

# Pulsar timing and black holes

**Robert Ferdman**  
Jodrell Bank Centre for Astrophysics  
University of Manchester

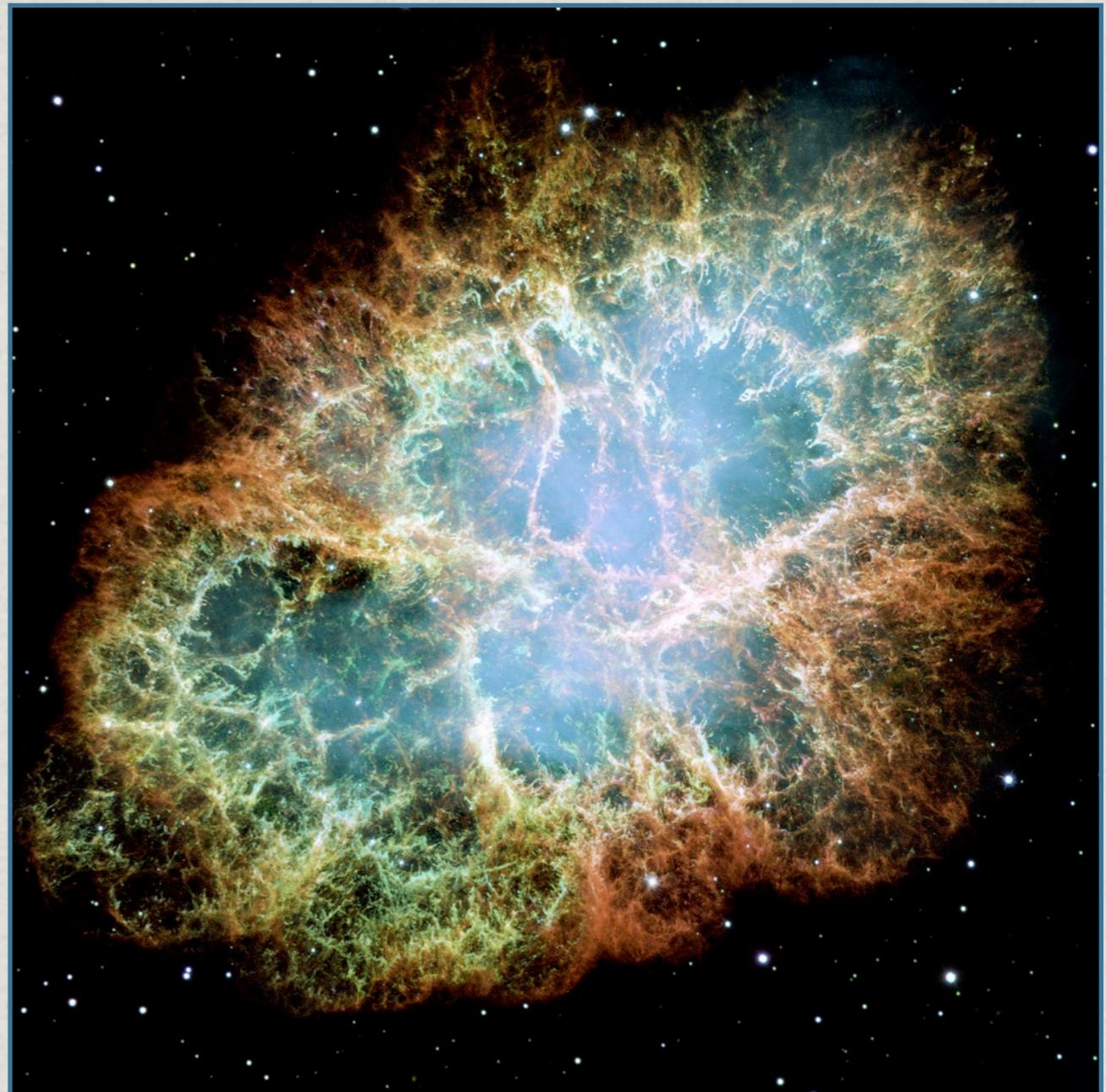
# Born-again stars

Massive stars:  $\sim 8\text{-}15 M_{\odot}$

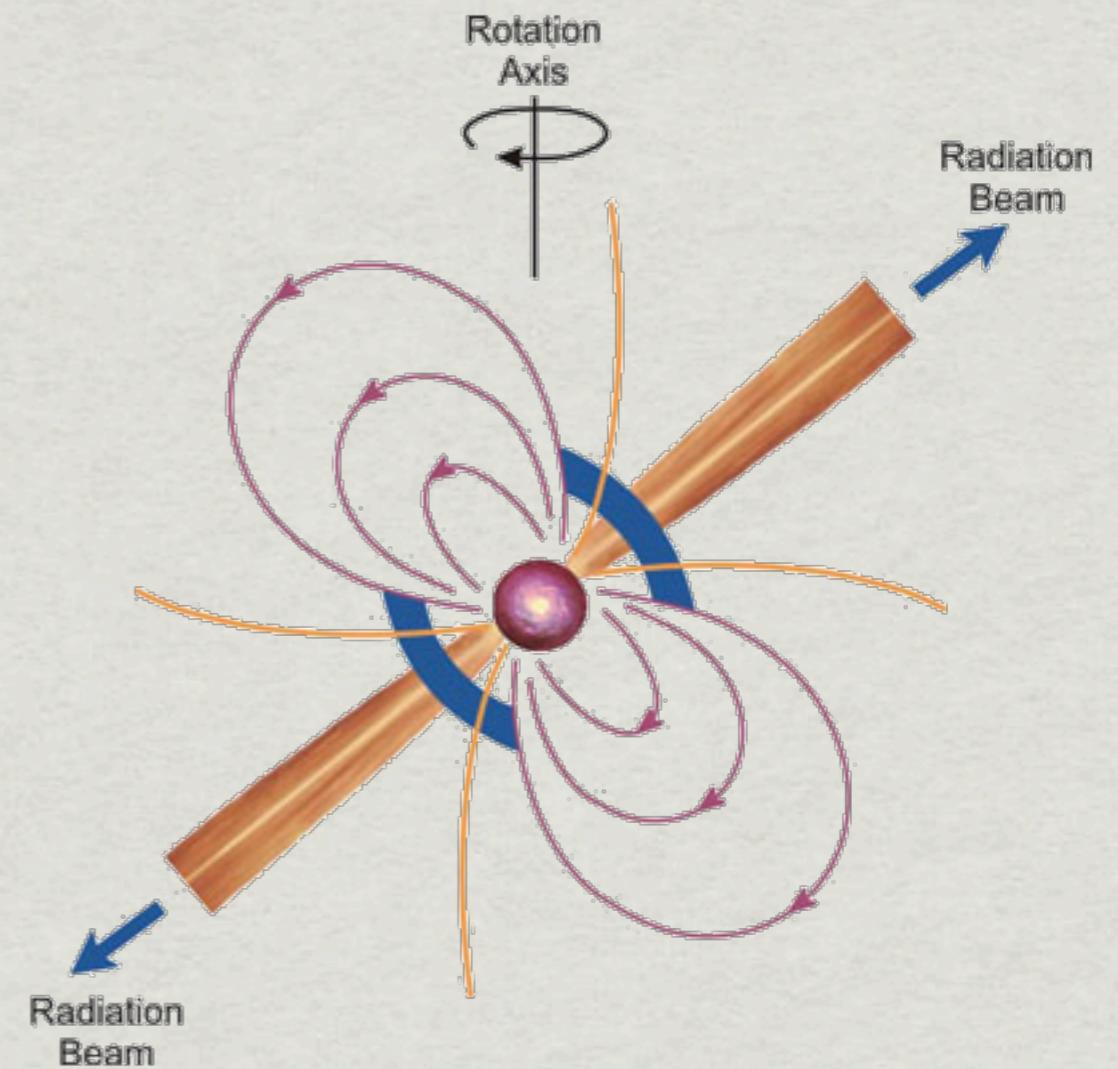
- \* core collapse SN
- \* others?

Neutron star remnant

- \* nuclear densities  
→ highly exotic conditions!
- \* mass  $\sim 1.4 M_{\odot}$
- \* radius  $\sim 10 \text{ km}$
- \* strong magnetic field!



# Pulsars: cosmic lighthouses



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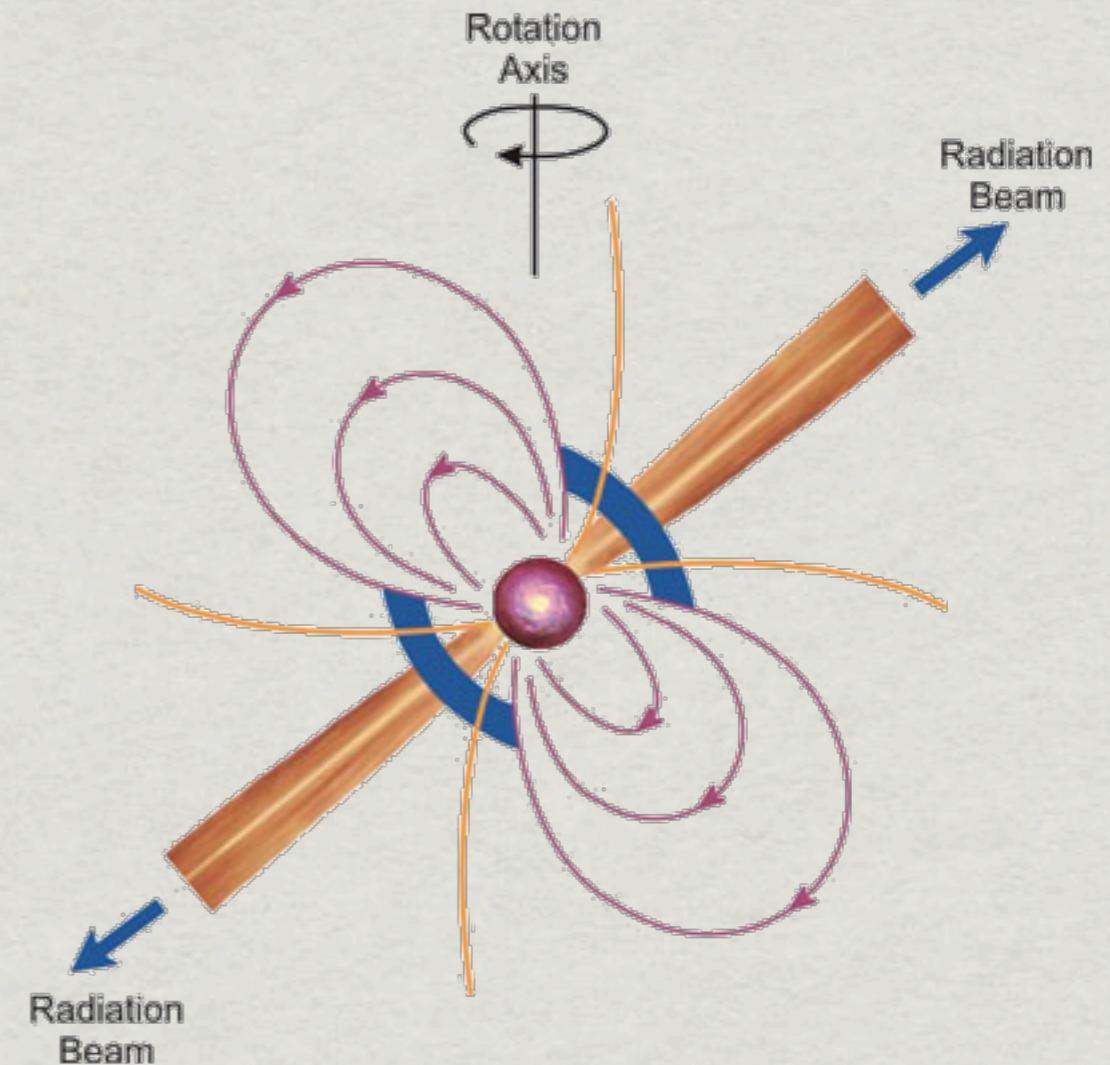
Spin axis, magnetic axis not aligned

- \* each rotation → pulse

Spins on axis once every  
~ms-sec

**Spin down**

- \* magnetic dipole radiation
- \* at the expense of rotational energy



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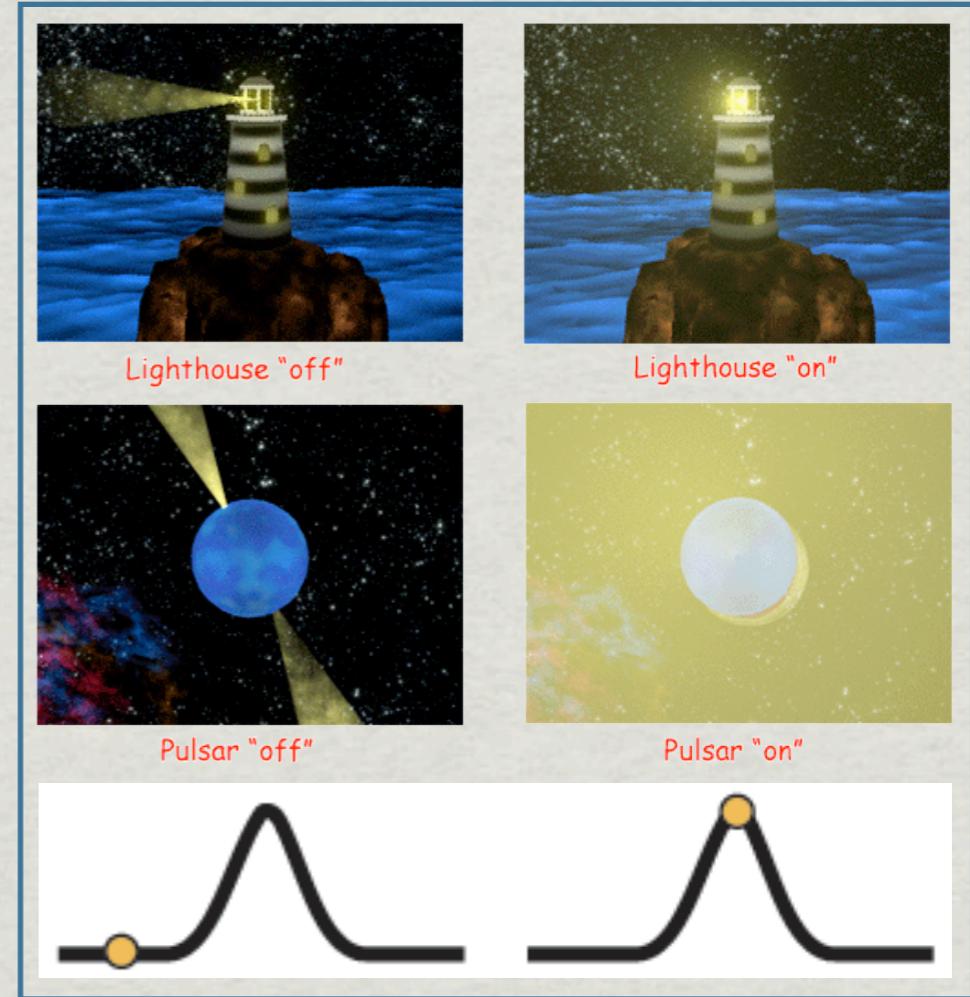
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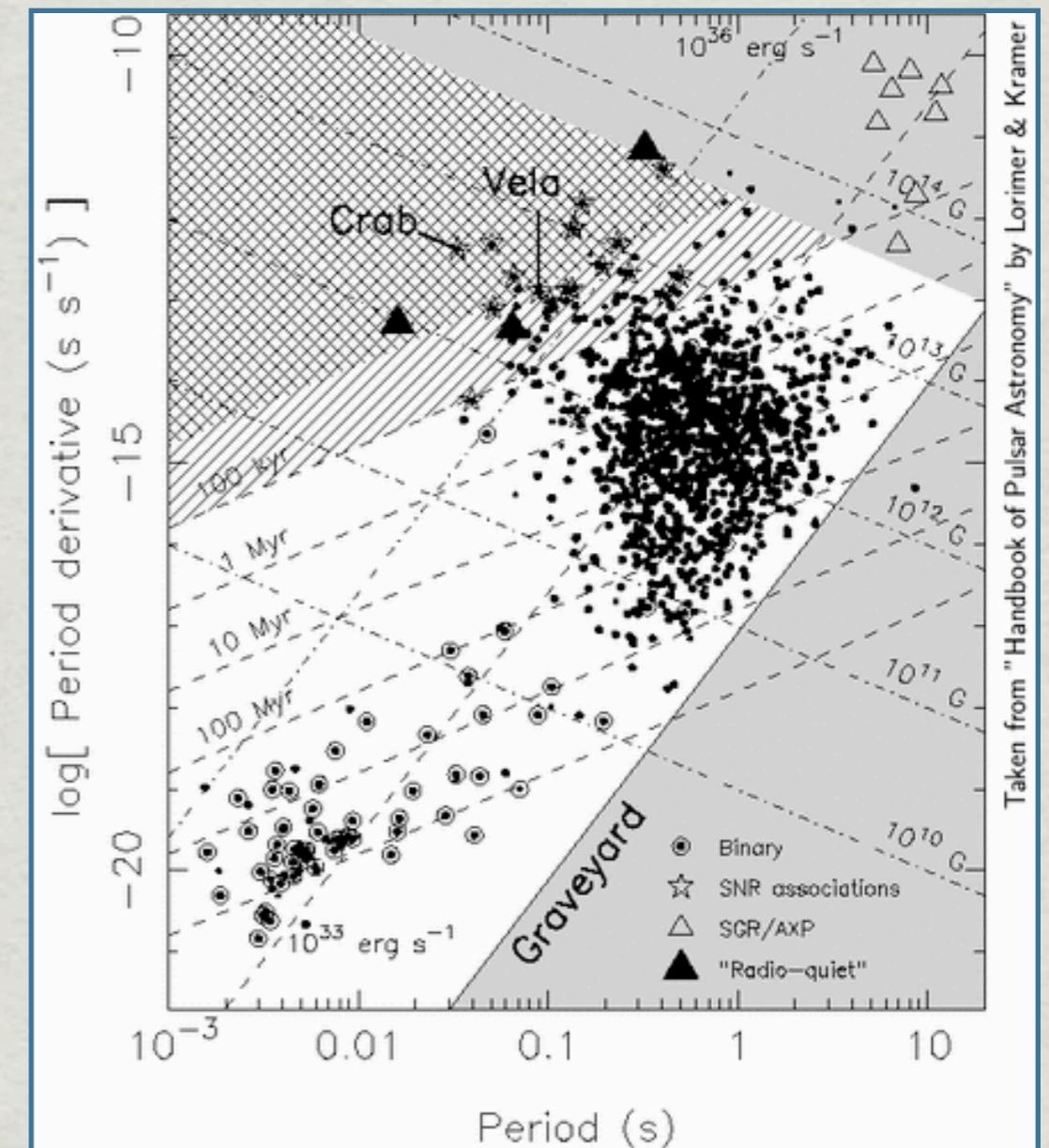
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# Pulsars: cosmic lighthouses

