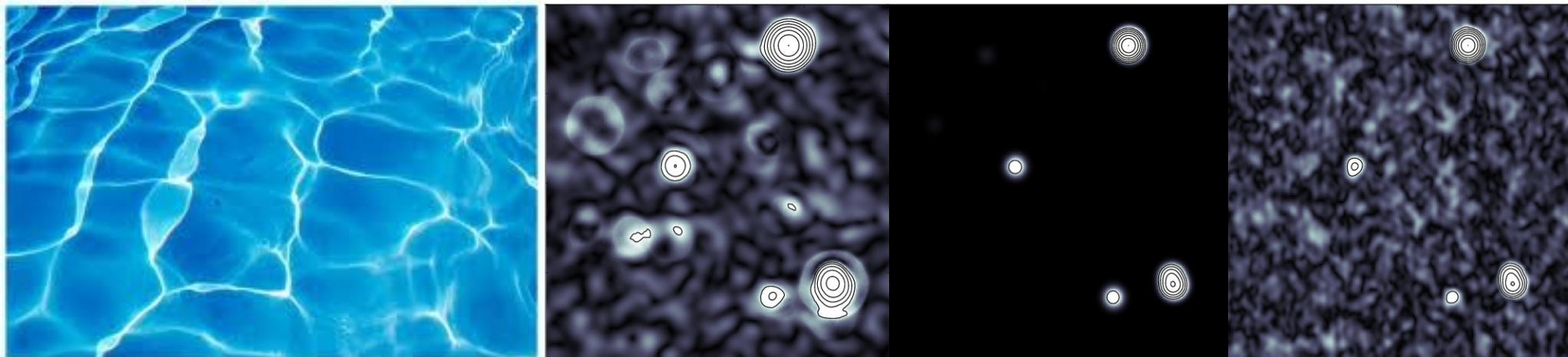


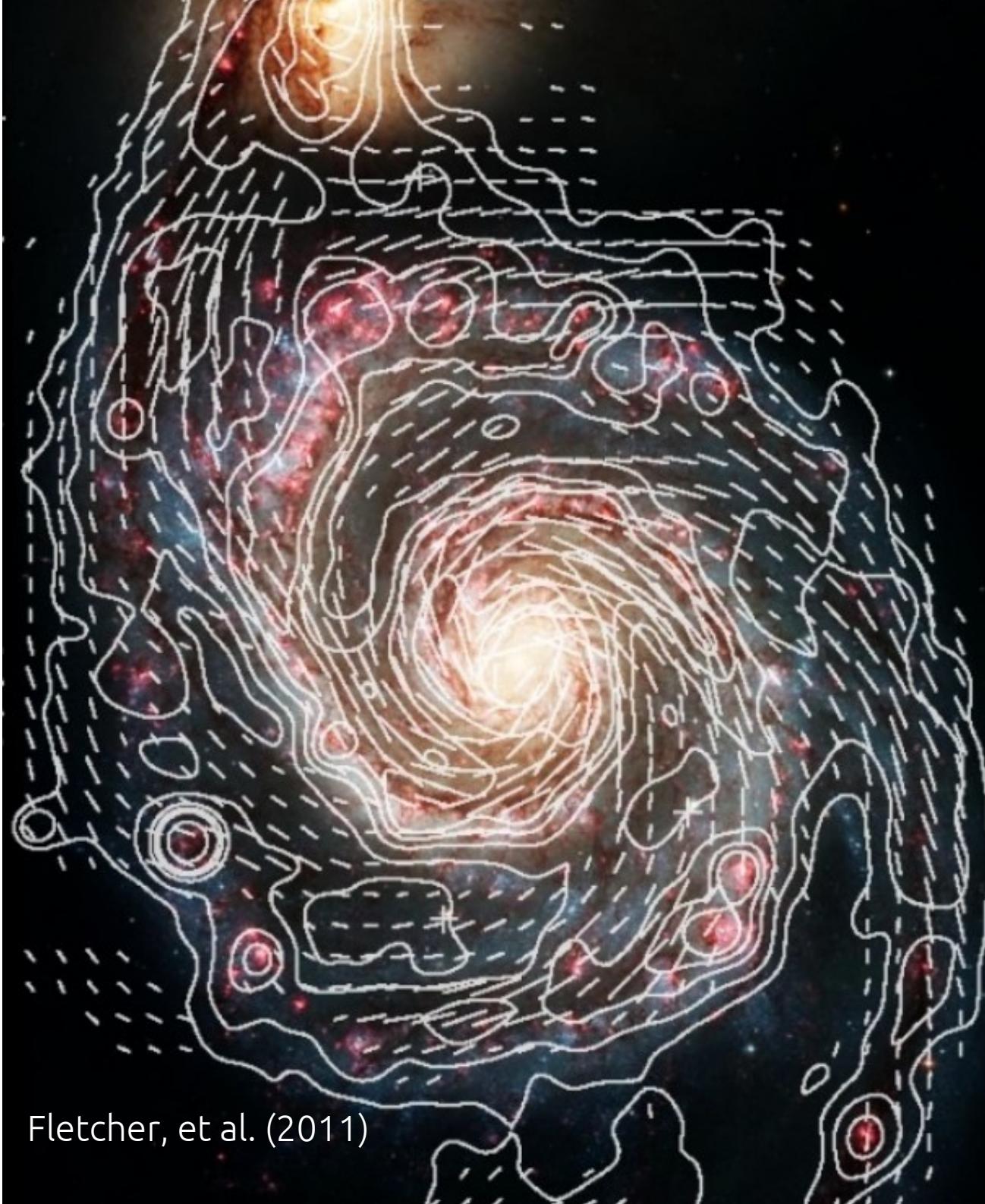
# A new view of magnetic fields: Faraday caustics and Faraday Synthesis



