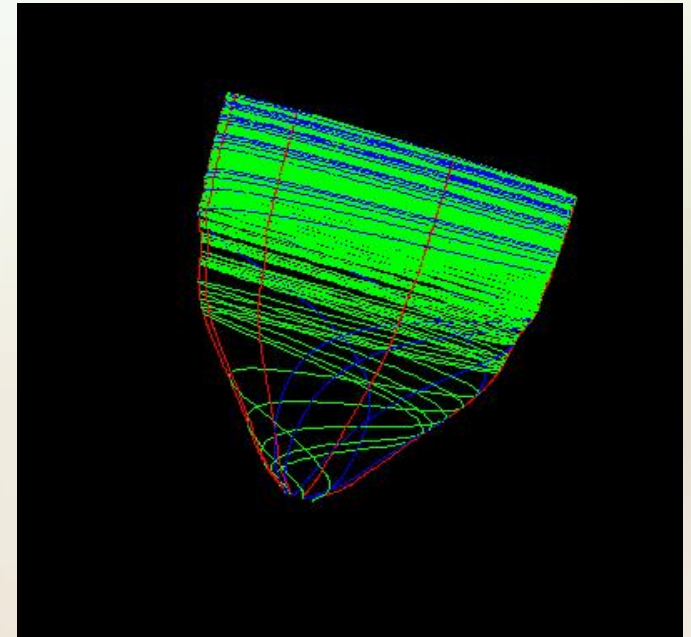
Jet in Fanaroff Riley I galaxies

Collimation by the external pressure

Jet in Fanaroff Riley II galaxies

Magnetic collimation

Quantity of the Poynting flux ejected in the jet



Magnetic ligne in 3D

# Conclusion

- **The disk coroneae has sub-Kepler rotation**
- **The difference YSO/AGN jets are not only scaling**
  - **Special relativity : decreases the efficiency of the Lorentz force to collimate the jet**
  - **General relativity: Enhance the thermal efficiency to accelerate the jet**