Two principal populations:  
young vs. recycled

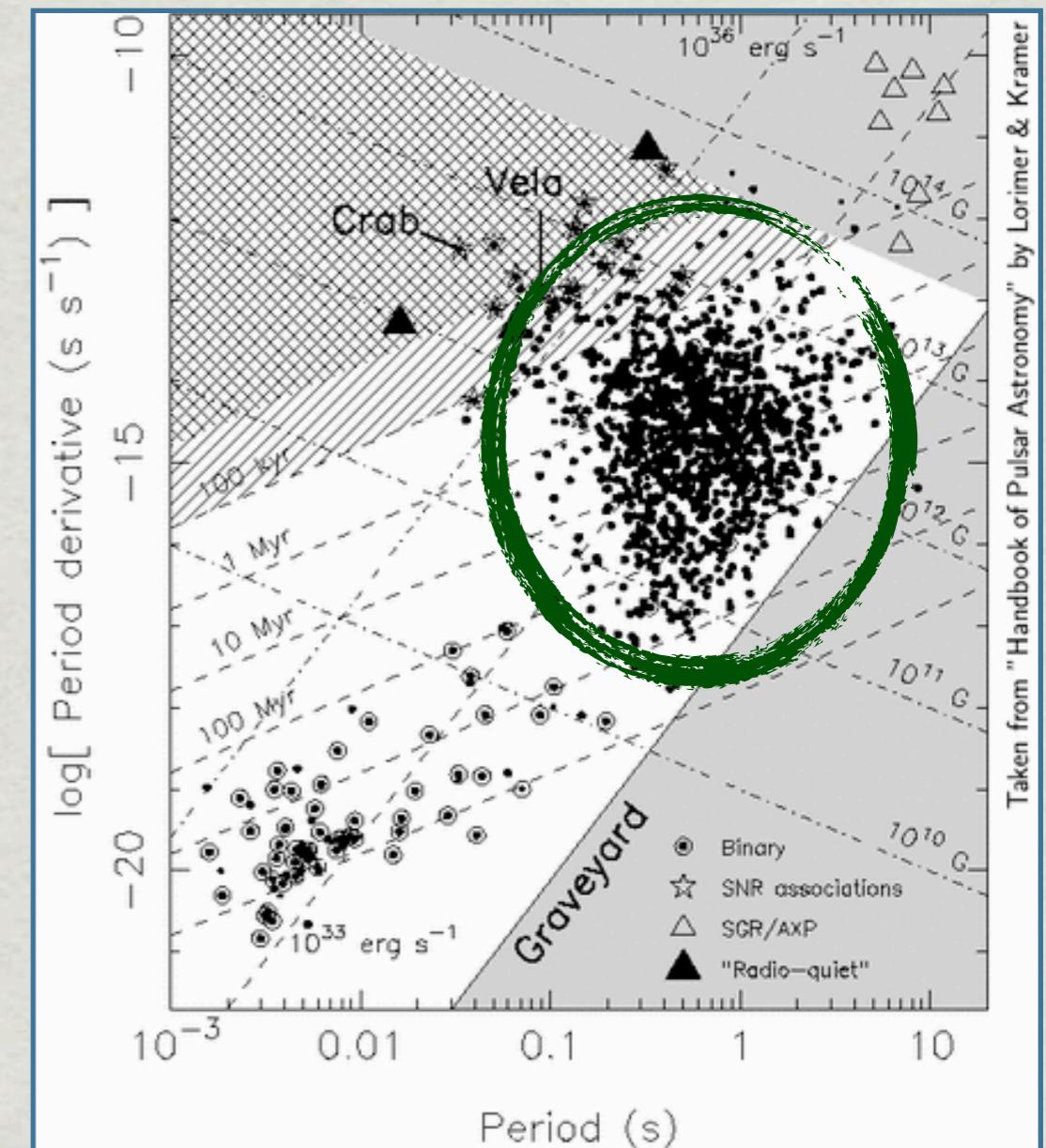
- \* **young** (age  $\sim 10^5 - 10^8$  yr)
  - $\rightarrow P \sim 10^{-15}$  s/s
  - $\rightarrow B \sim 10^{12}$  G
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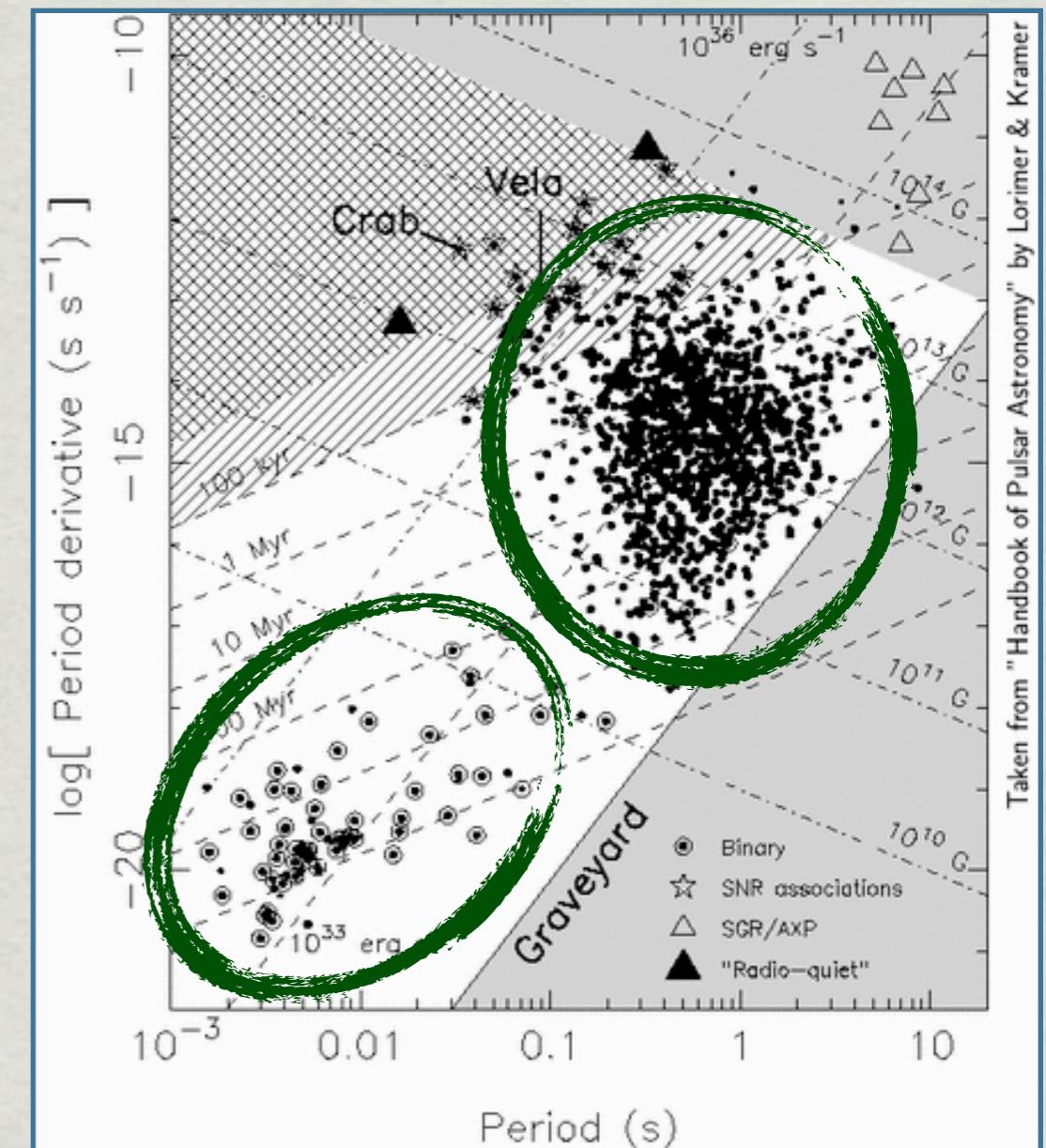
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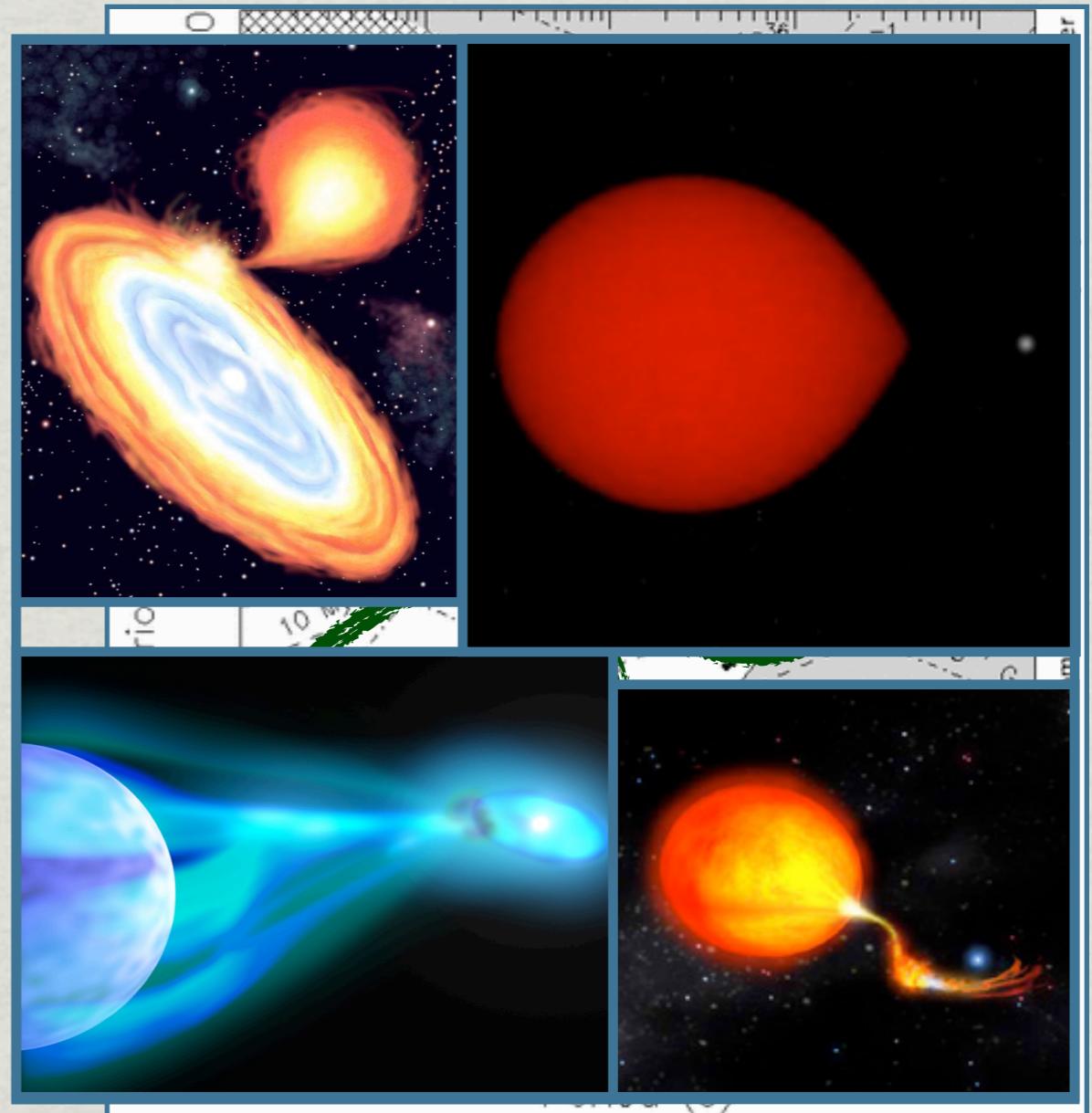


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Spun up due to accretion of  
matter/angular momentum  
from companion



# Pulsar timing in a millisecond

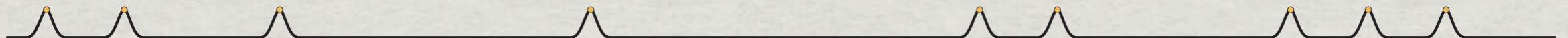
# Pulsar timing in a millisecond



# Pulsar timing in a millisecond

Record pulse times of arrival (TOAs)

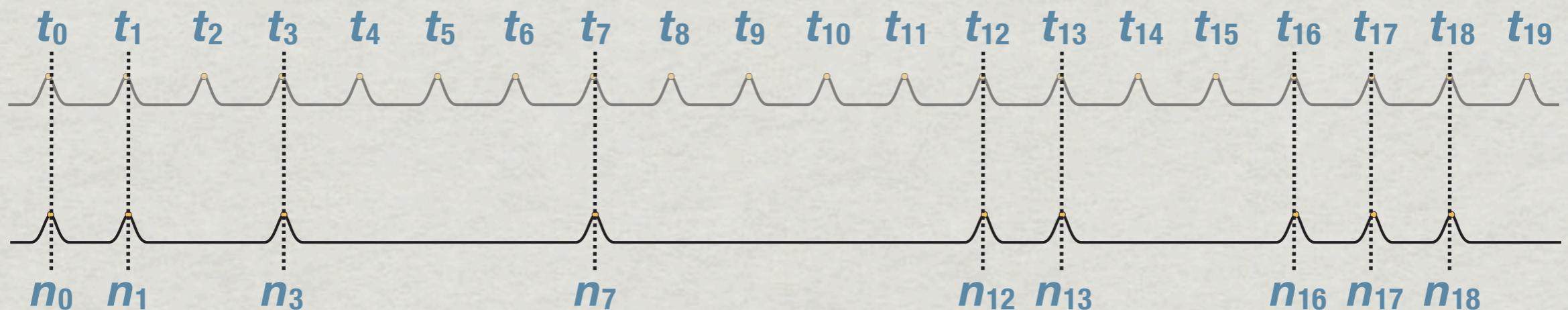
$t_0 \quad t_1 \quad t_2 \quad t_3 \quad t_4 \quad t_5 \quad t_6 \quad t_7 \quad t_8 \quad t_9 \quad t_{10} \quad t_{11} \quad t_{12} \quad t_{13} \quad t_{14} \quad t_{15} \quad t_{16} \quad t_{17} \quad t_{18} \quad t_{19}$