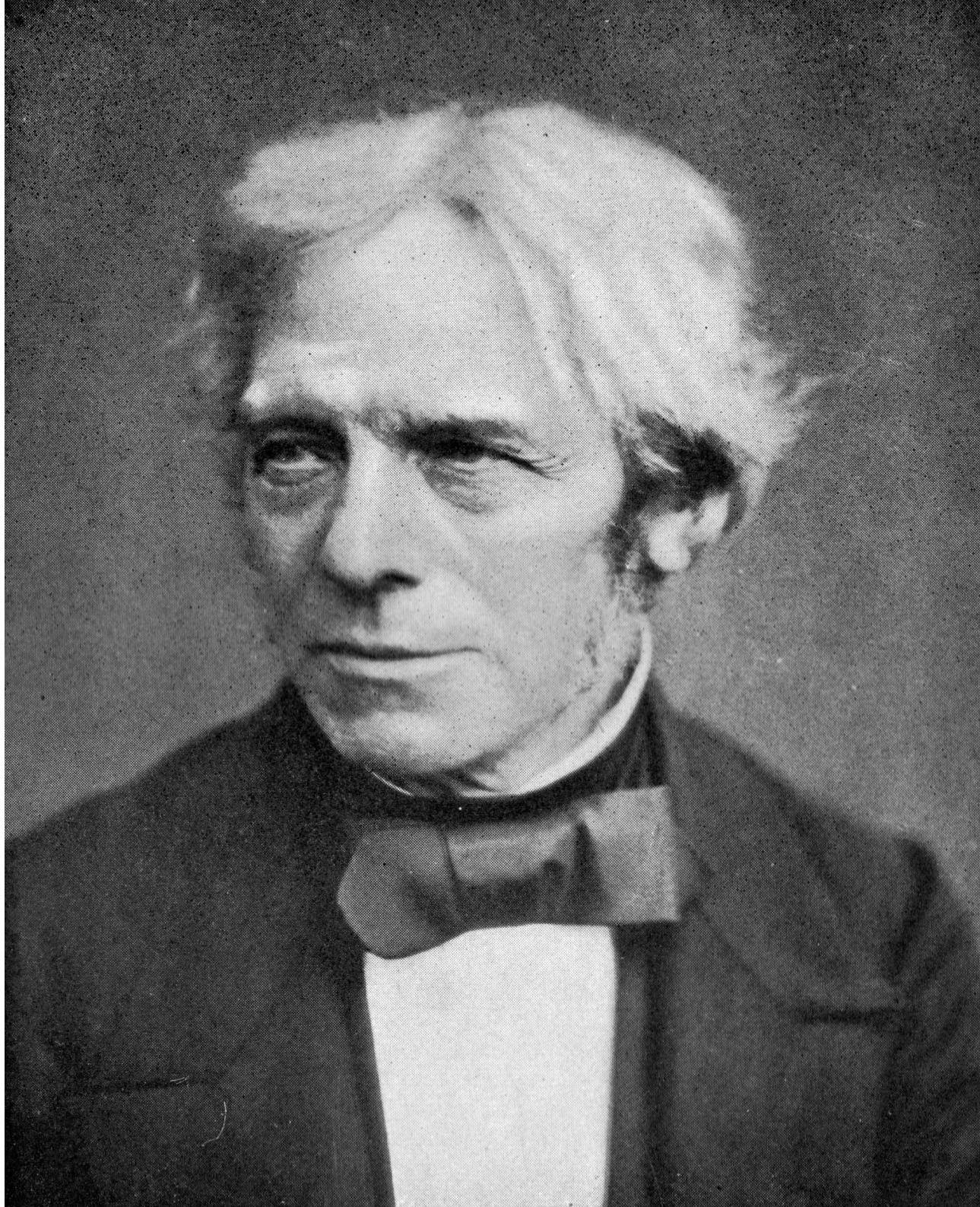
Max-Planck-Institut  
für Astrophysik



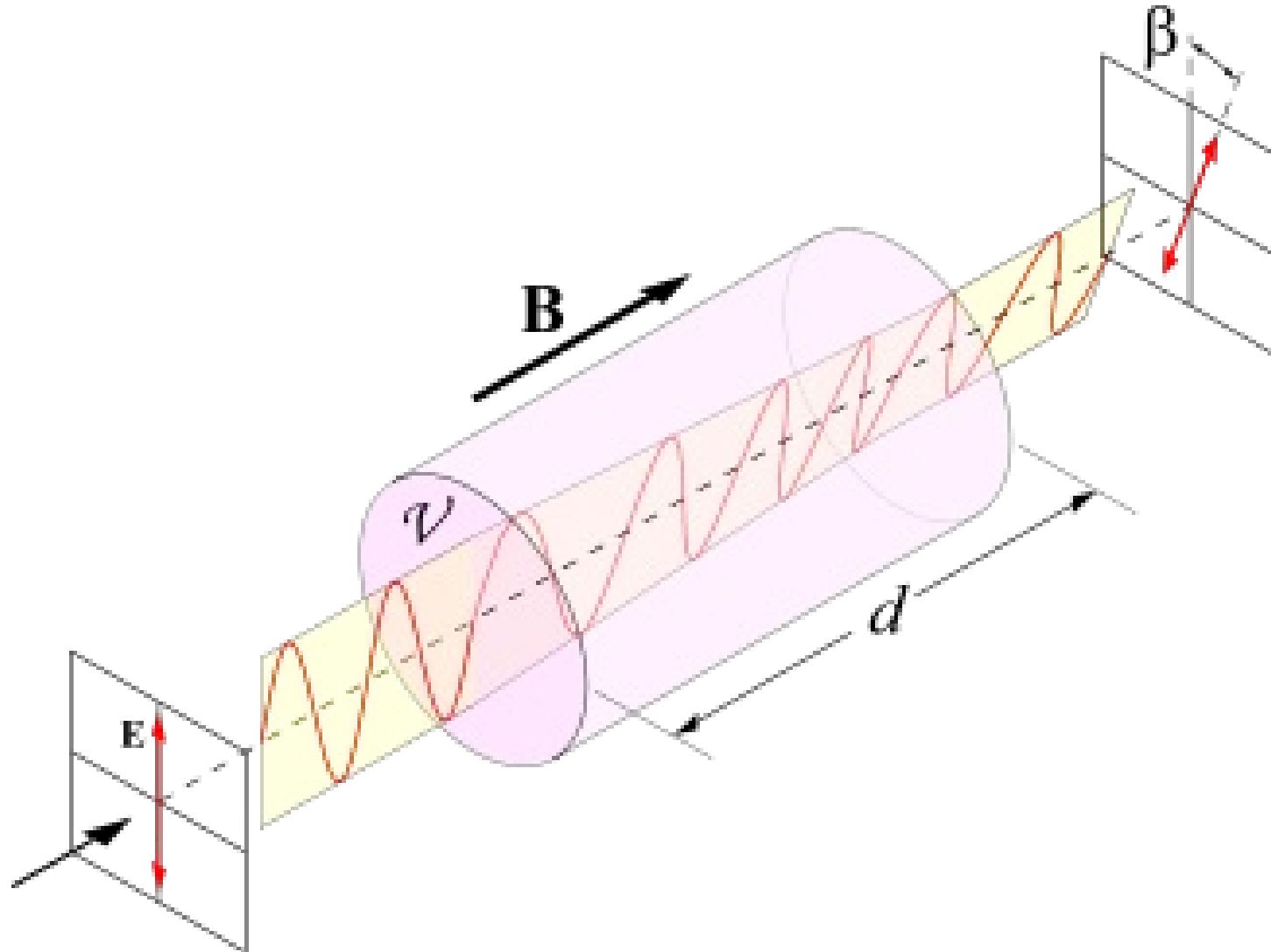
Michael Bell – MPA Garching  
with Torsten Enßlin  
and Henrik Junklewitz



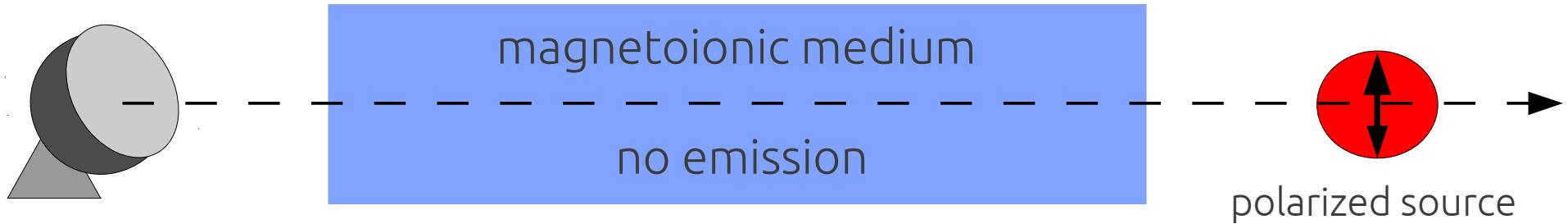
Fletcher, et al. (2011)



# Faraday Rotation



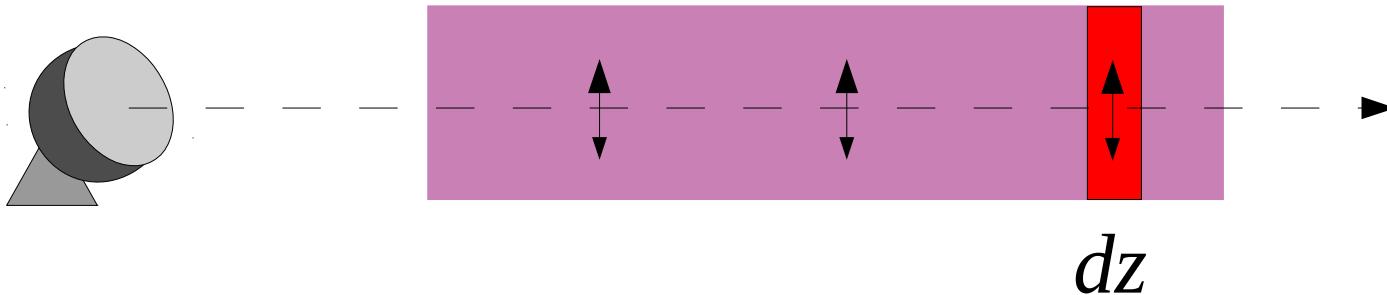
# Faraday Rotation



$$\chi = \chi_0 + \varphi \lambda^2 \quad \text{polarization angle}$$

$$\varphi \propto \int_{here}^{there} dz n_e B_z \quad \text{Faraday depth}$$

# Mixed rotating and emitting media



recall

$$P(z)dz = p(z)e^{2i\chi_0}dz$$

$$\chi = \chi_0 + \varphi \lambda^2$$

$$\varphi \propto \int_{here}^{there} n_e B_z dz$$

$$P(z)dz = F(\varphi)d\varphi$$

$$P(\lambda^2) = \int_{-\infty}^{\infty} d\varphi F(\varphi) e^{2i\varphi\lambda^2}$$

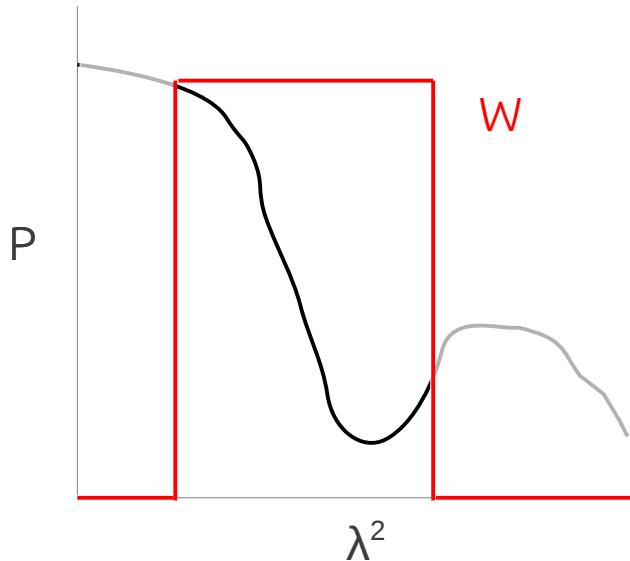
**Faraday spectrum**

i.e. Pol. Intensity  
per unit Faraday  
depth

Burn (1966)

# RM Synthesis

see Brentjens & de Bruyn (2005)

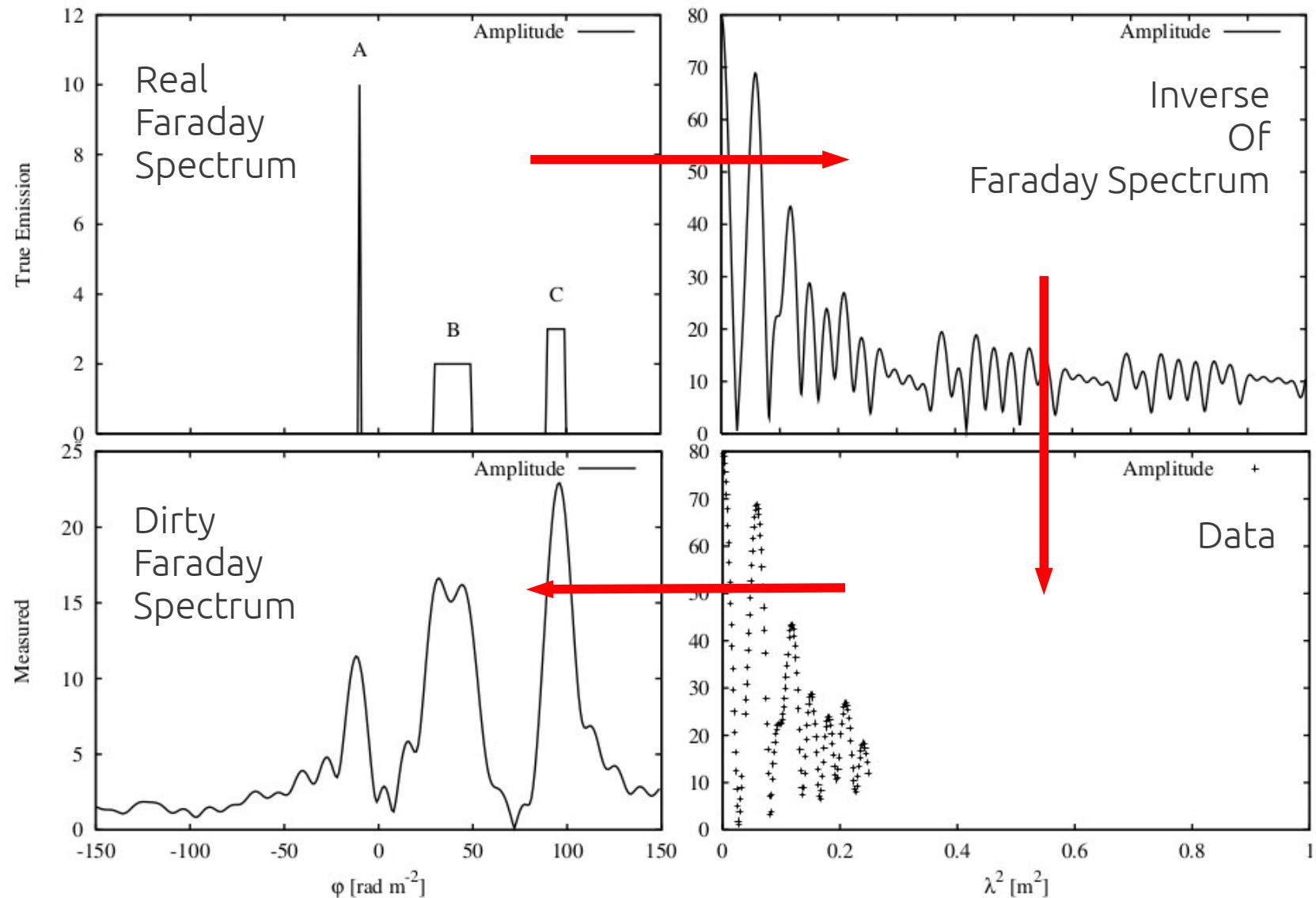


$$F'(\varphi) = FT[W P(\lambda^2)] = F(\varphi) * R(\varphi)$$

$$R(\varphi) = FT[W(\lambda^2)] \quad \text{"Point spread function"}$$

# RM Synthesis

see Brentjens & de Bruyn (2005)