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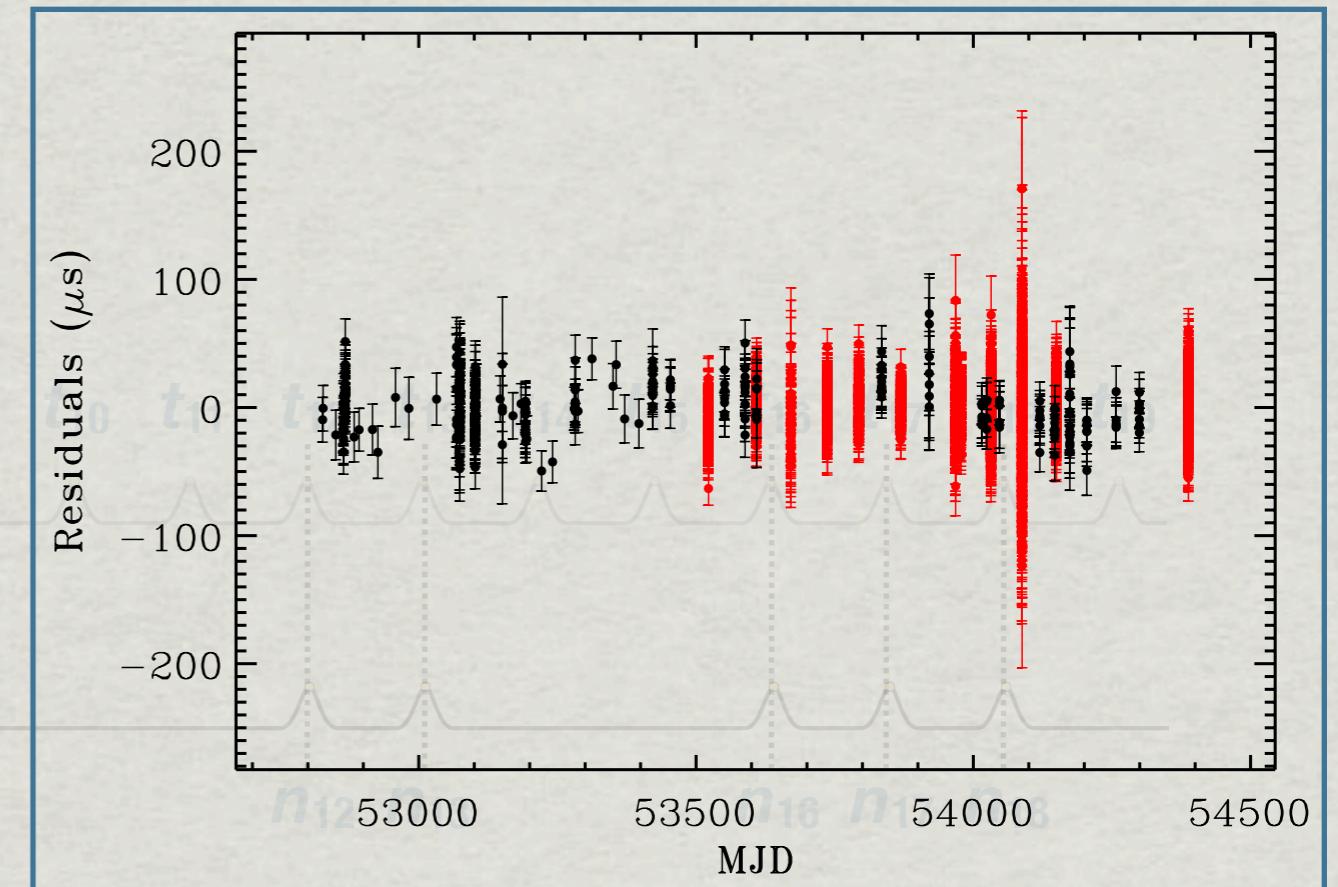
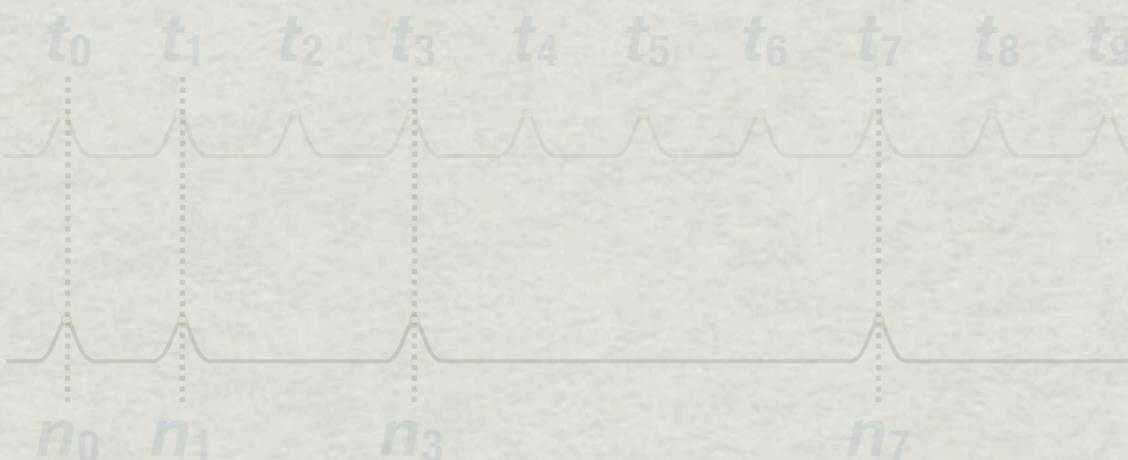
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# Pulsar timing in a millisecond

Record pulse times of arrival (TOAs)

- \* label each incoming pulse based on ephemeris
- \* new data → update model
- \* **timing residuals**  
→ **(observed – model)**

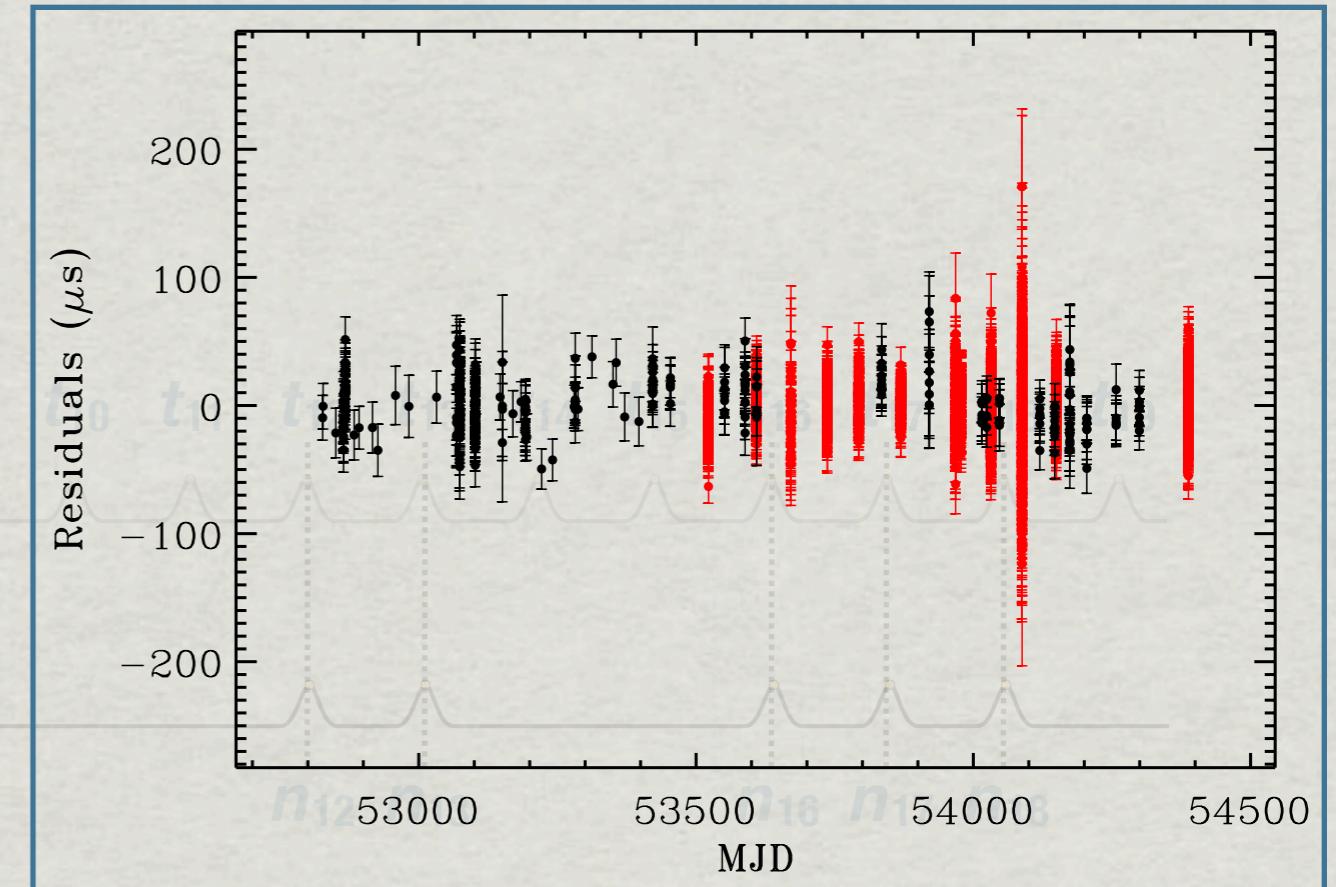
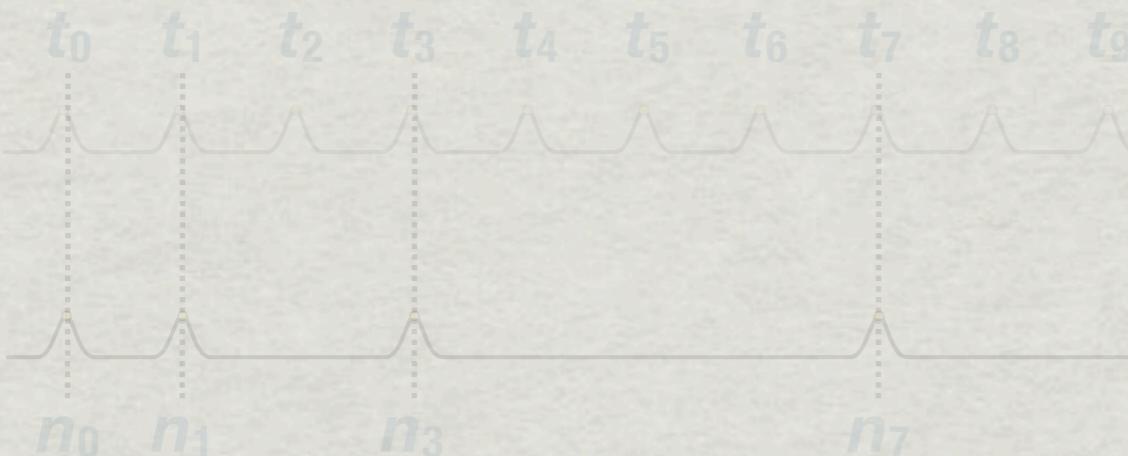


(Ferdman et al., in prep.)

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(Ferdman et al., in prep.)

**Phase connection** → account for each rotation of NS

- \* powerful -- how we get such high timing precision

# What goes into the timing model?

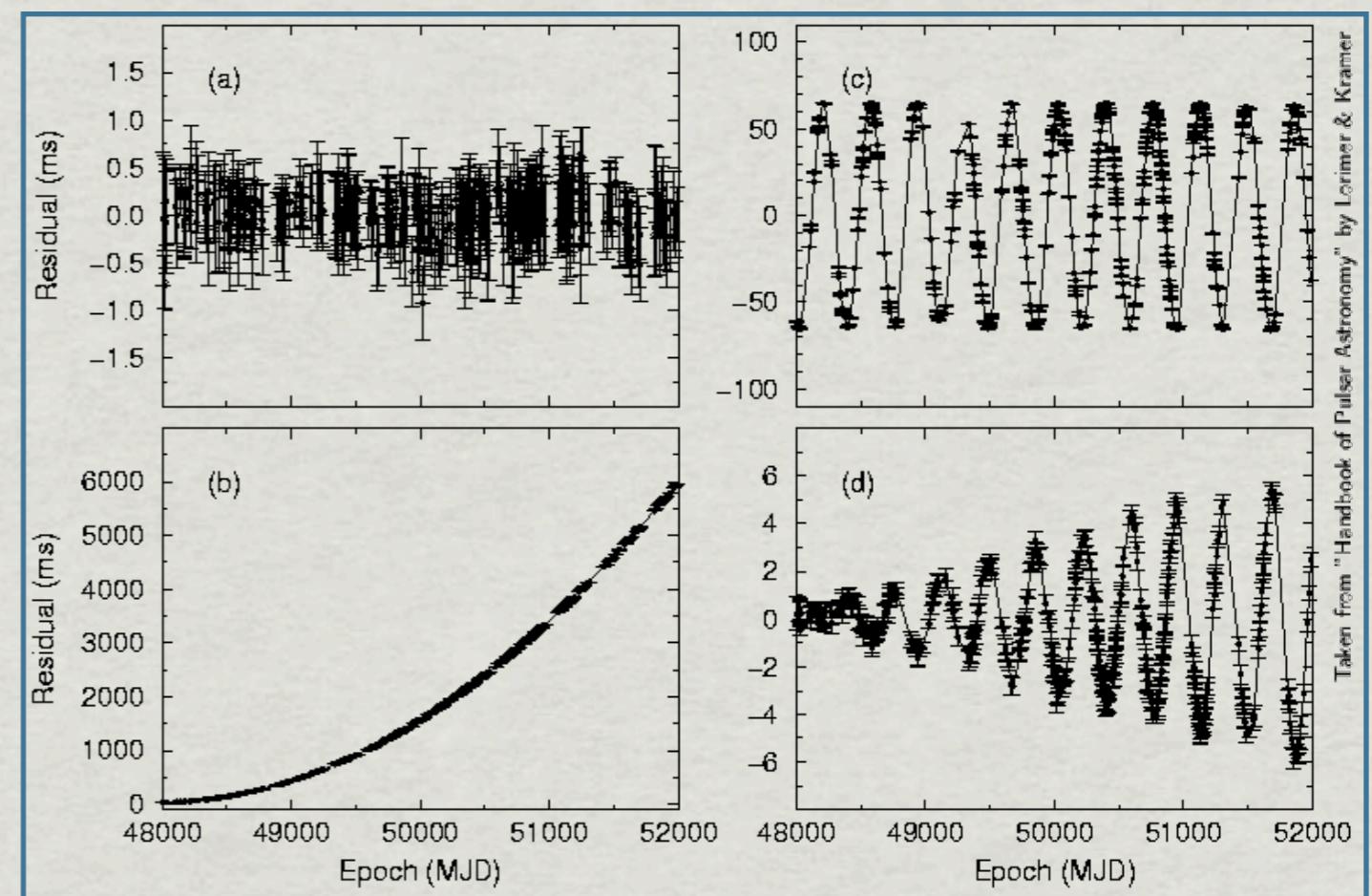
Isolated, slow pulsar

- \* Spin, spin-down
- \* Earth, solar system motions
- \* pulsar position, proper motion
- \* interstellar dispersion