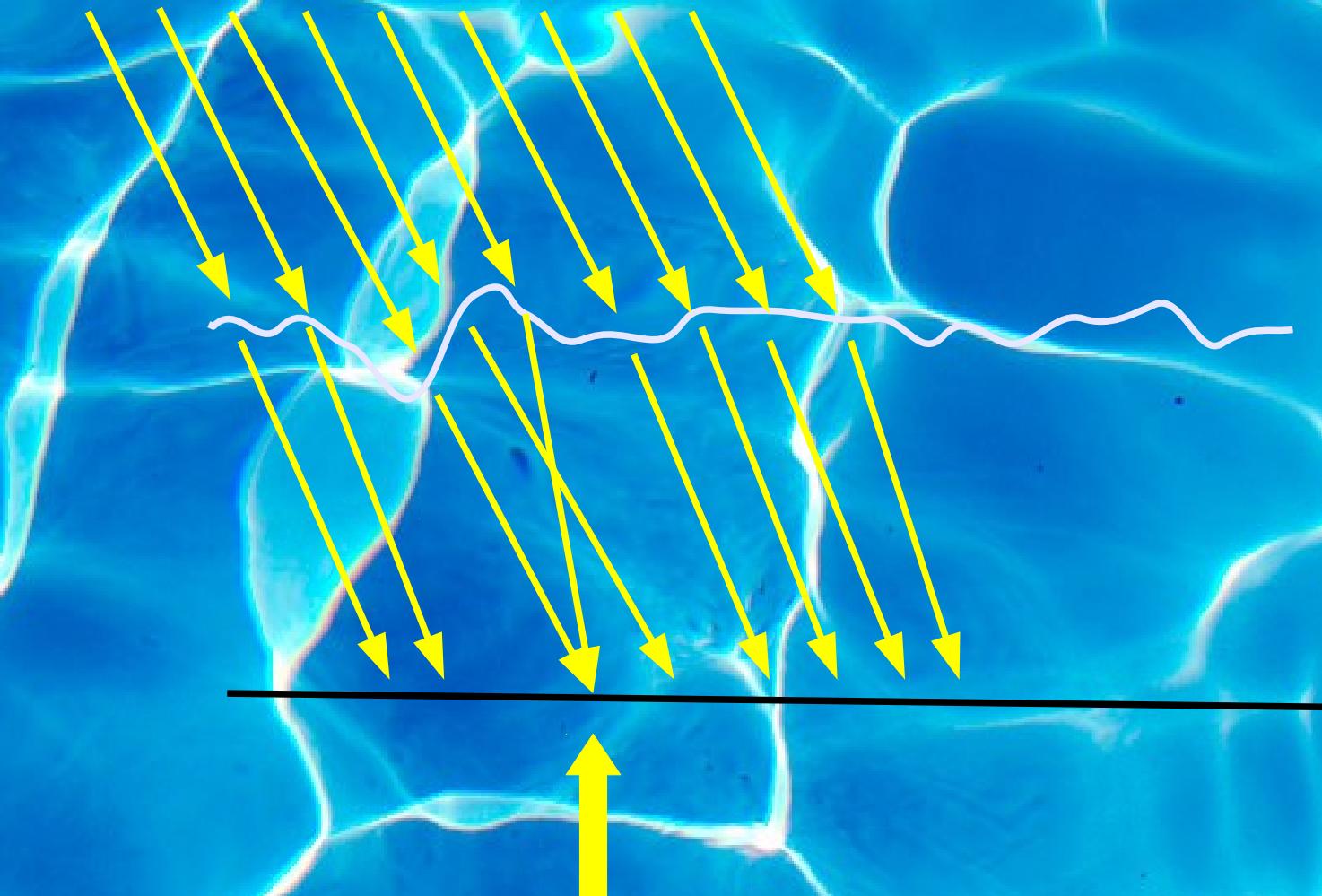


# Faraday Caustics

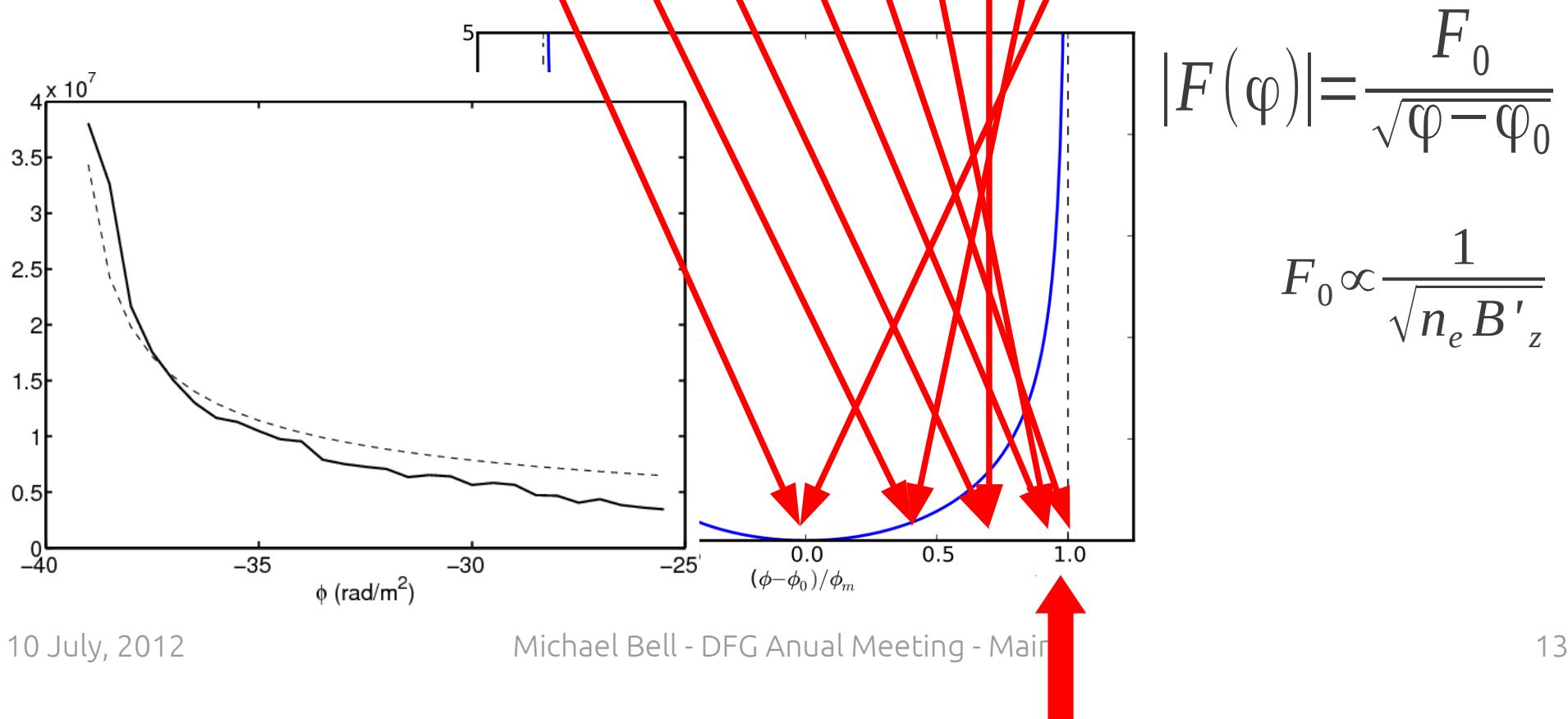
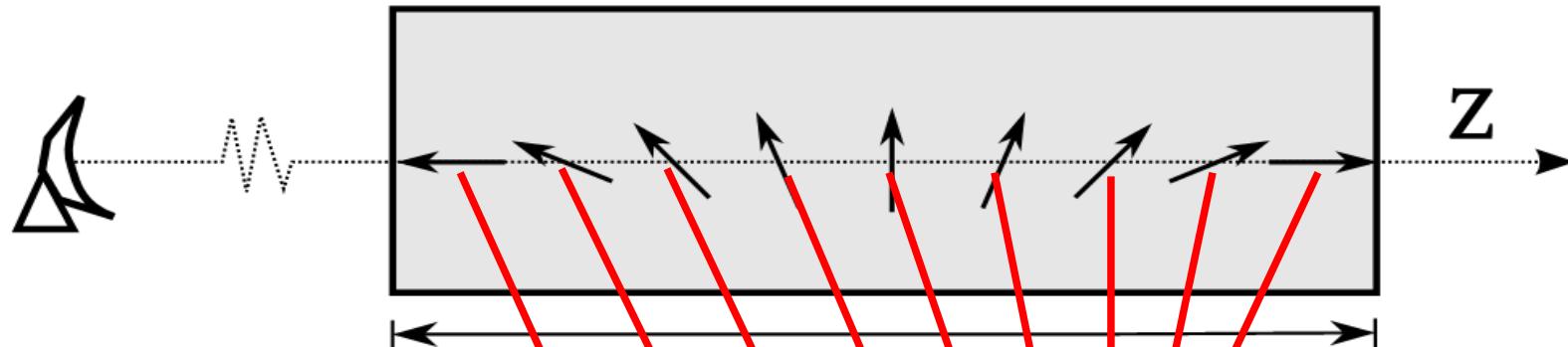
Singularities in the Faraday spectrum and their utility as probes of magnetic field properties



# Optical caustics

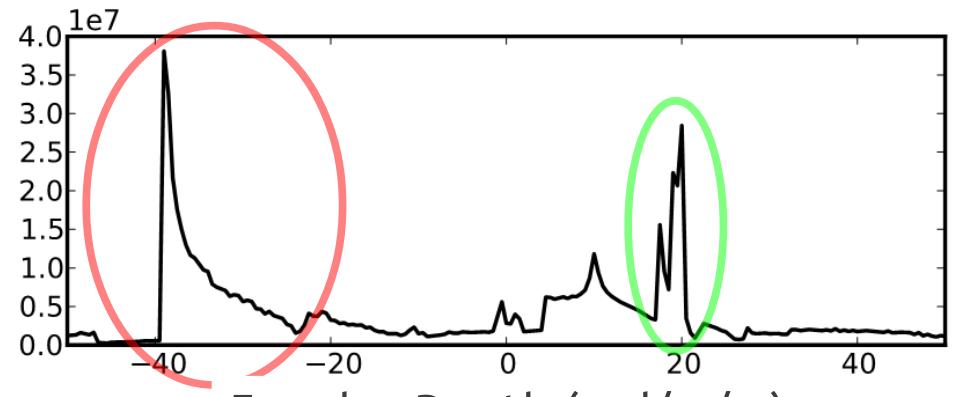


# Faraday Caustics



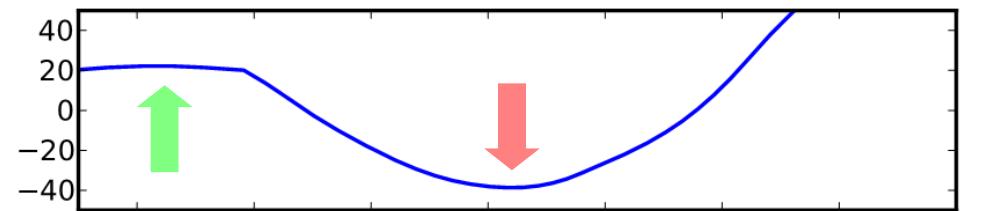
# Faraday Caustics

Faraday spectrum

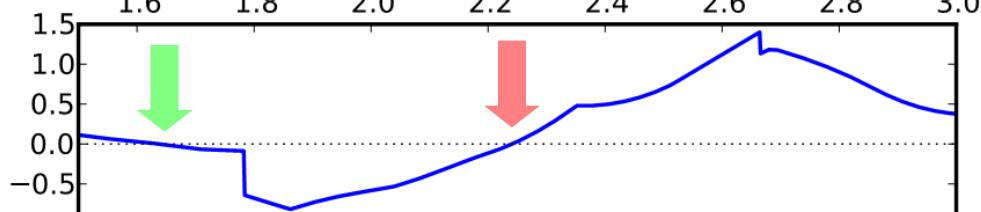


Faraday Depth (rad/m/m)