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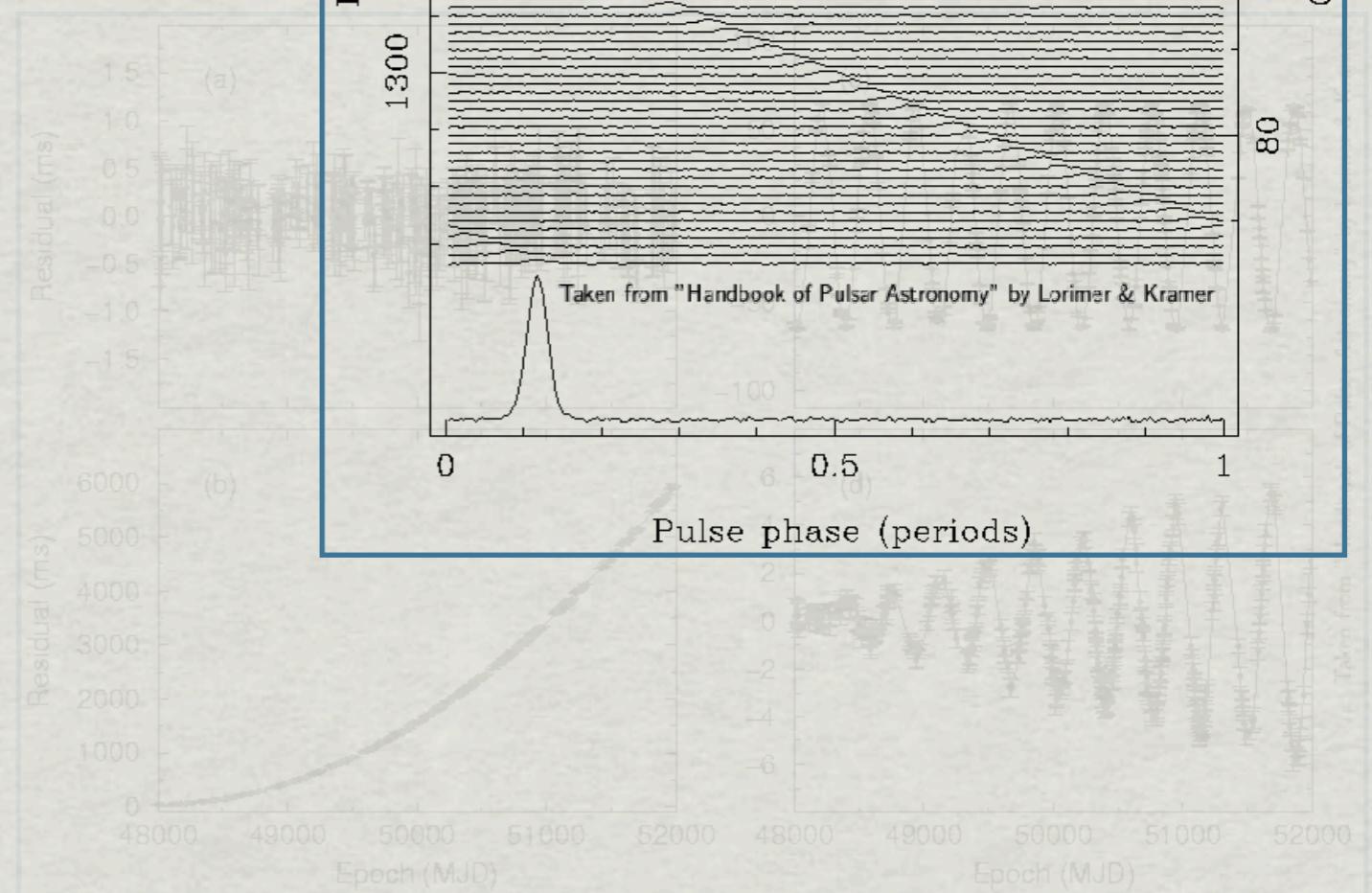
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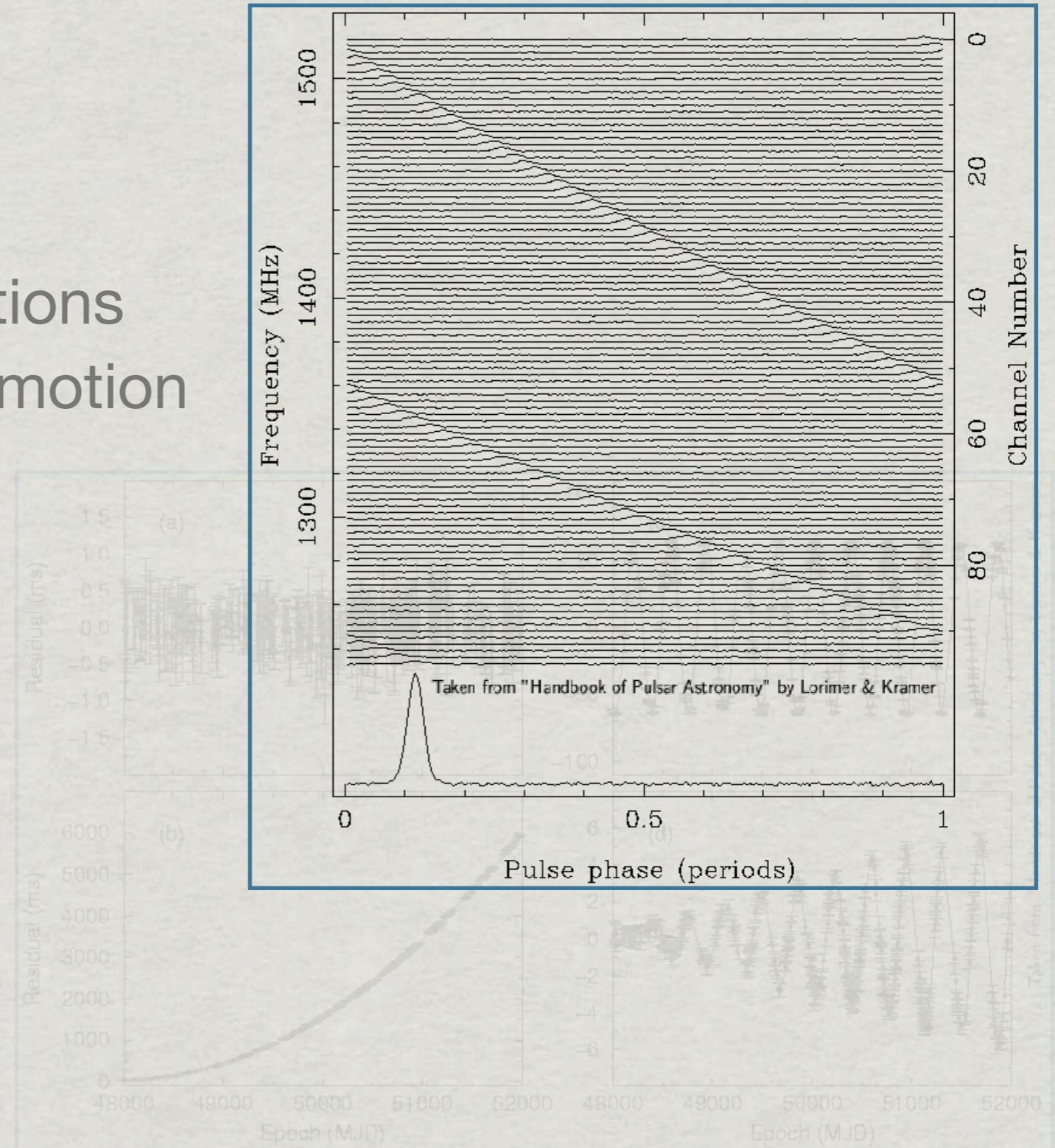


# What goes into the timing model?

Isolated, slow pulsar

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Aim of timing model:  
account for and remove  
each possible delay

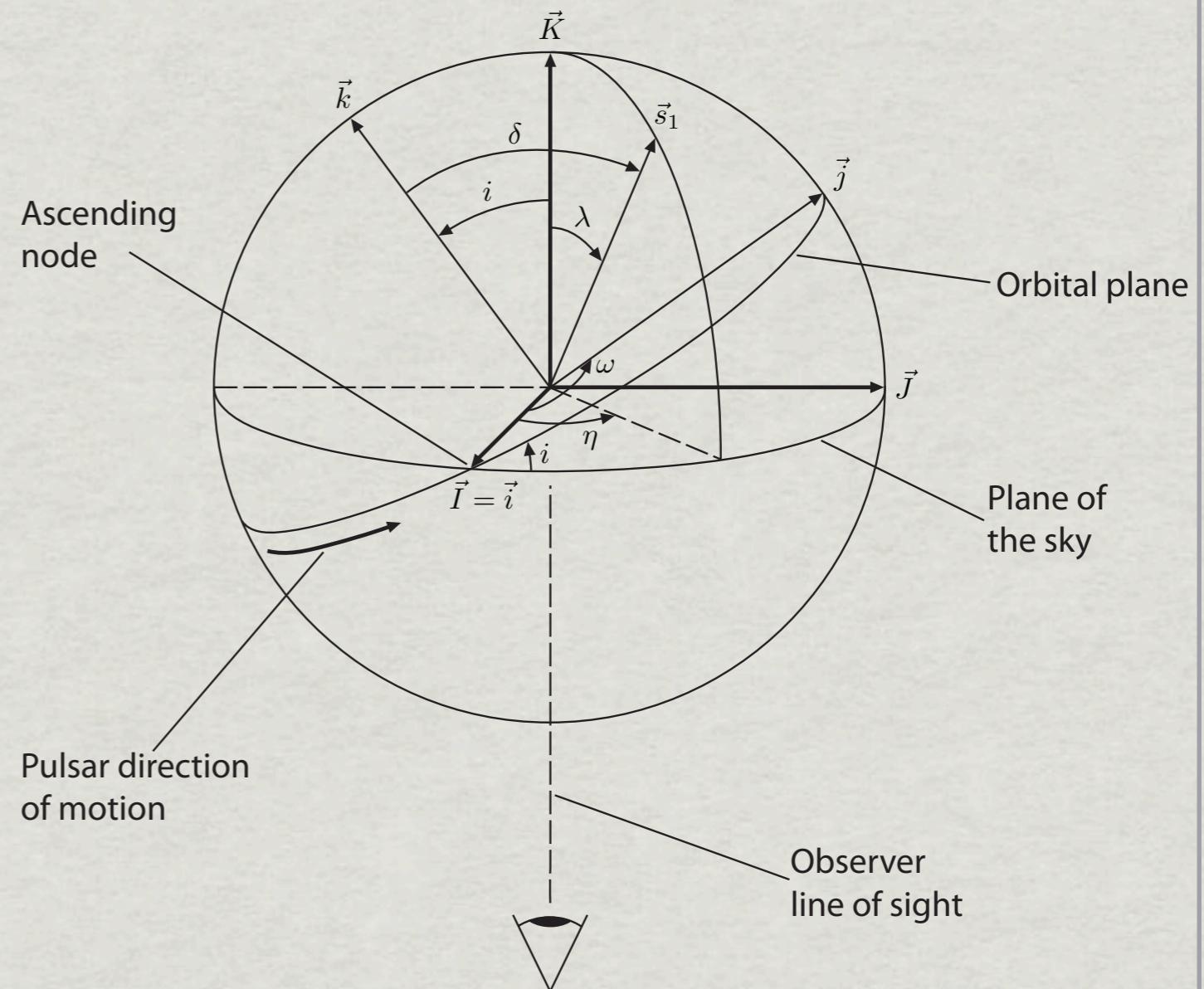


# Pulsar binary systems

More complex → more delays:

## Orbital parameters

- \* orbital period
- \* eccentricity
- \* longitude of periastron
- \* time of periastron passage
- \* projected semimajor axis
- \* if system is relativistic...



# Post-Keplerian parameters

Corrections to Keplerian orbital parameters

PK parameters are theory-independent

Dependencies are different depending on theory of gravity

- \* GR, for example (e.g., Damour & Deruelle 1986; Damour & Taylor 1992, PRD, 45, 1840):

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Dependencies are different depending on theory of gravity

- \* GR, for example (e.g., Damour & Deruelle 1986; Damour & Taylor 1992, PRD, 45, 1840):

$$\dot{\omega} = 3T_{\odot}^{2/3} \left(\frac{P_b}{2\pi}\right)^{-5/3} \frac{1}{1-e^2} (m_1 + m_2)^{2/3}$$

$$\dot{P}_b = -\frac{192\pi}{5} T_{\odot}^{5/3} \left(\frac{P_b}{2\pi}\right)^{-5/3} \left(1 + \frac{73}{24}e^2 + \frac{37}{96}e^4\right) (1-e^2)^{-7/2} \frac{m_1 m_2}{(m_1 + m_2)^{1/3}}$$

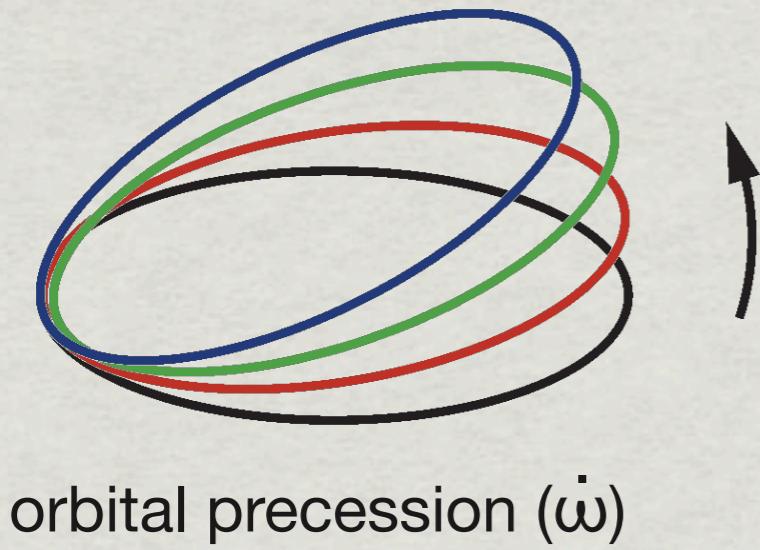
$$\gamma = T_{\odot}^{2/3} \left(\frac{P_b}{2\pi}\right)^{1/3} e \frac{m_2(m_1 + 2m_2)}{(m_1 + m_2)^{4/3}}$$

$$r = T_{\odot} m_2$$

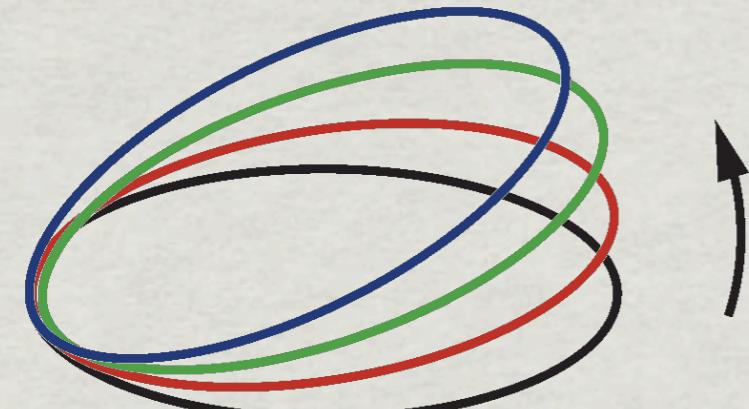
$$s = T_{\odot}^{-1/3} \left(\frac{P_b}{2\pi}\right)^{-2/3} x \frac{(m_1 + m_2)^{2/3}}{m_2} = \sin i$$

# Post-Keplerian parameters

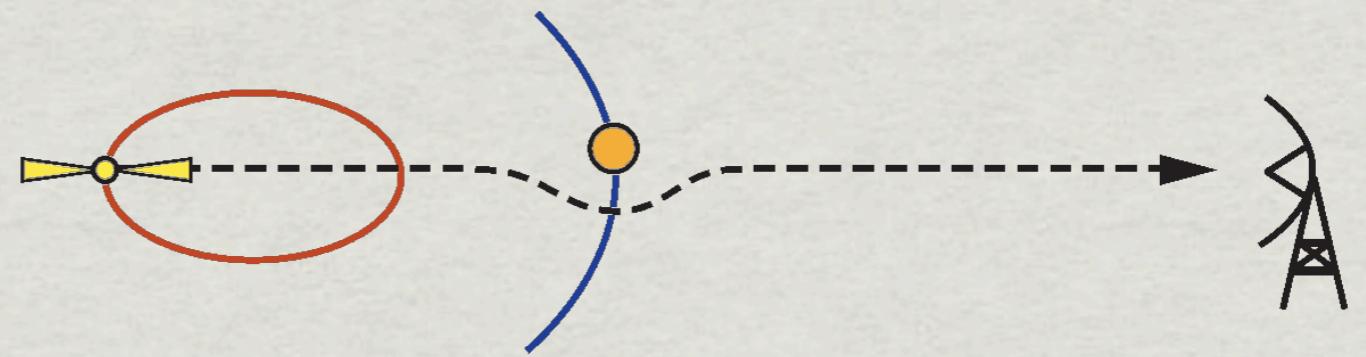
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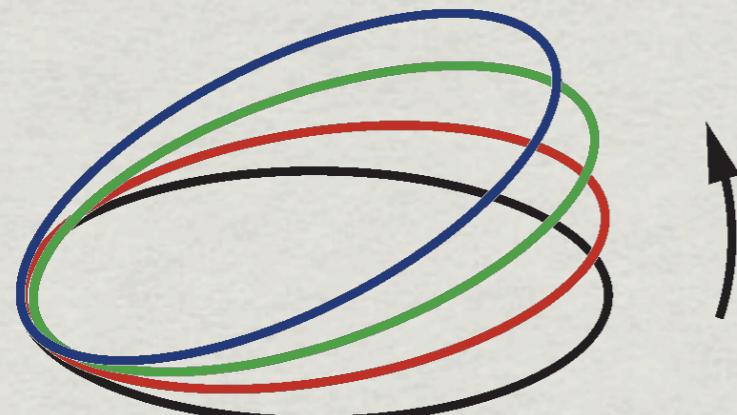


orbital precession ( $\dot{\omega}$ )

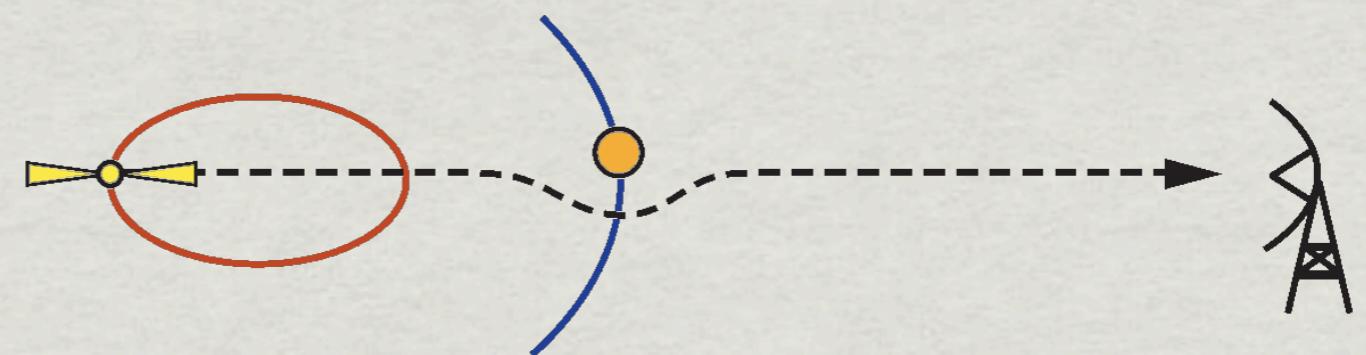


Shapiro delay ( $r, s$ )