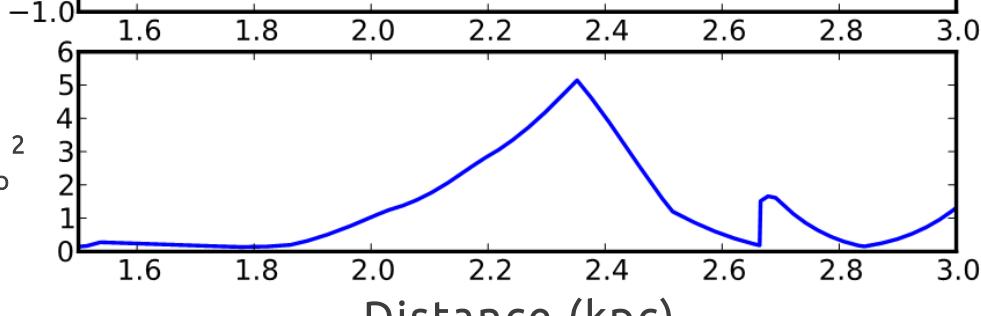
$n_e B_{\text{par}}$



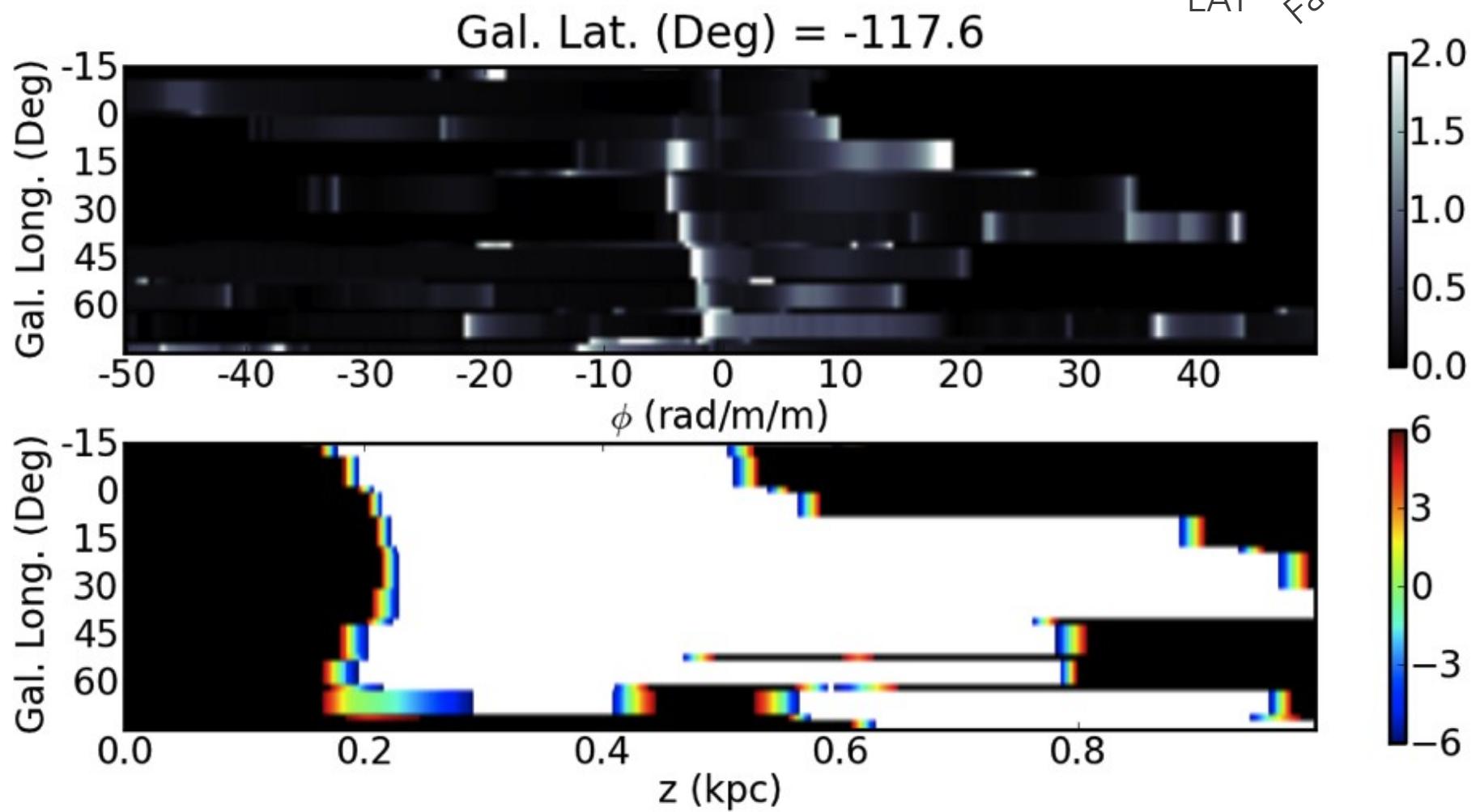
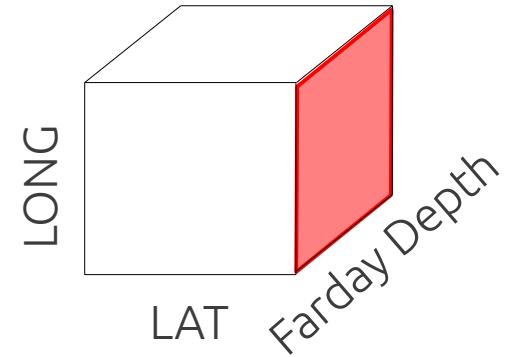
$n_e B_{\text{par}}$



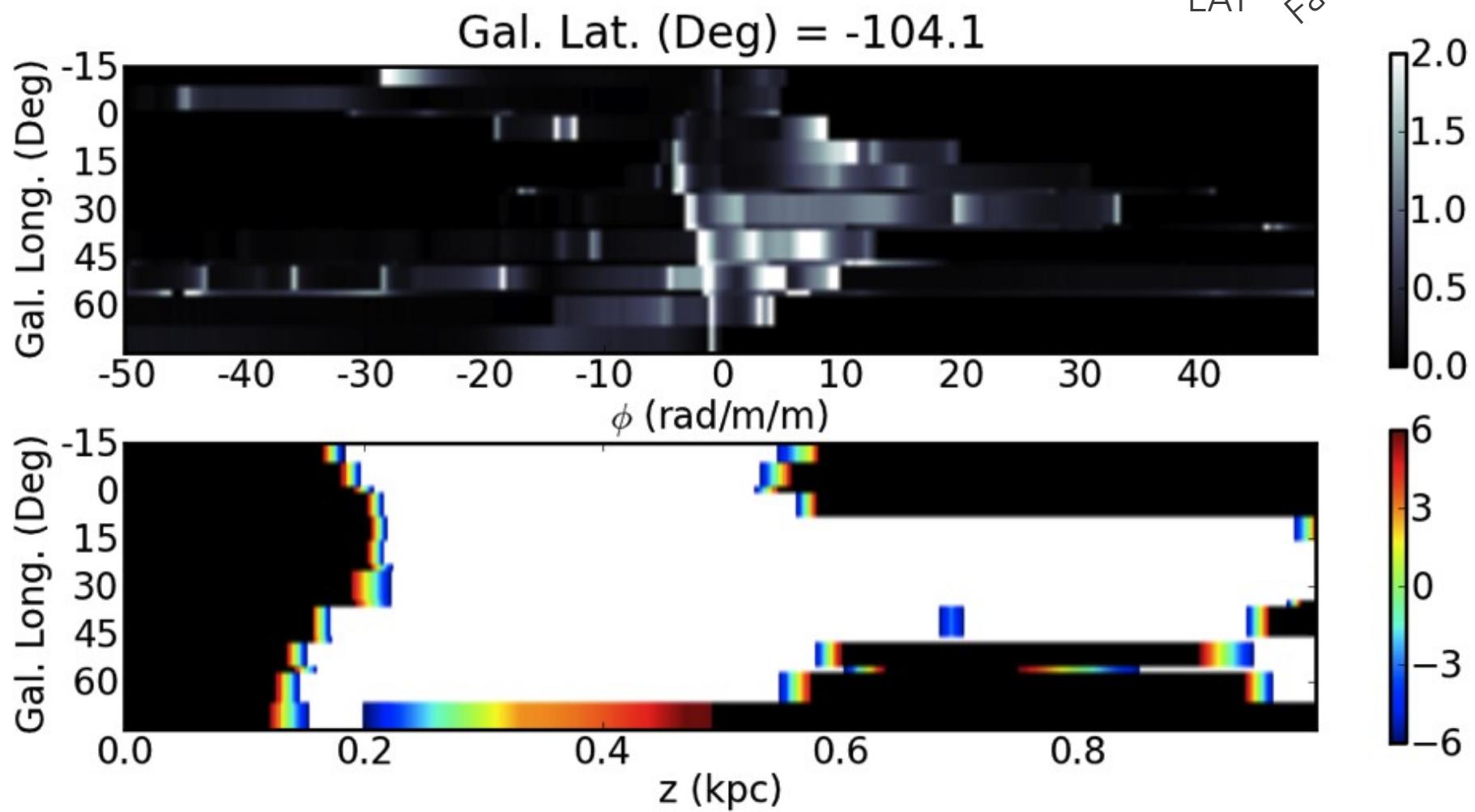
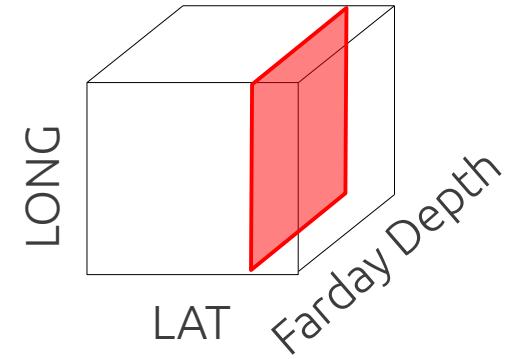
Synchrotron intensity  $\sim B_{\text{perp}}^2$



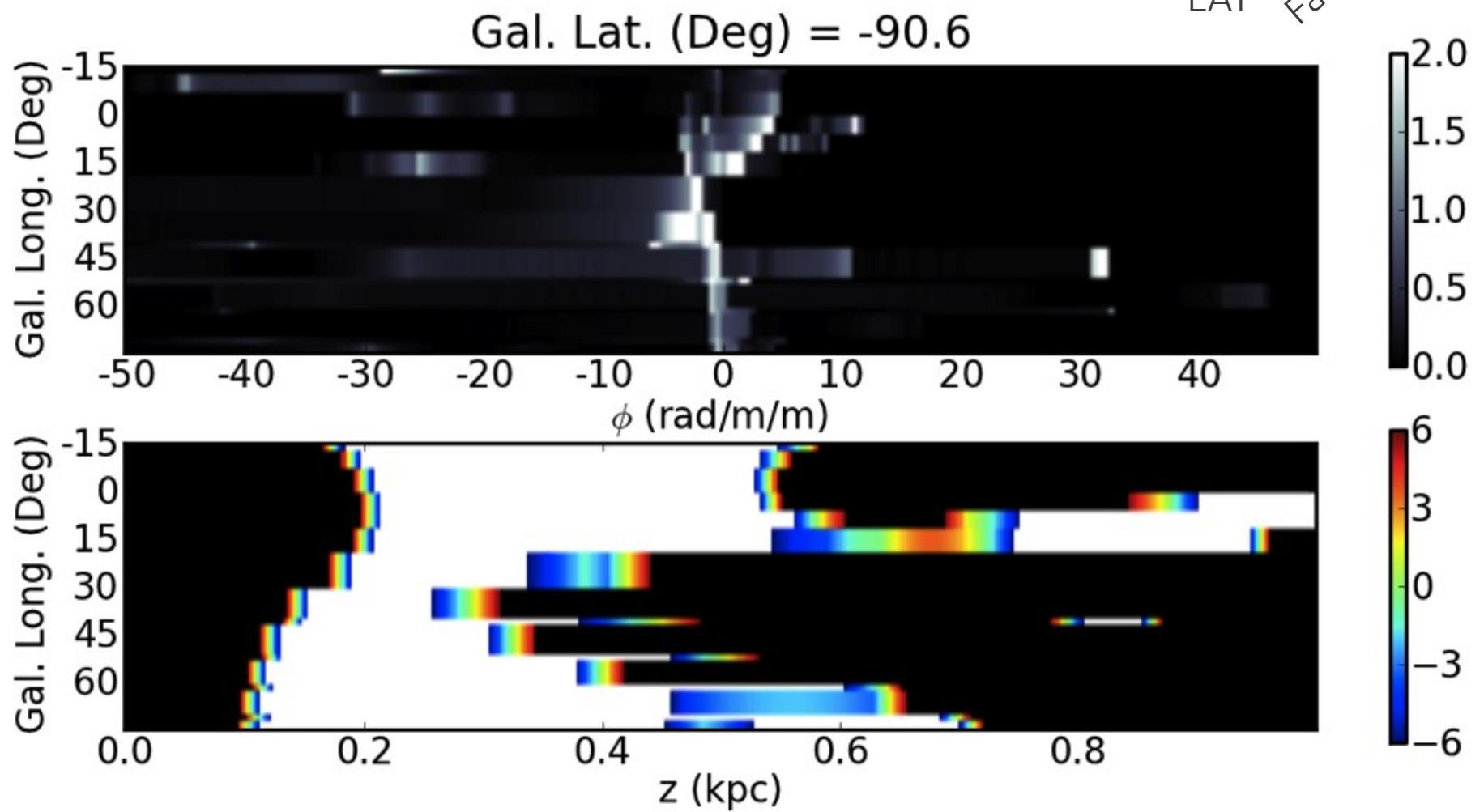
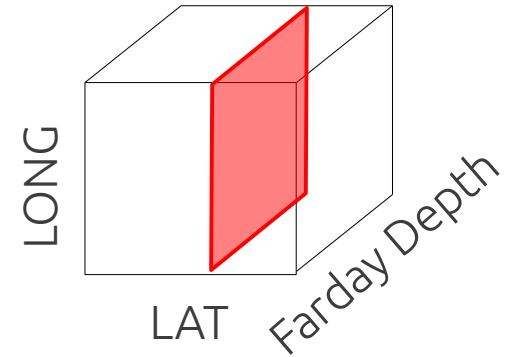
# 3D Structure



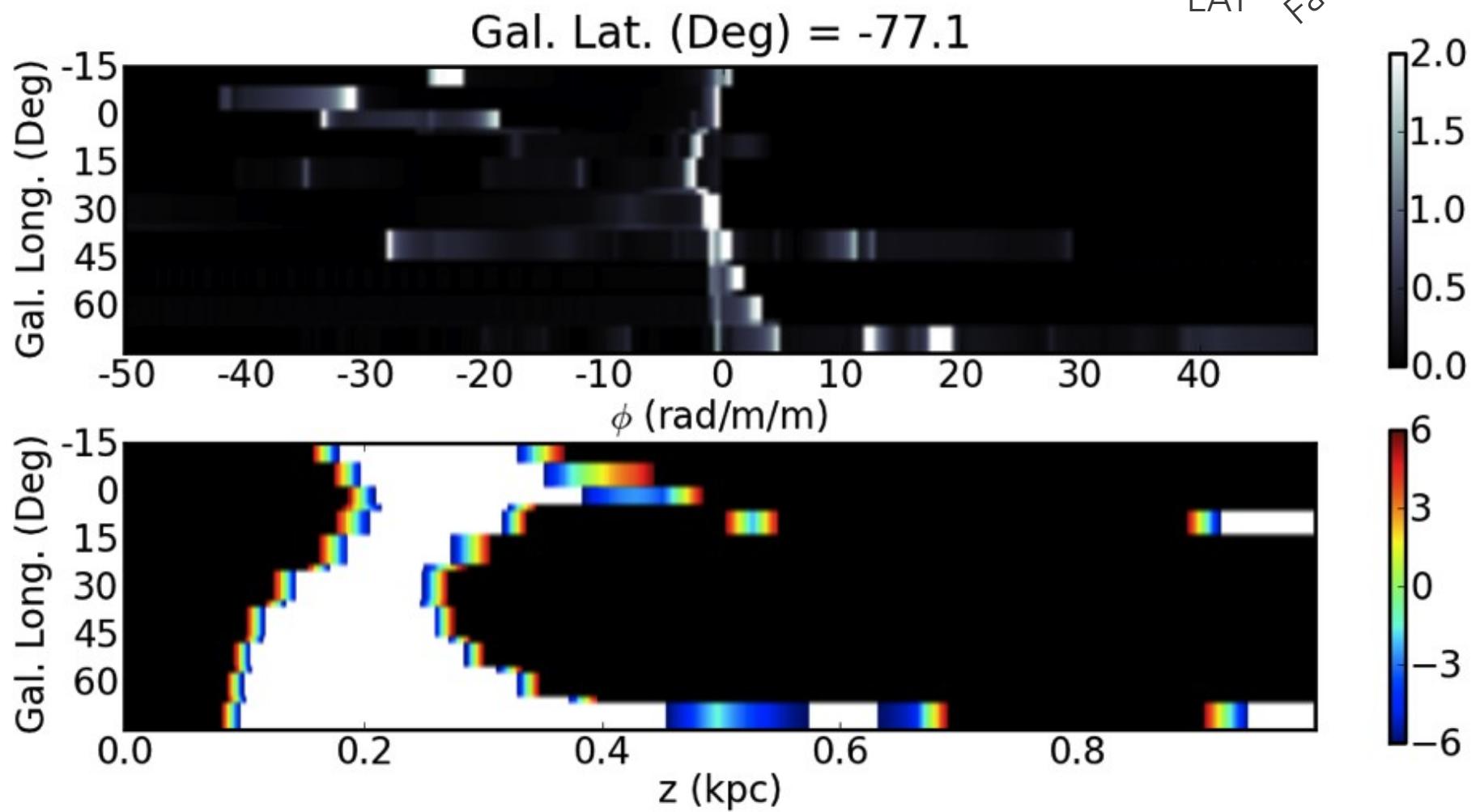
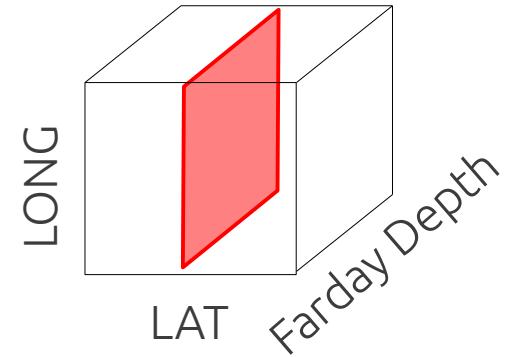
# 3D Structure



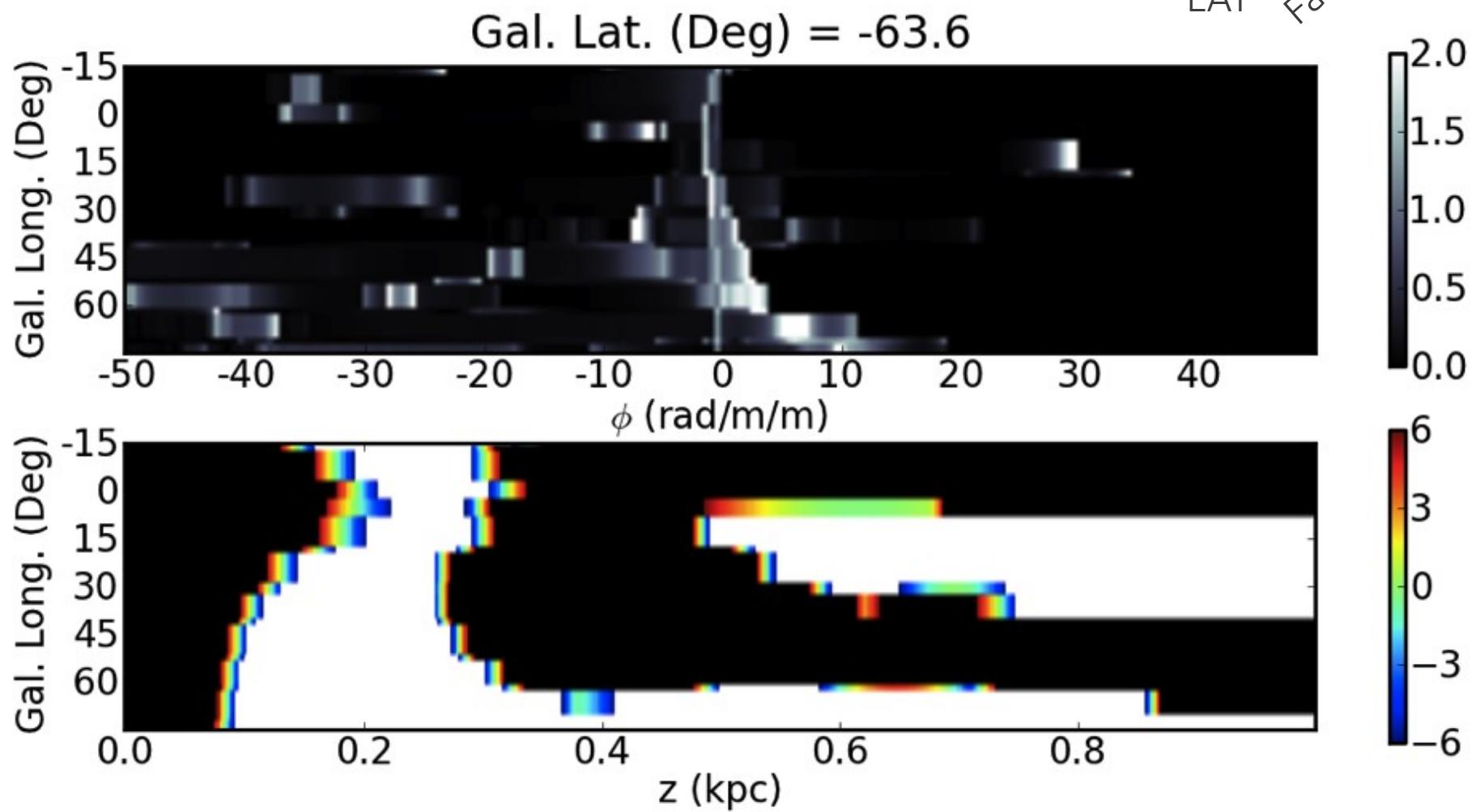
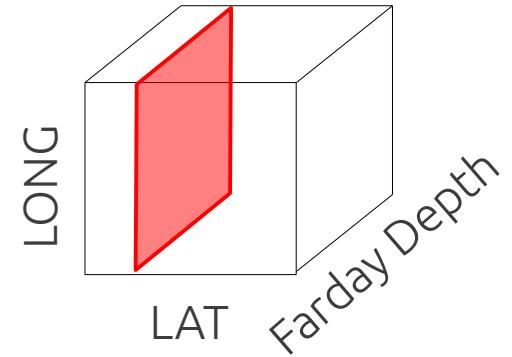
# 3D Structure