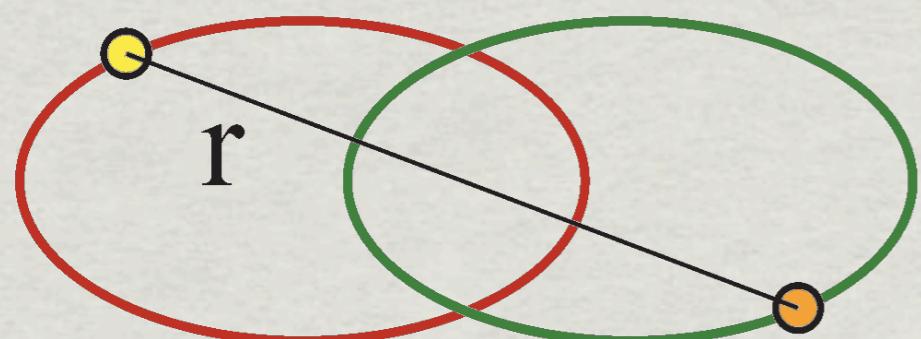
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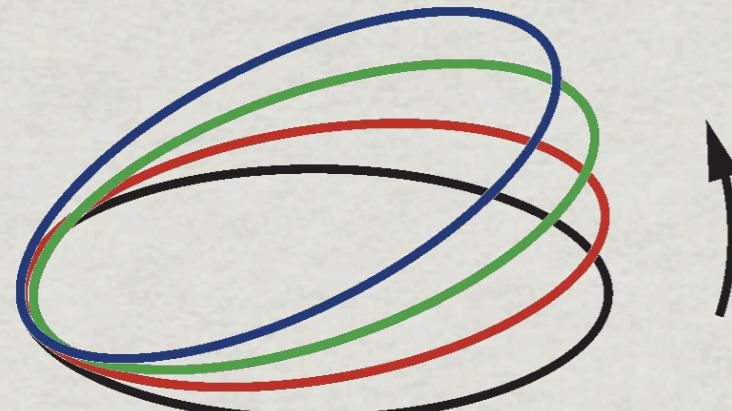


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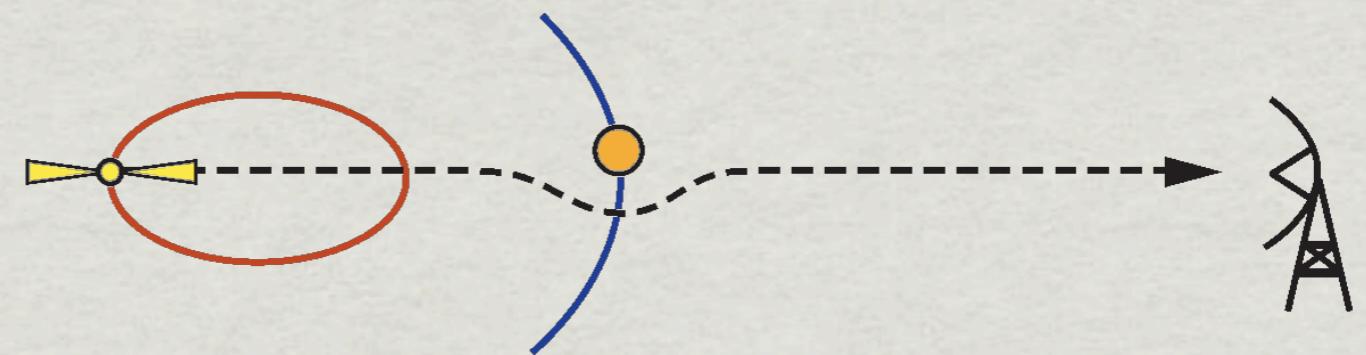


gravitational redshift/  
time dilation ( $\gamma$ )

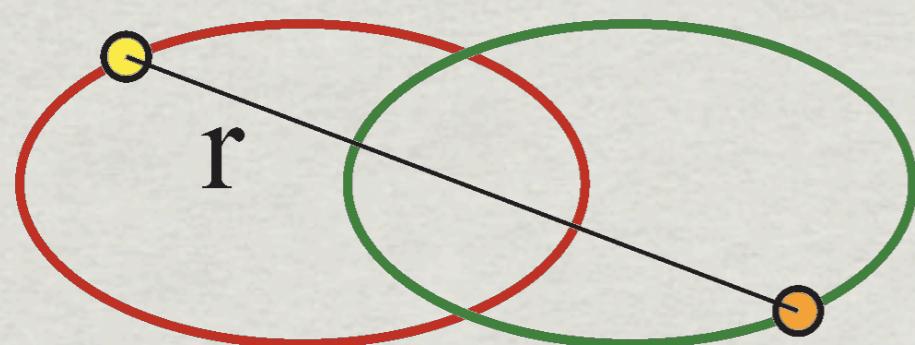
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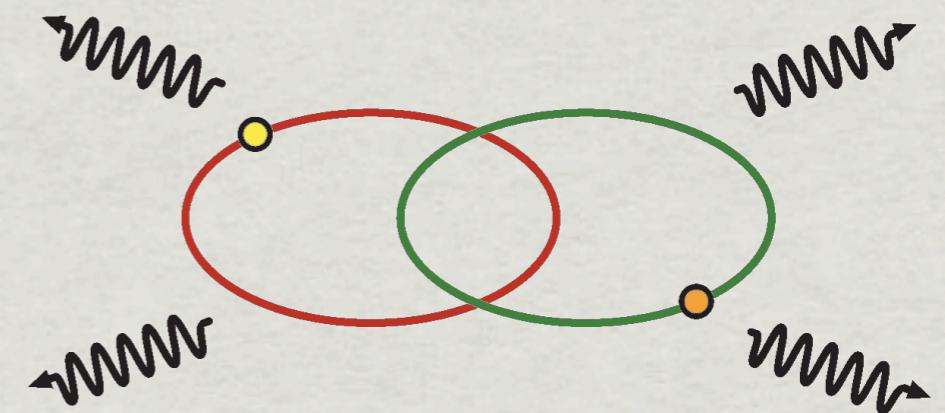
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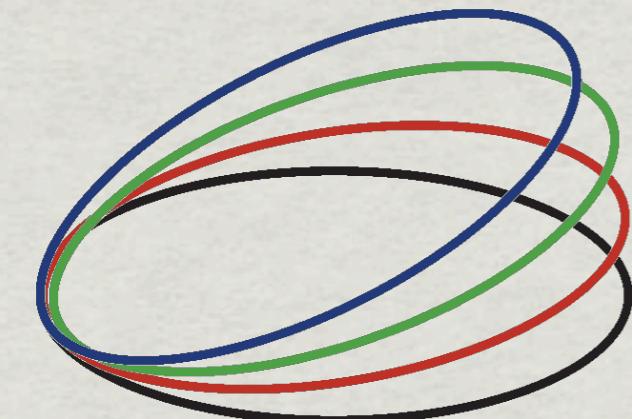


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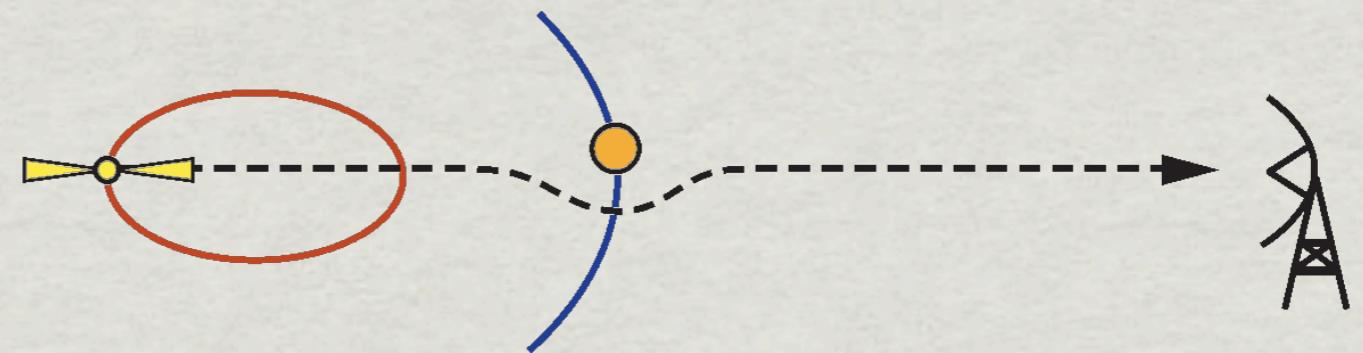


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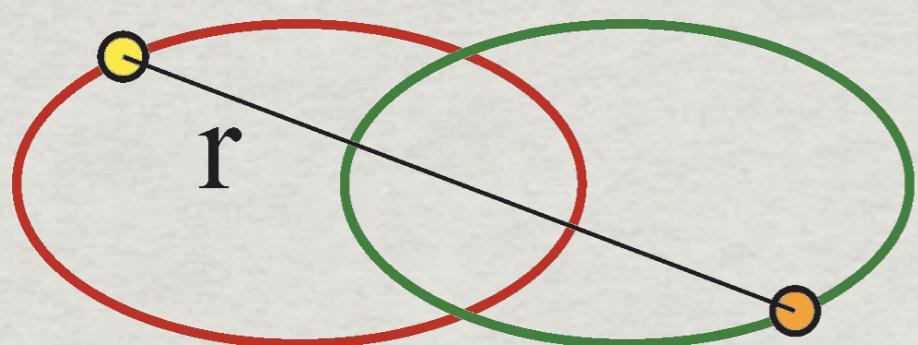


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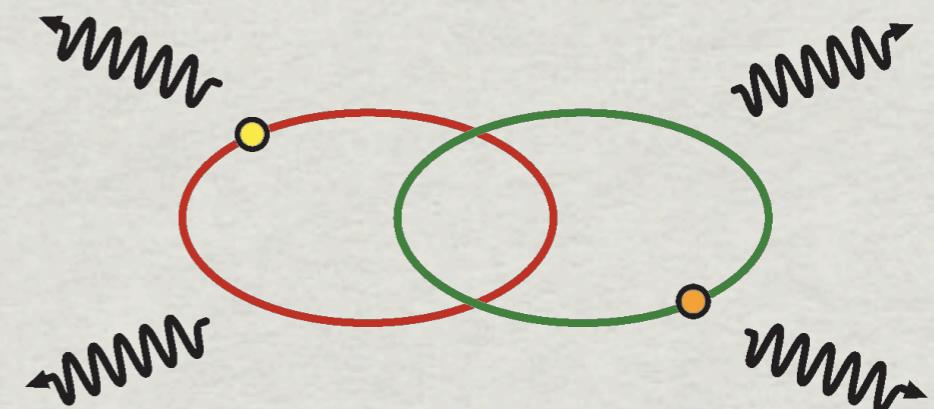


Shapiro delay ( $r, s$ )

Any two  $\Rightarrow$  masses

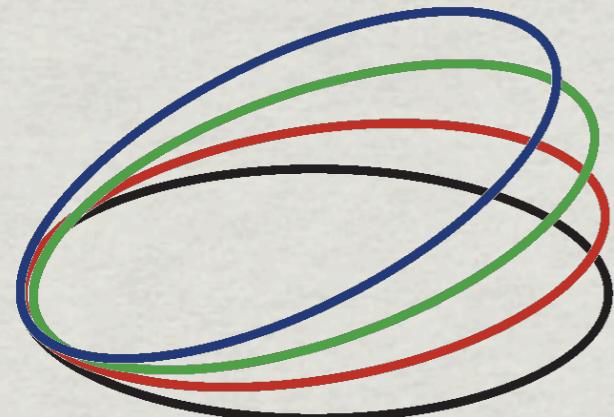


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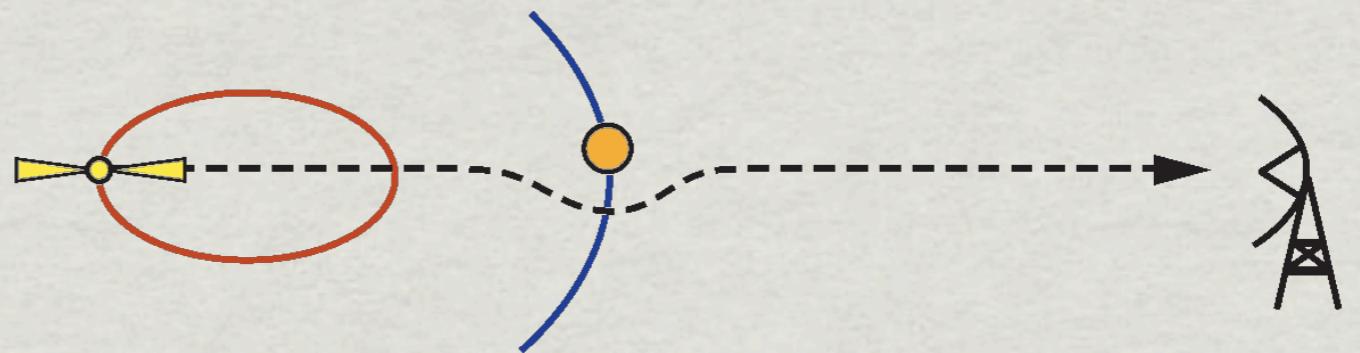


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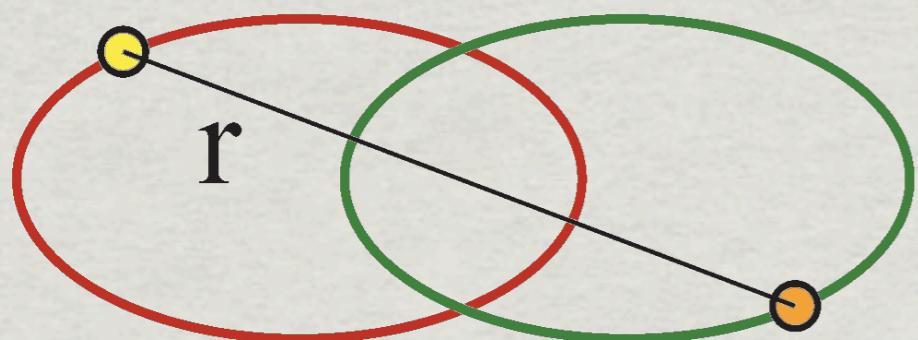
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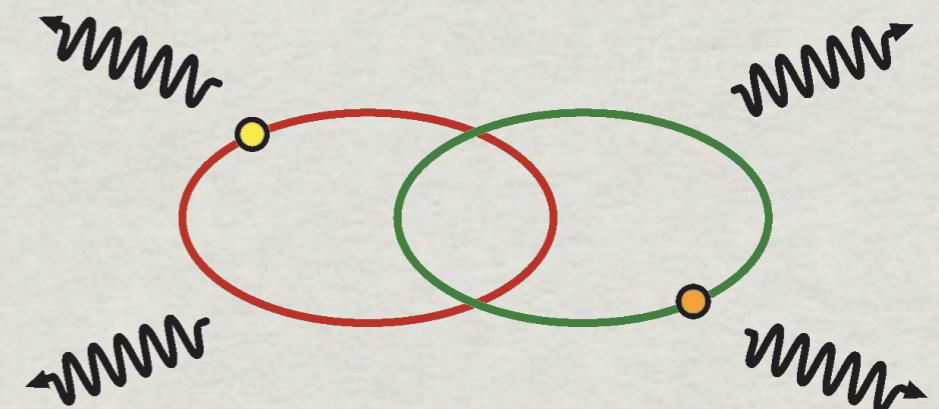
Shapiro delay ( $r, s$ )

Any two  $\Rightarrow$  masses

$\geq$  three  $\Rightarrow$  GR test

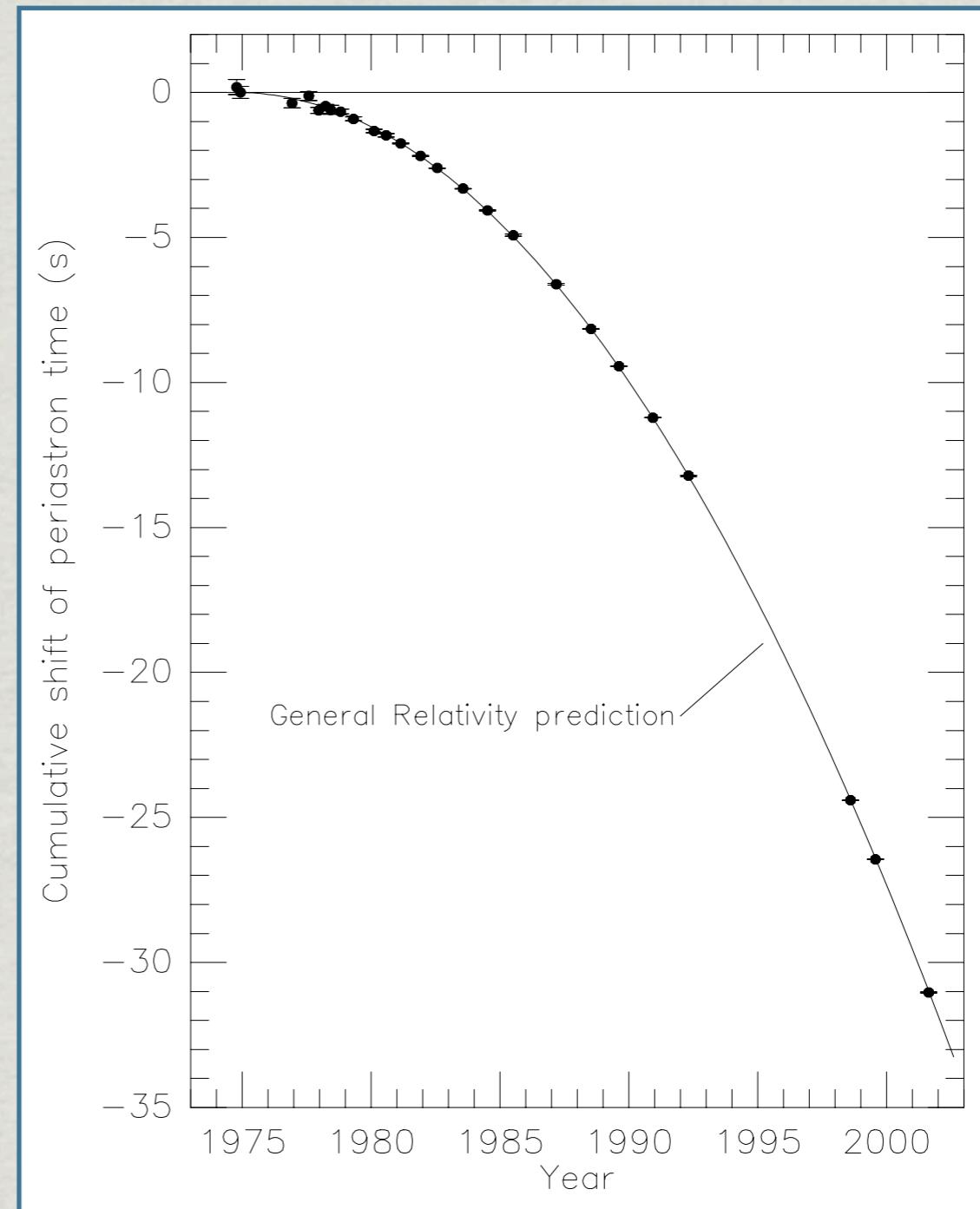


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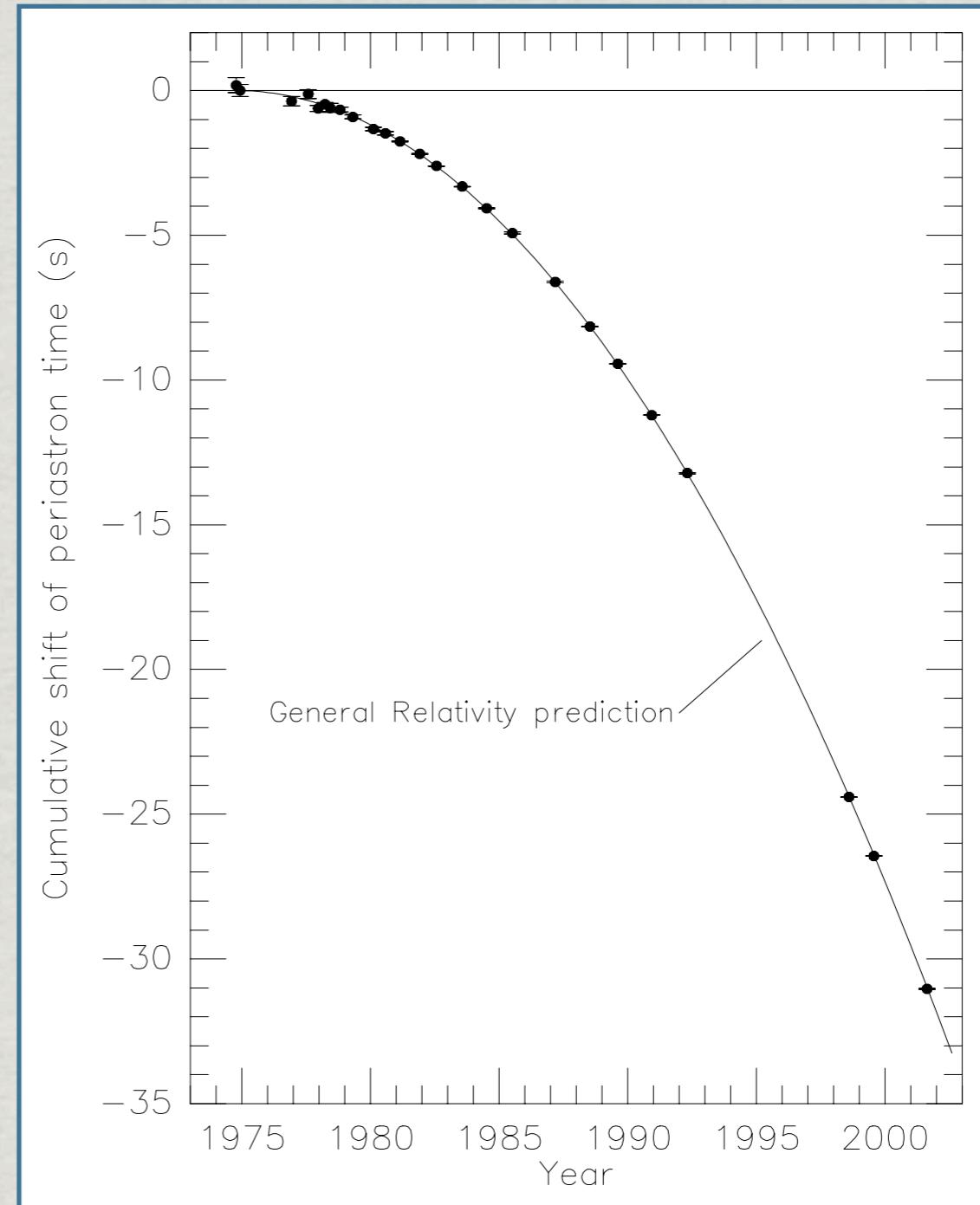
# Pulsars as GR probes



J. Weisberg, private communication

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GR tests since  
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binary pulsar:



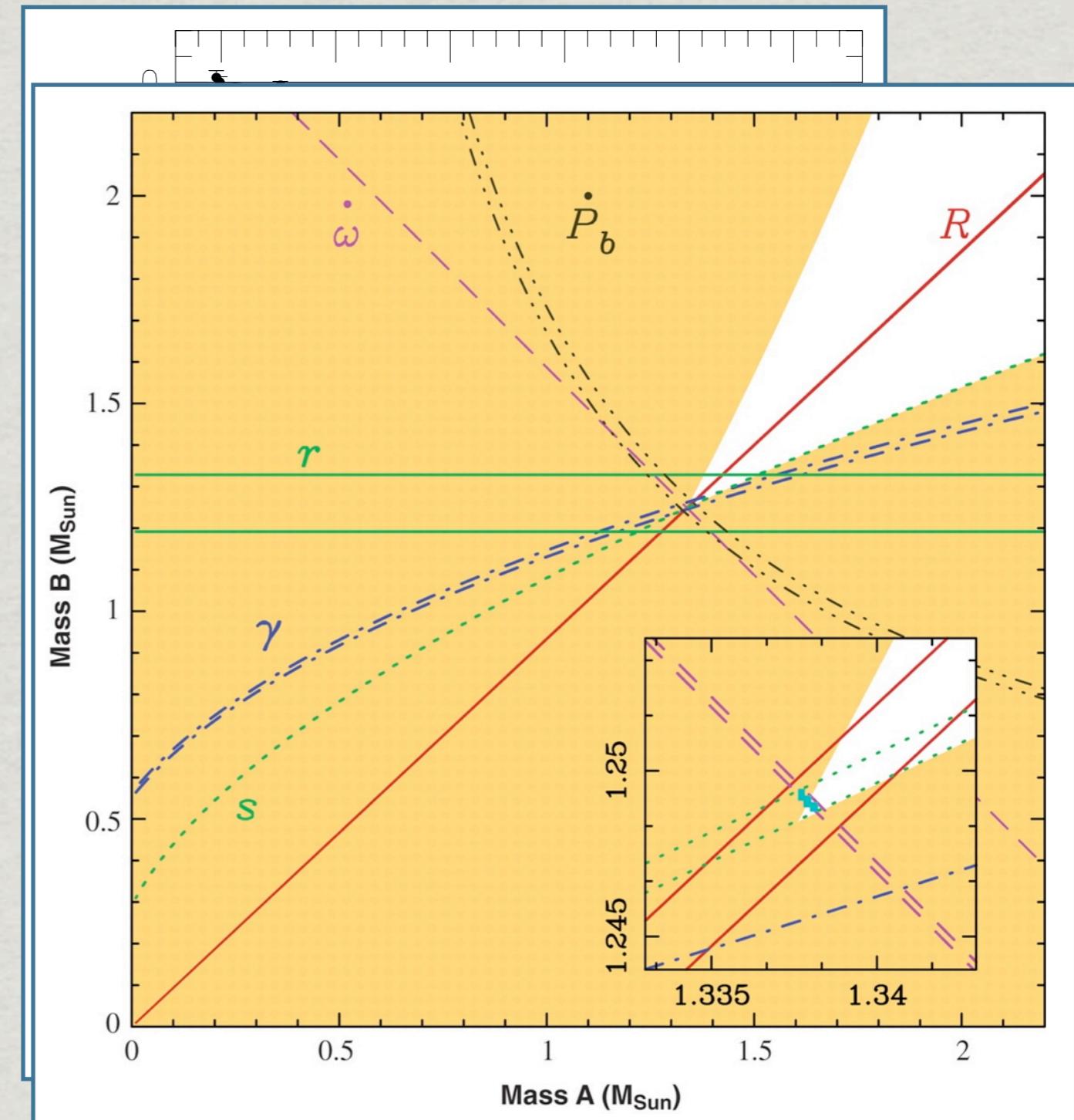
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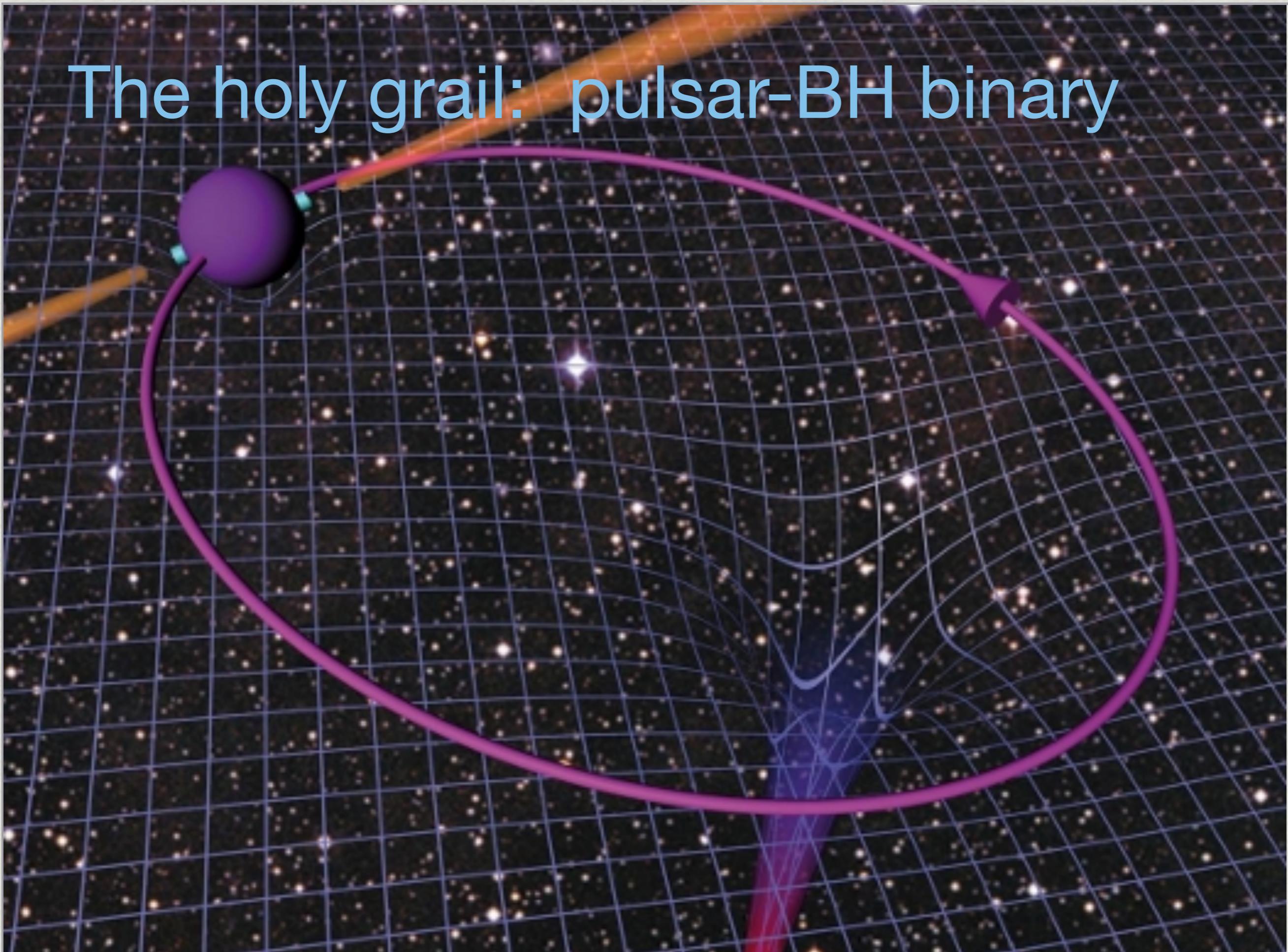
Double pulsar  
PSR J0737–3039A/B

- \* Shapiro delay  $s$  consistent to within 0.05%
- \* most precise strong-field test



Kramer et al. 2006, Science, 314,

# The holy grail: pulsar-BH binary



# The holy grail: pulsar-BH binary

## Further GR tests

- \* beyond first-order PN corrections, dipole radiation, ...