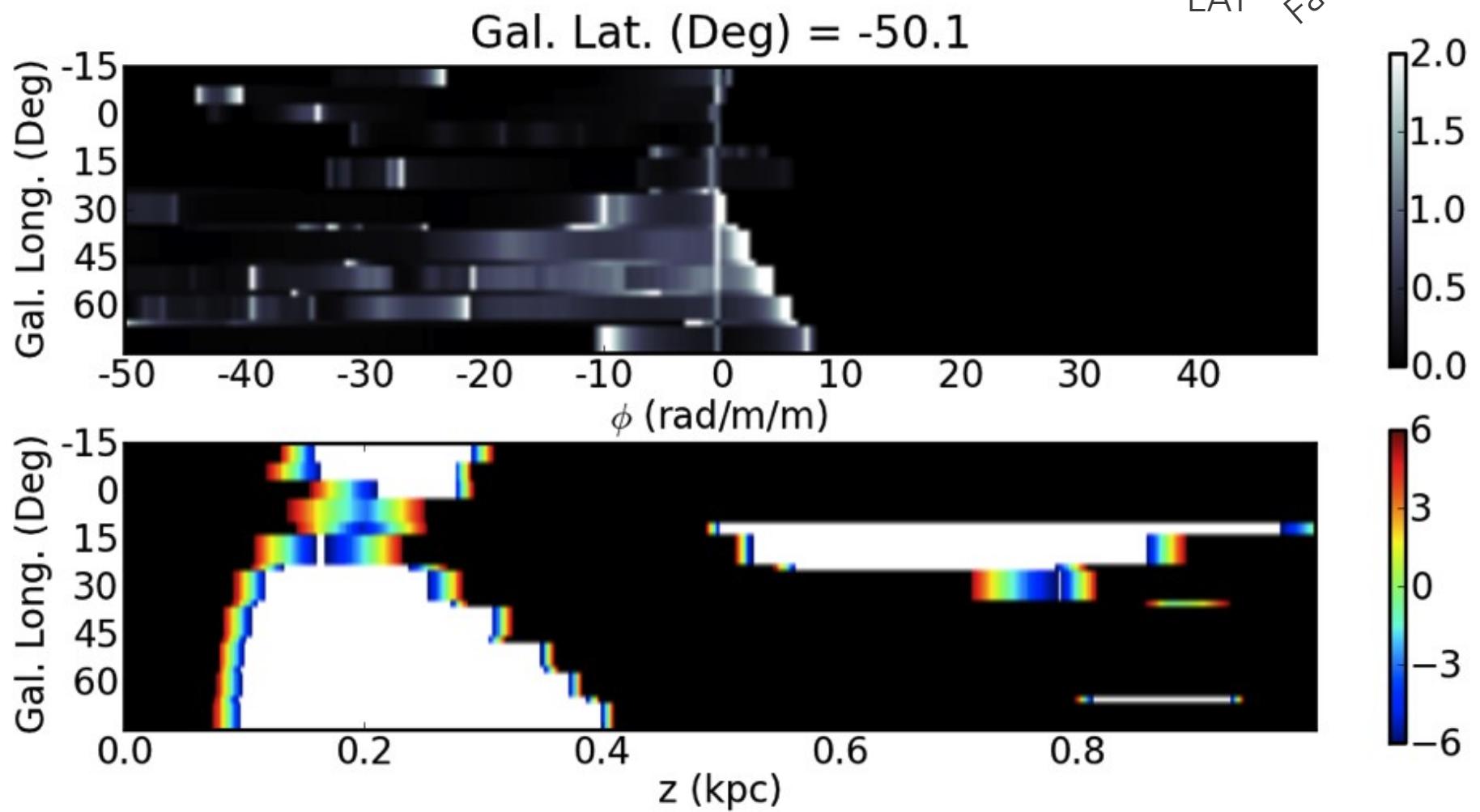
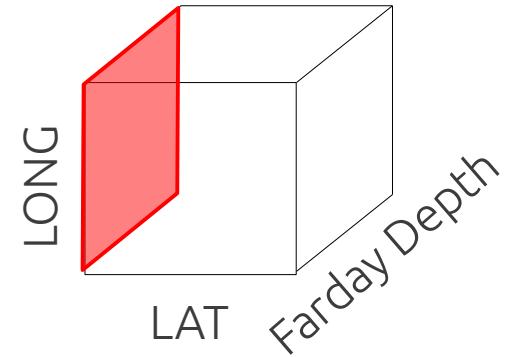
# 3D Structure



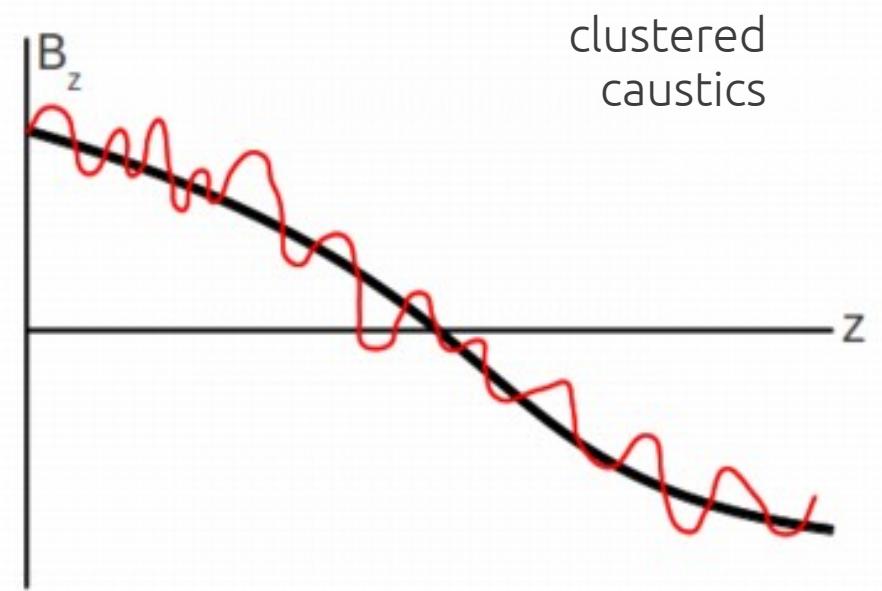
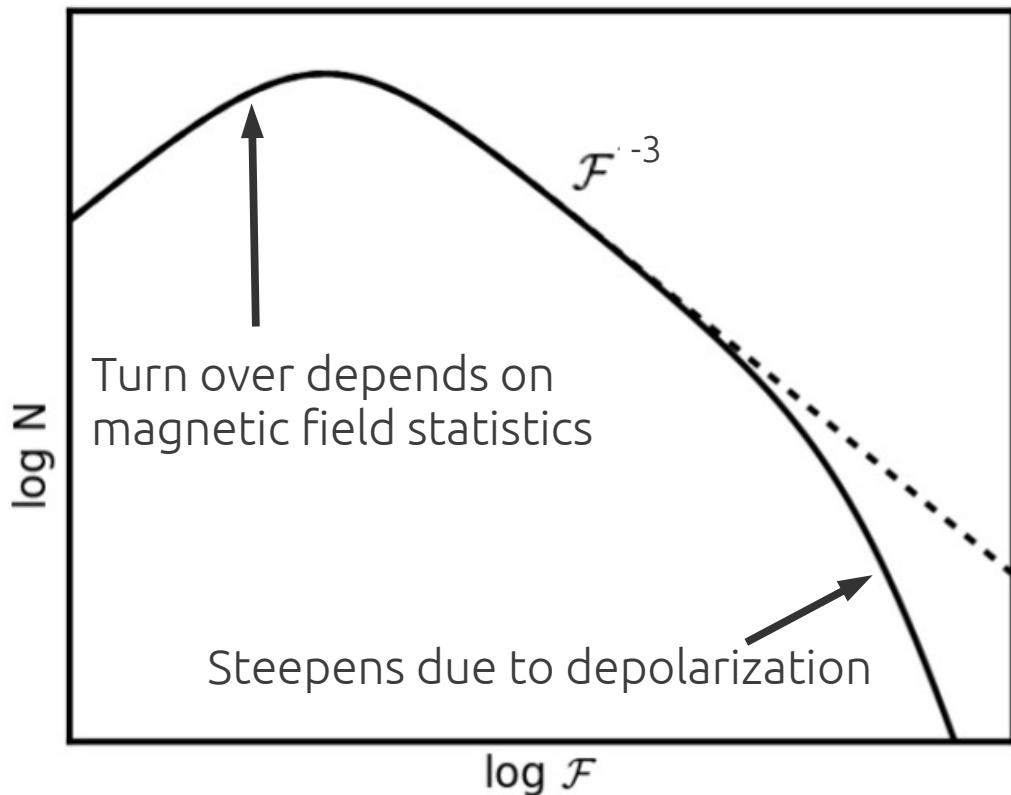
# 3D Structure