## Black hole/system properties

- \* mass
- \* spin-orbit coupling
- \* effects of BH quadrupole moment

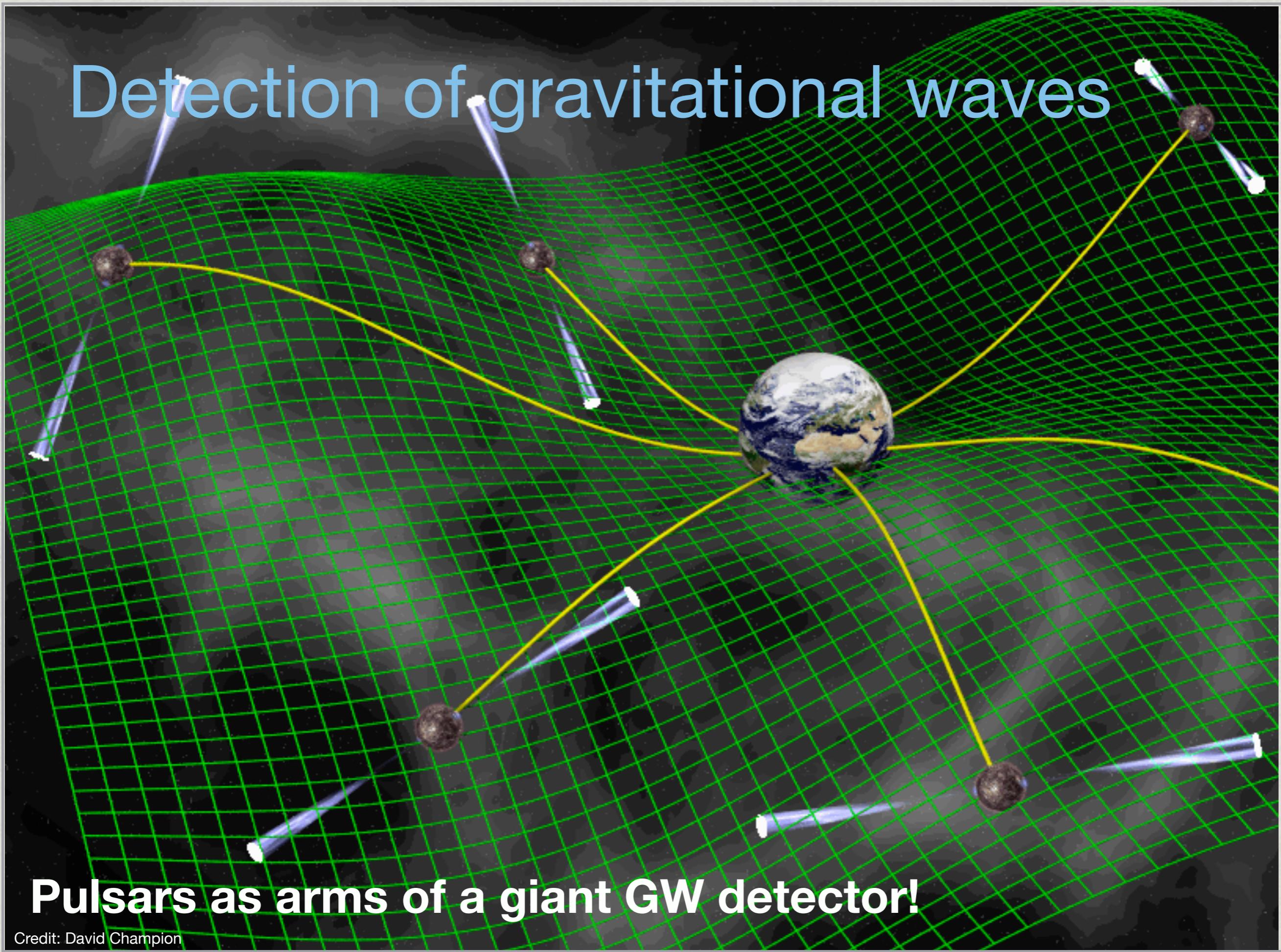
What we really want is a close black hole-millisecond pulsar binary

- \* highly relativistic, precise timer

## Intermediate-mass BH/pulsar?

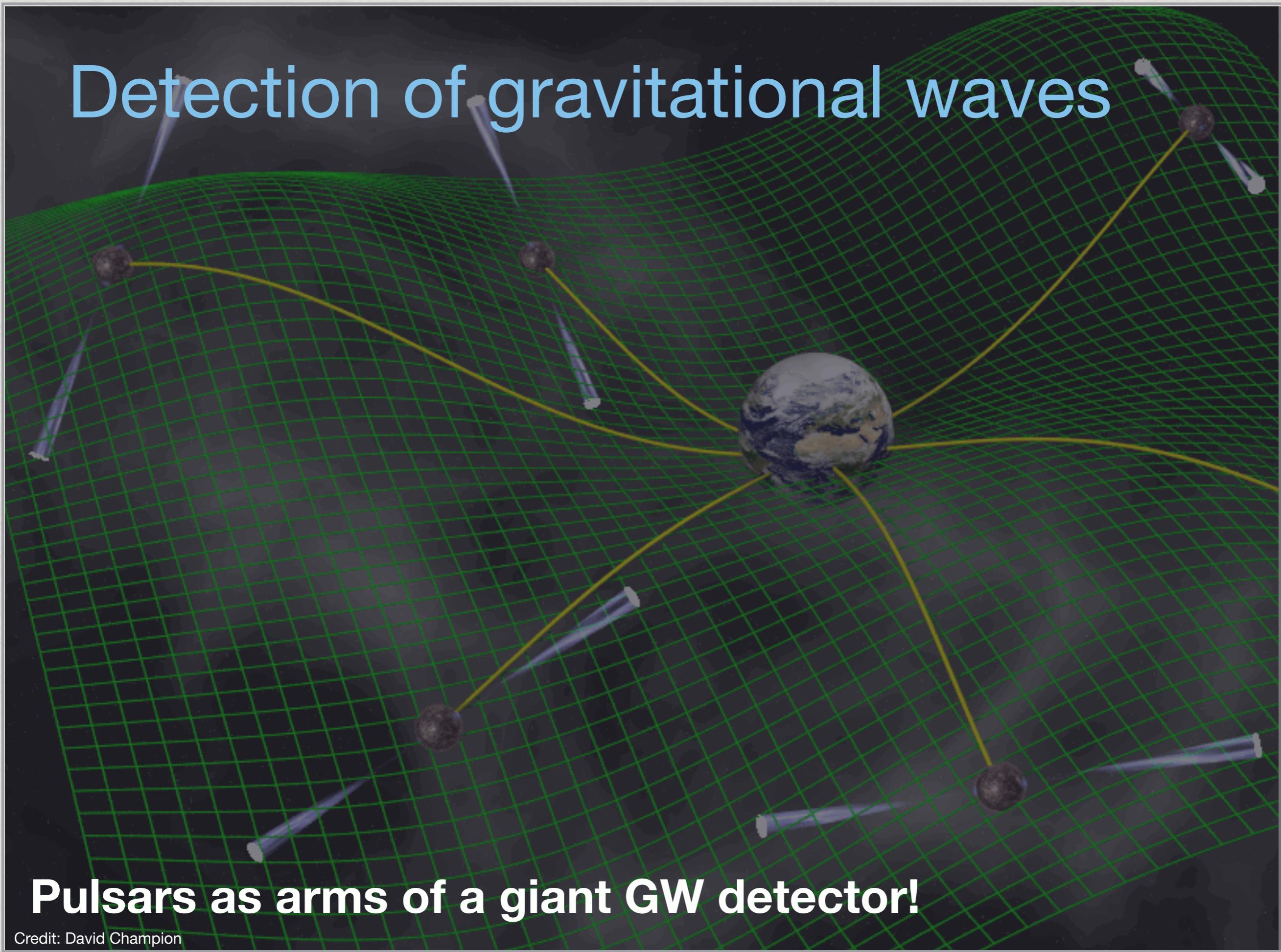
- \* some tests not currently possible with SMBHs

# Detection of gravitational waves



Credit: David Champion

# Detection of gravitational waves



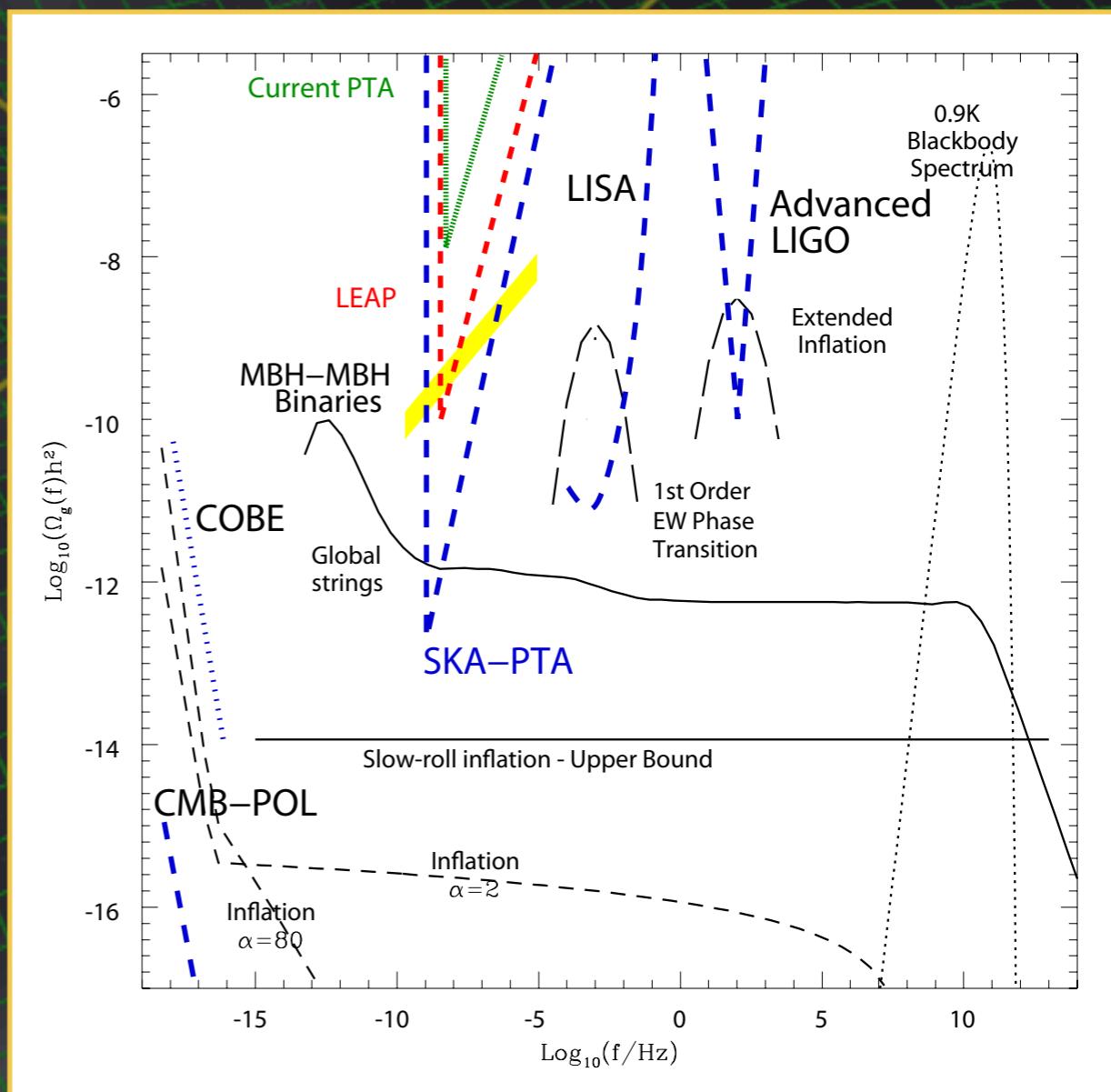
Pulsars as arms of a giant GW detector!

Credit: David Champion

# Detection of gravitational waves

Direct detection through common effect on arrival times

- \* period  $\sim$  observation time
  - \* nHz regime
- \* coalescence of SMBHs due to galaxy mergers
- \* stochastic GW background

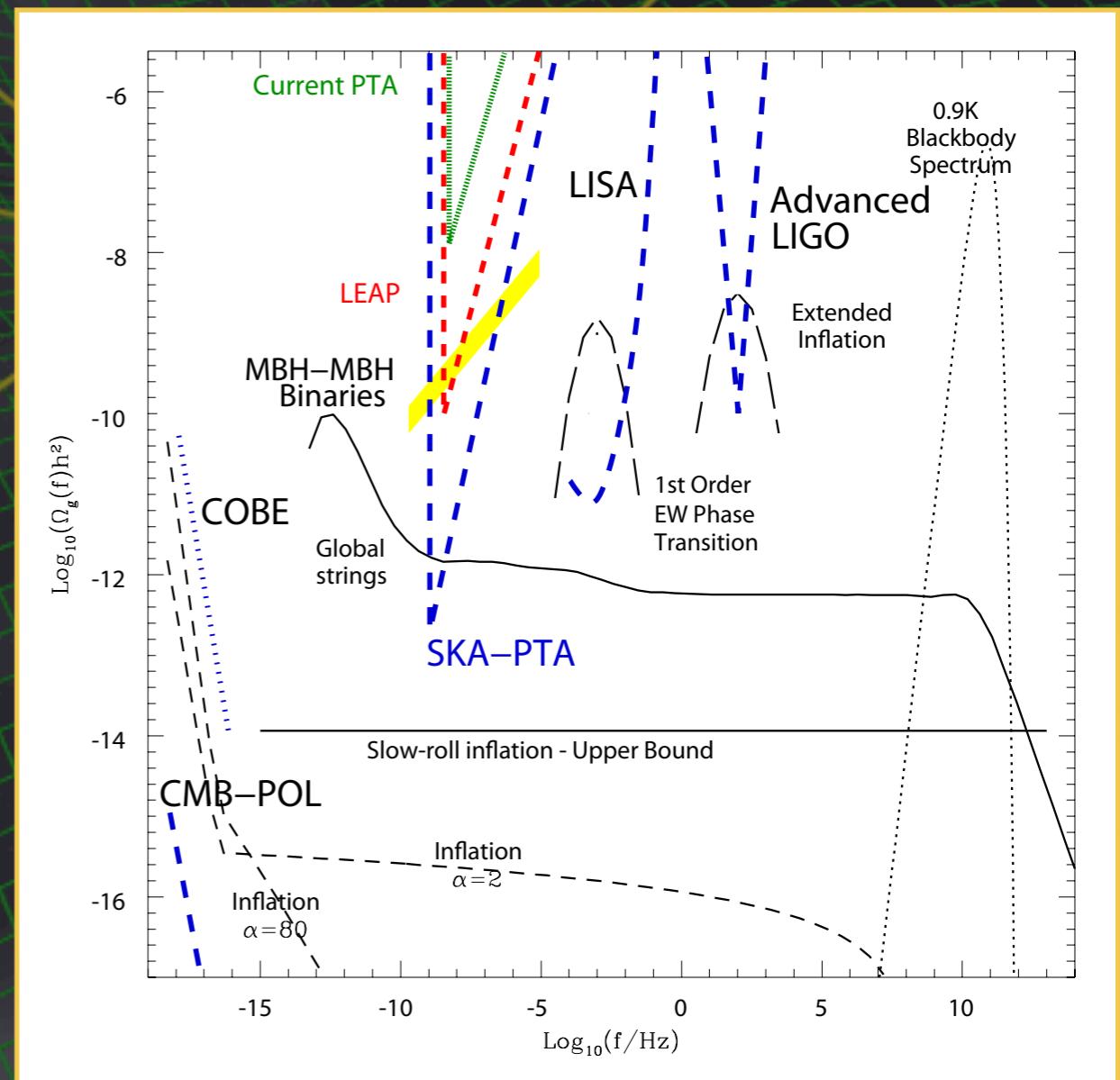


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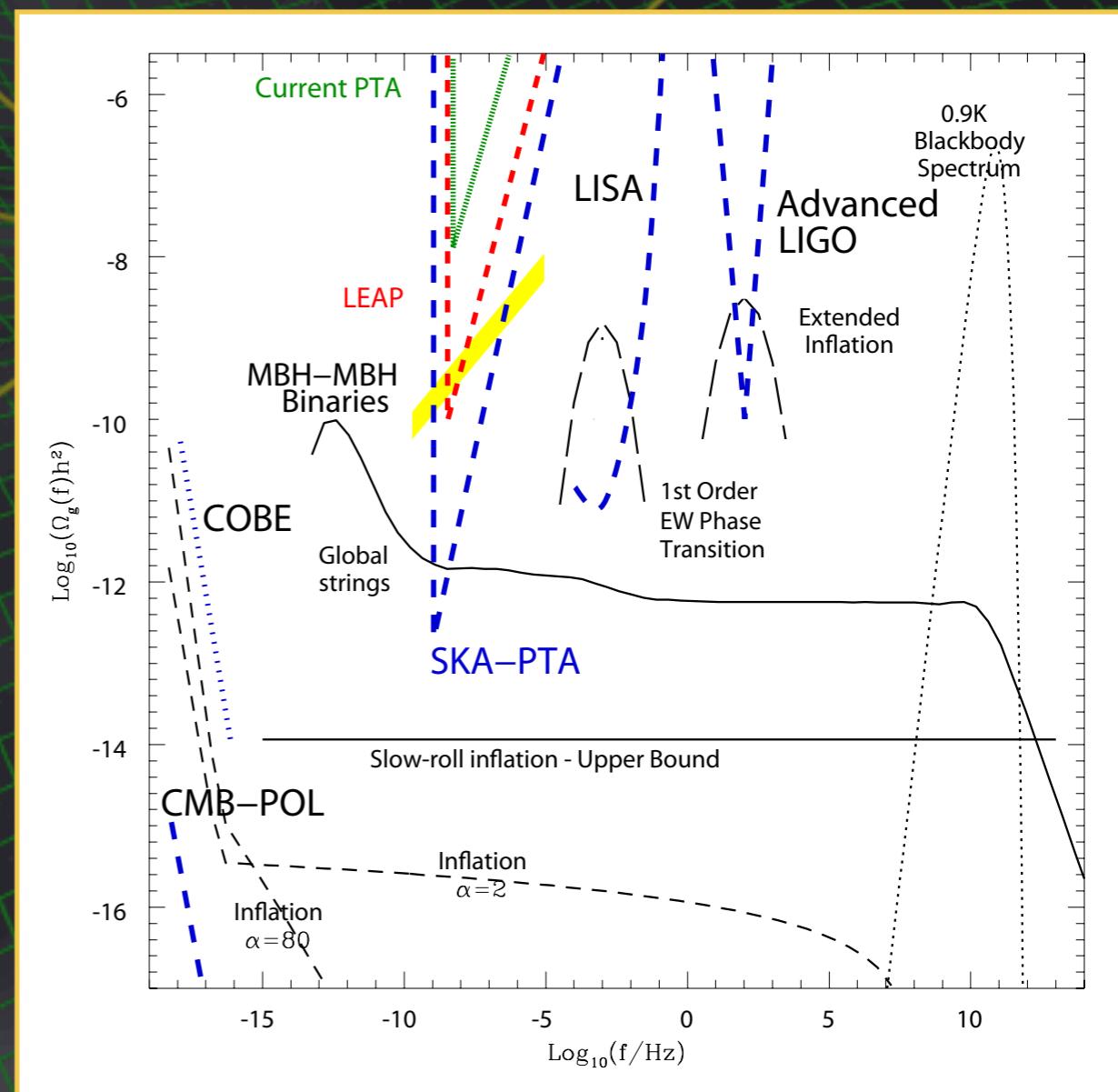


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- \* need  $\sim$  20 pulsars at  $\sim 100 \mu\text{s}$  precision timed for about 5-10 years

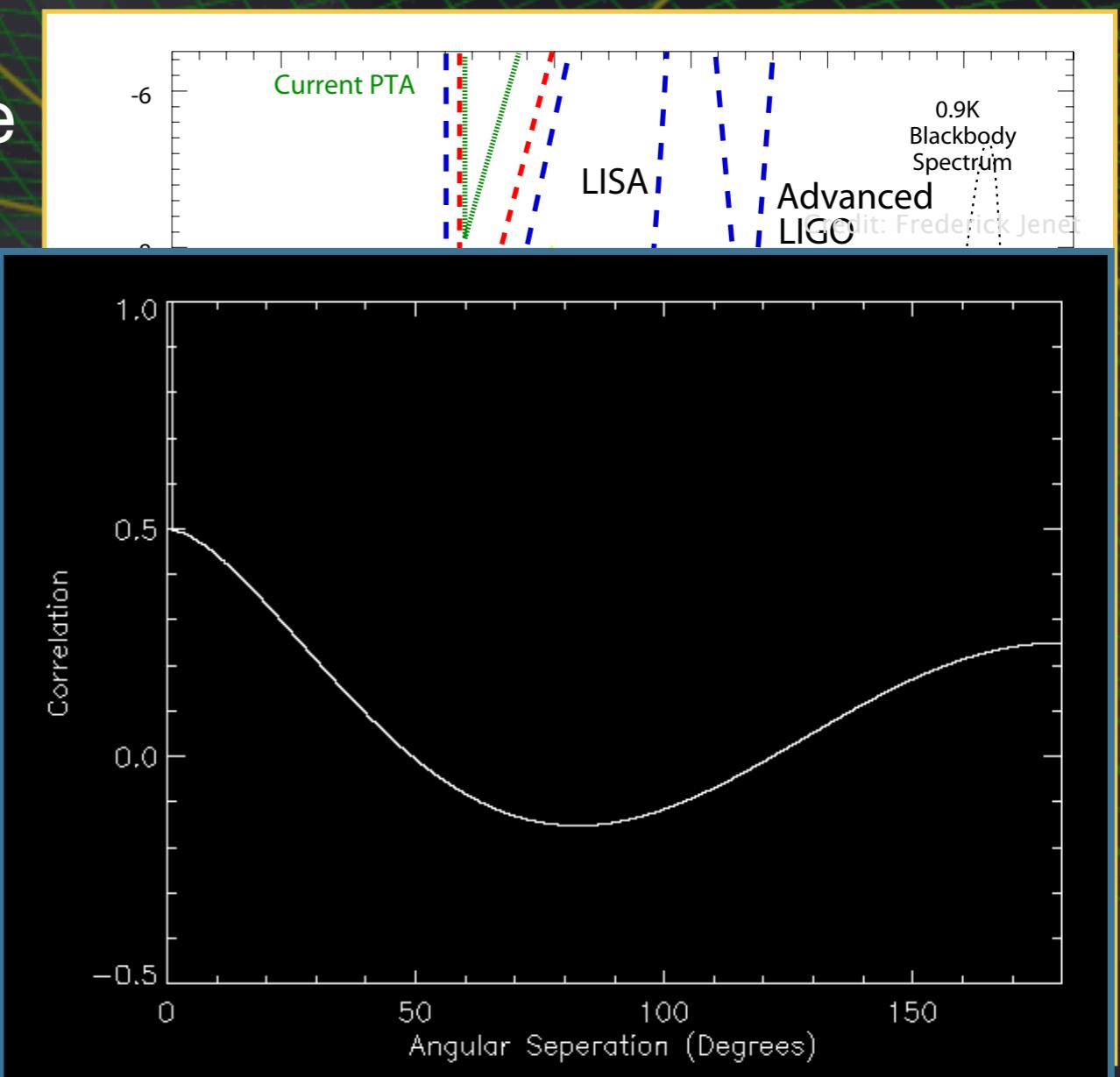


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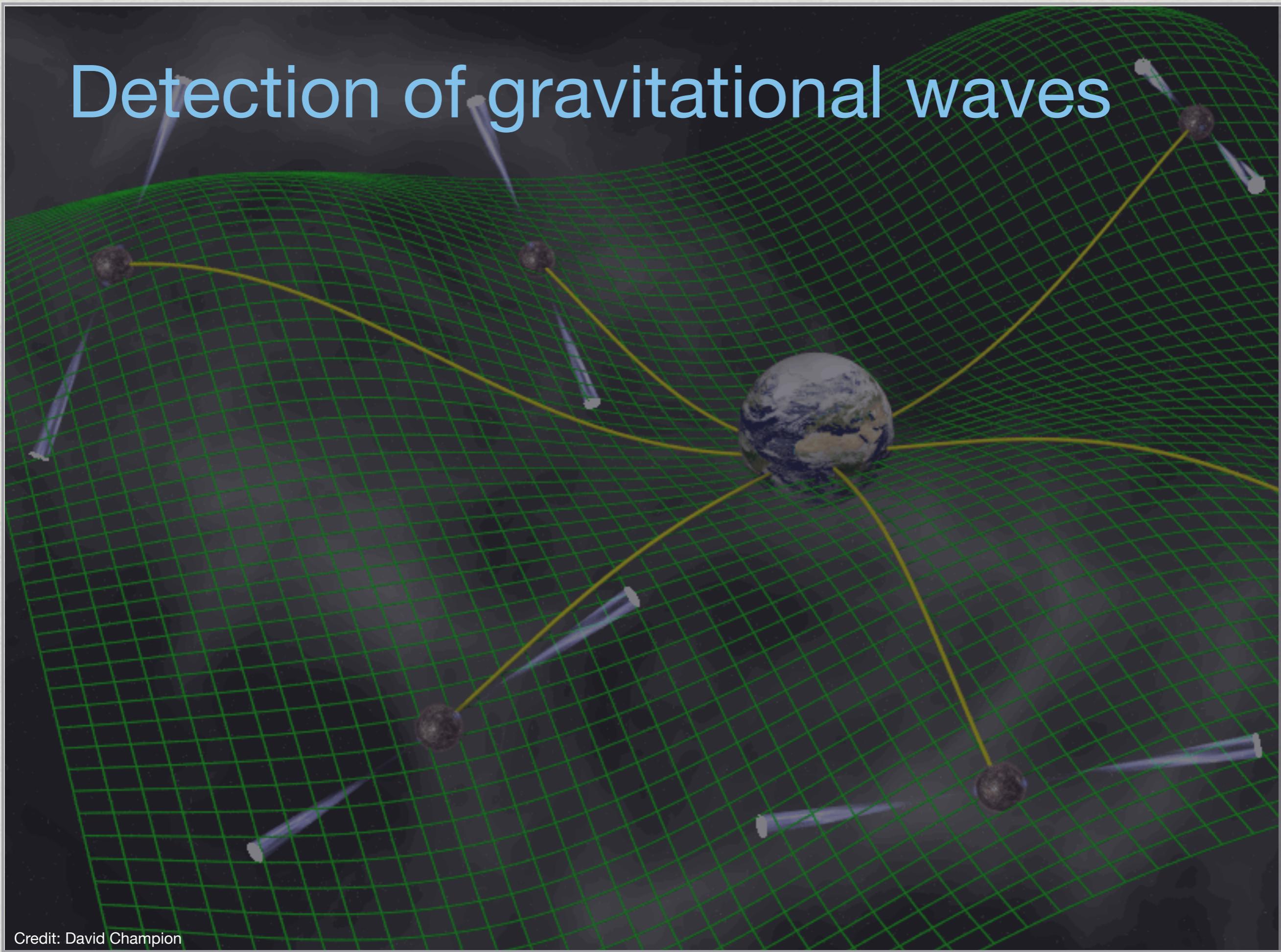
Direct detection through common effect on arrival times

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- \* well-distributed



Credit: David Champion

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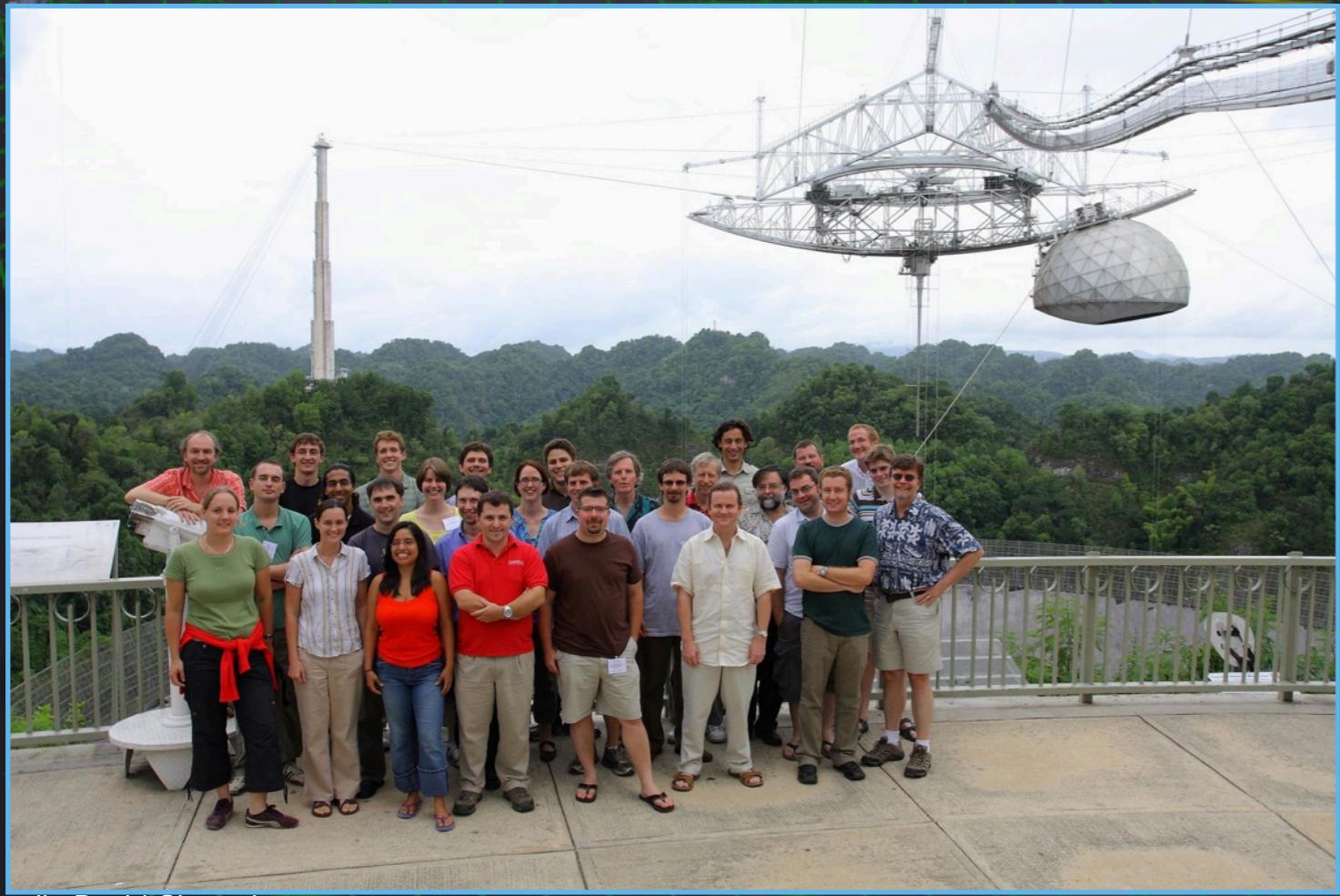


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# Detection of gravitational waves

International effort

- \* Europe, North America, Australia

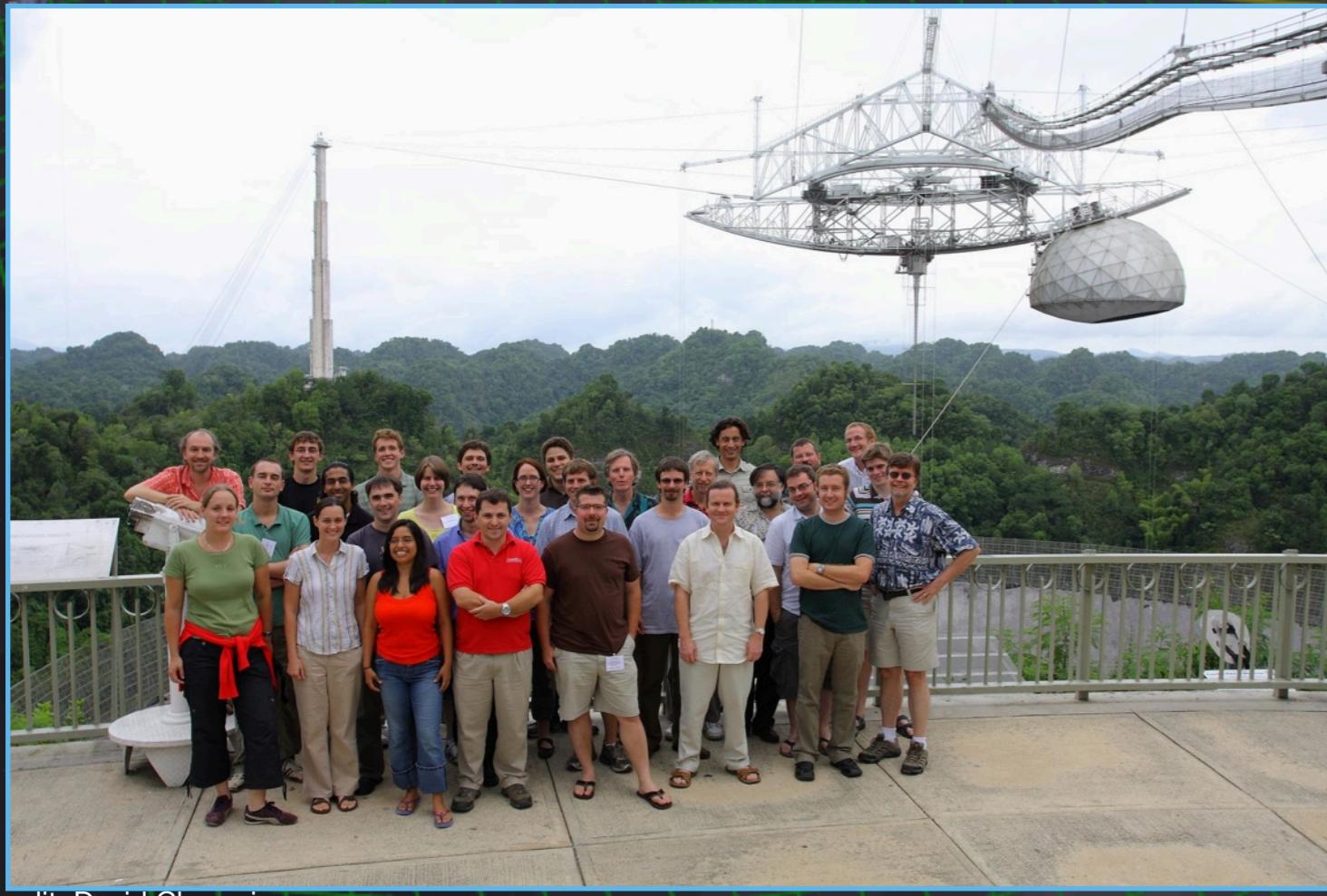


Credit: David Champion

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International effort

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- \* Europe: Large European Array for Pulsars (LEAP)

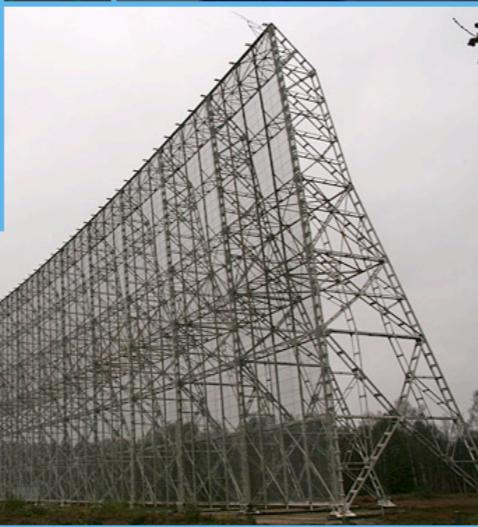


Credit: David Champion

# Detection of gravitational waves

## International effort

- \* Europe, North America, Australia
- \* **Europe:** Large European Array for Pulsars (LEAP)
- \* 5 major radio telescopes to form tied array



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## Future astrophysics

- \* individual source detection
- \* alternative gravity theories
- \* nature of galaxy mergers
- \* SKA?

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