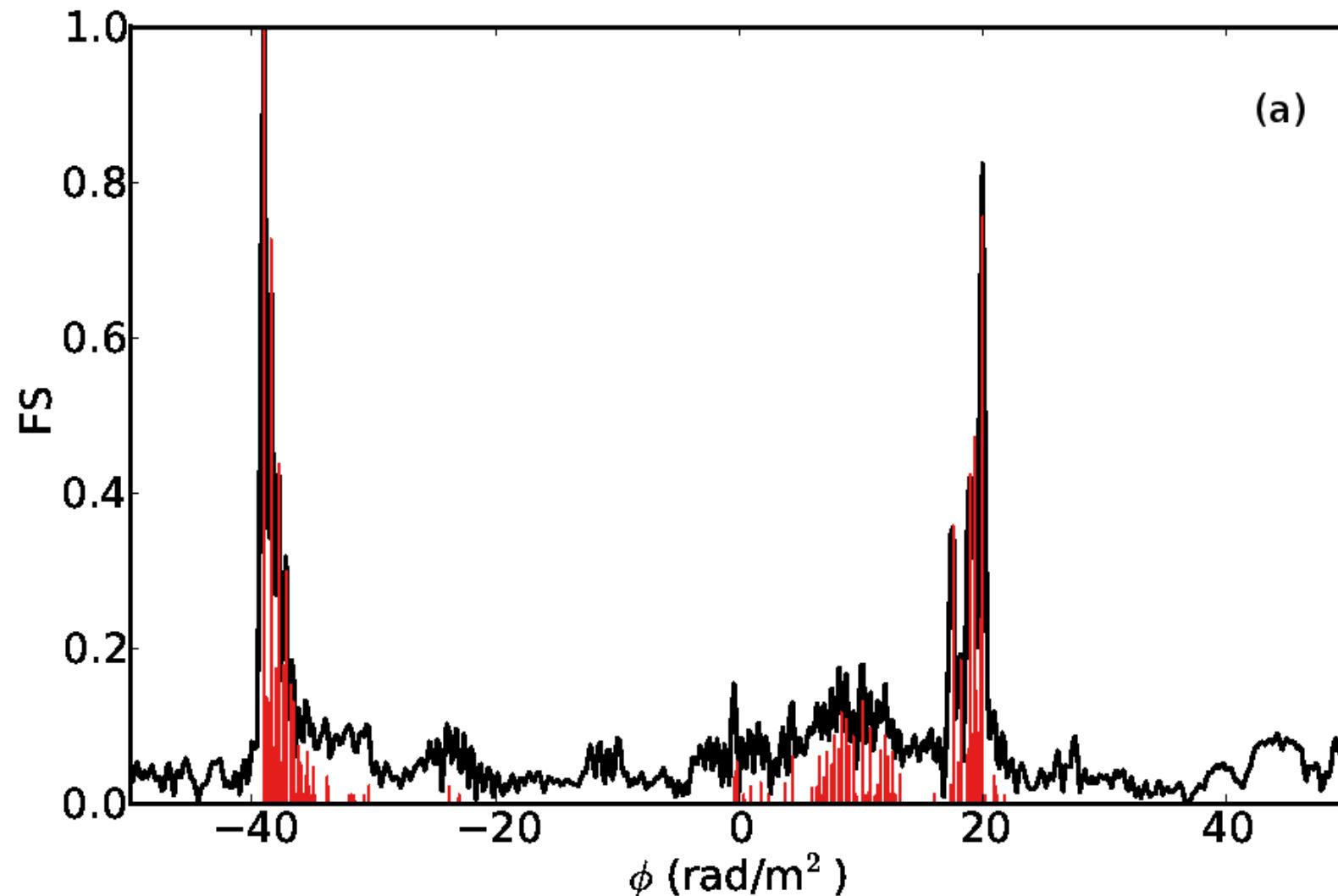
# 3D Structure



# Statistics

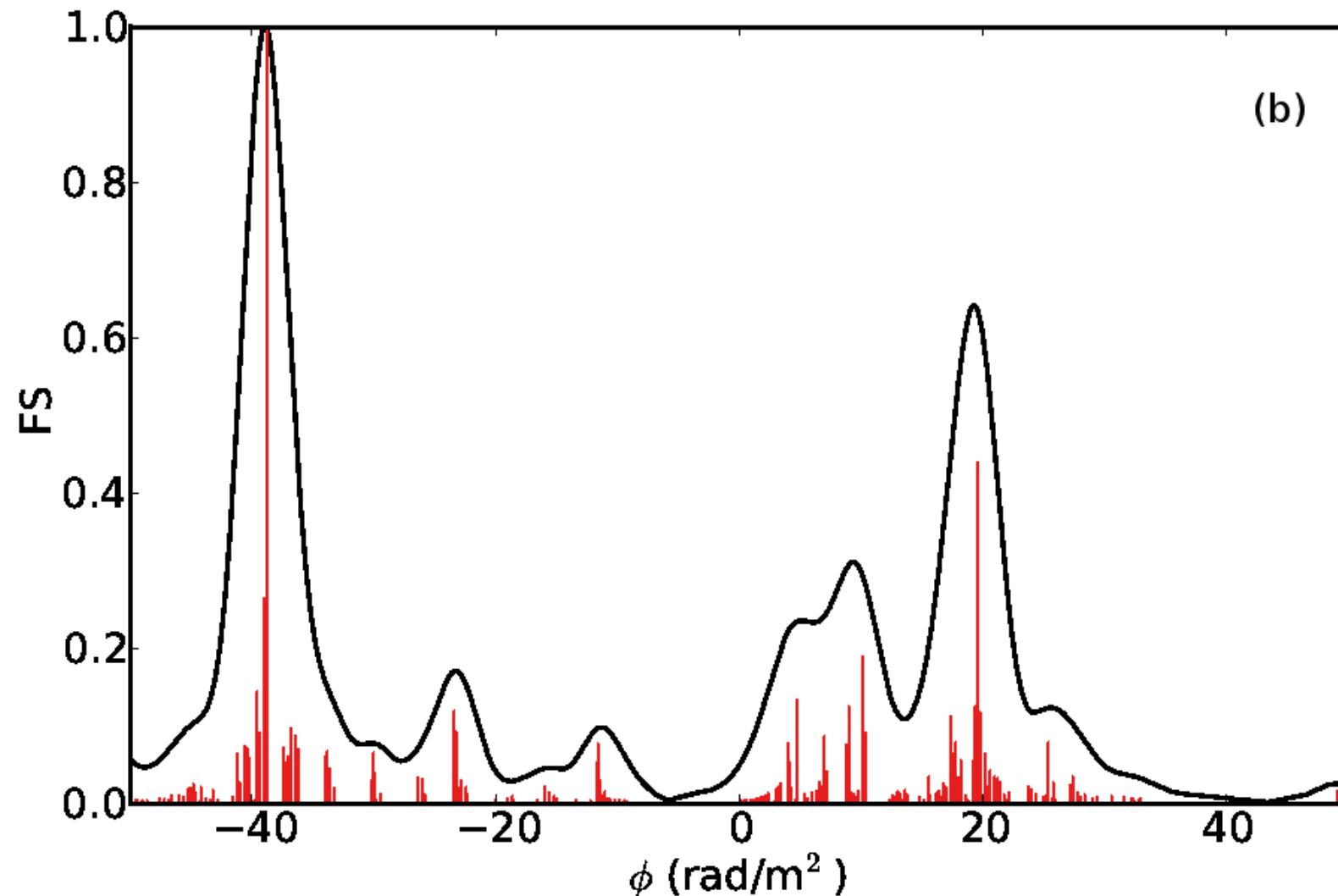


# Appearance



110 to 250 MHz, similar to the LOFAR high band antennas

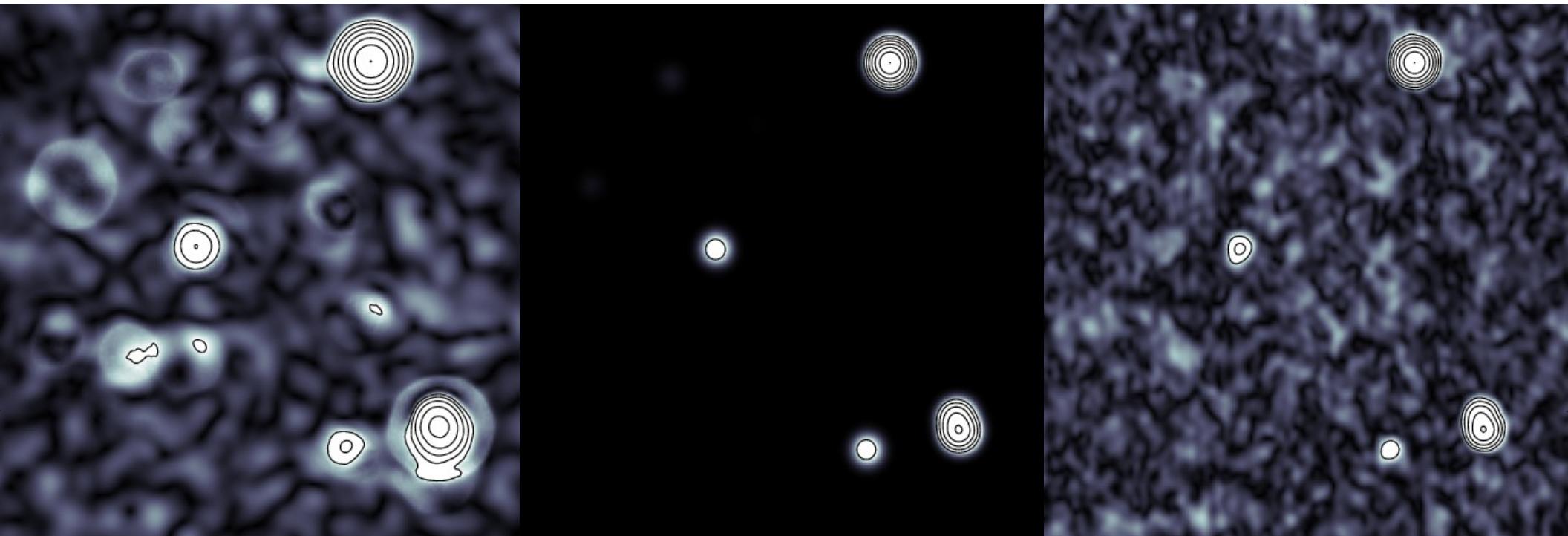
# Appearance

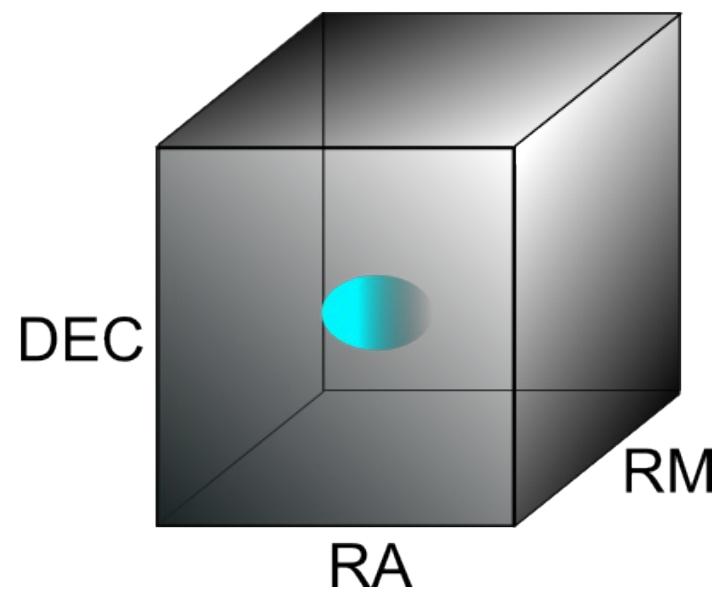


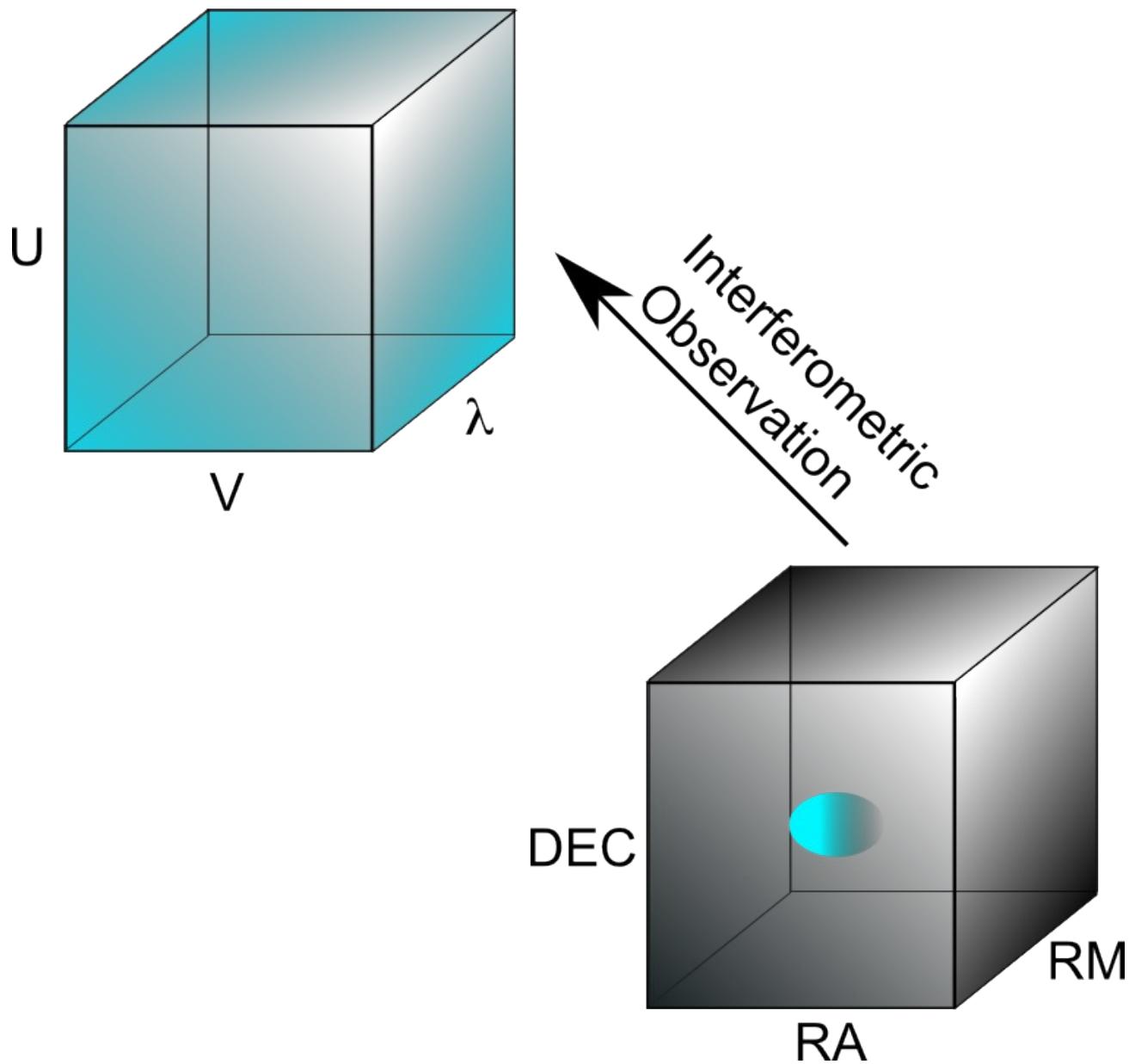
300 to 900 MHz similar to the low frequency portion of the GMIMS survey

# Faraday Synthesis

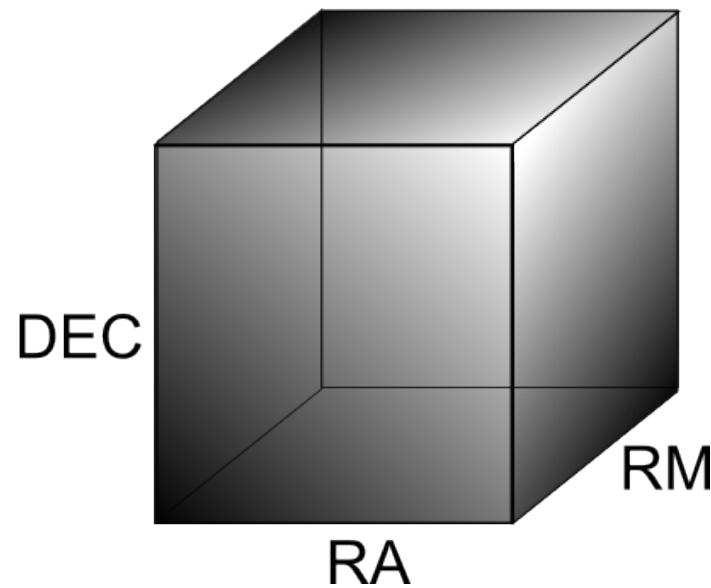
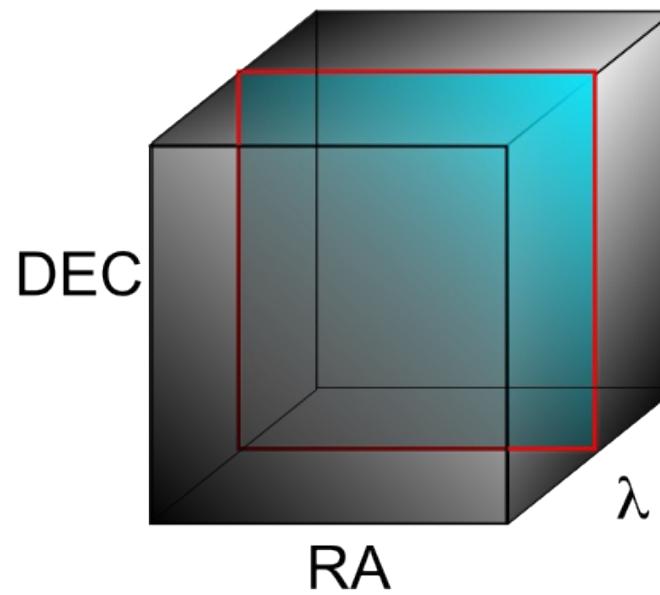
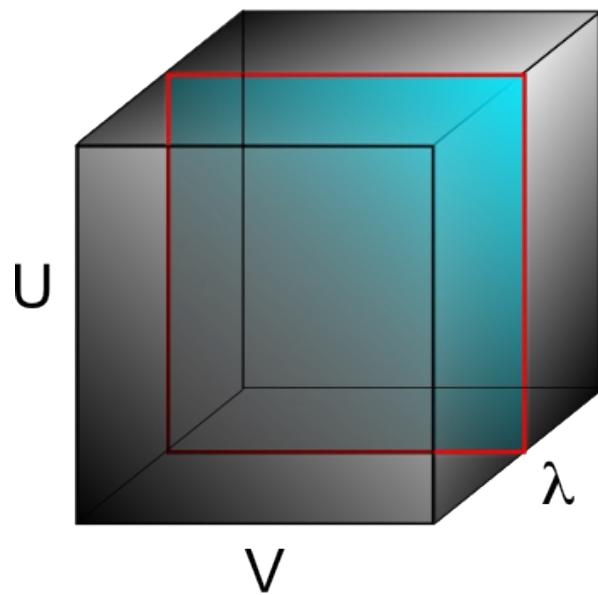
The synergy of aperture and rotation measure synthesis



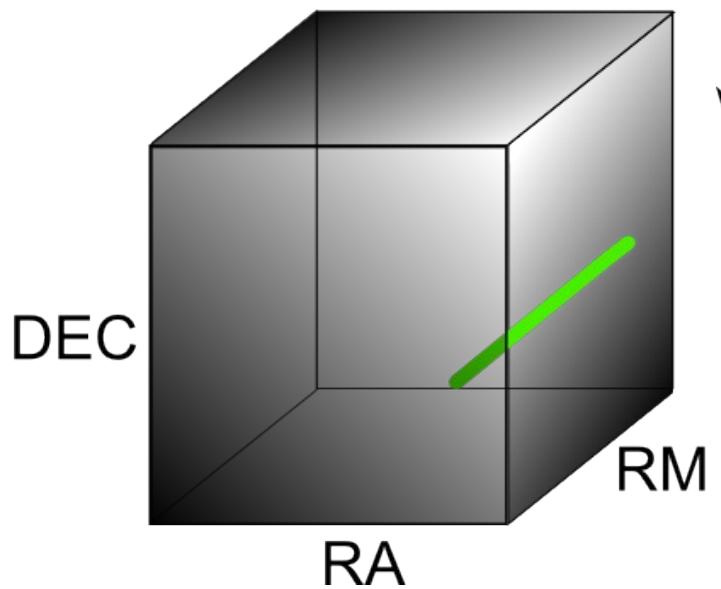
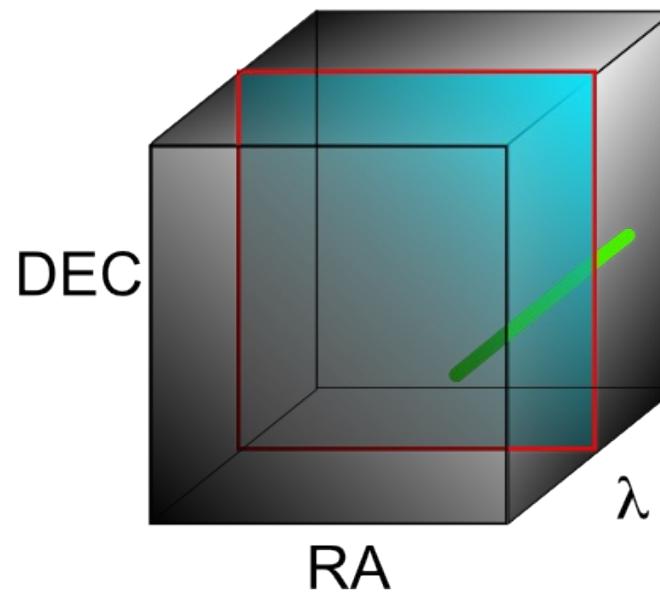
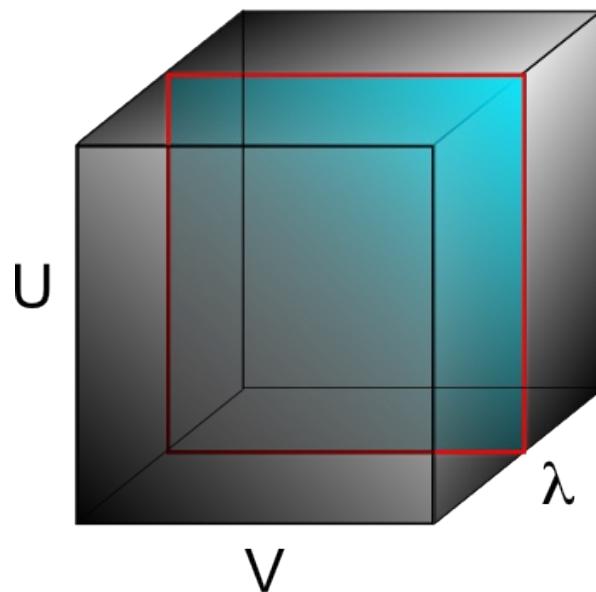




## 2-d Image Synthesis



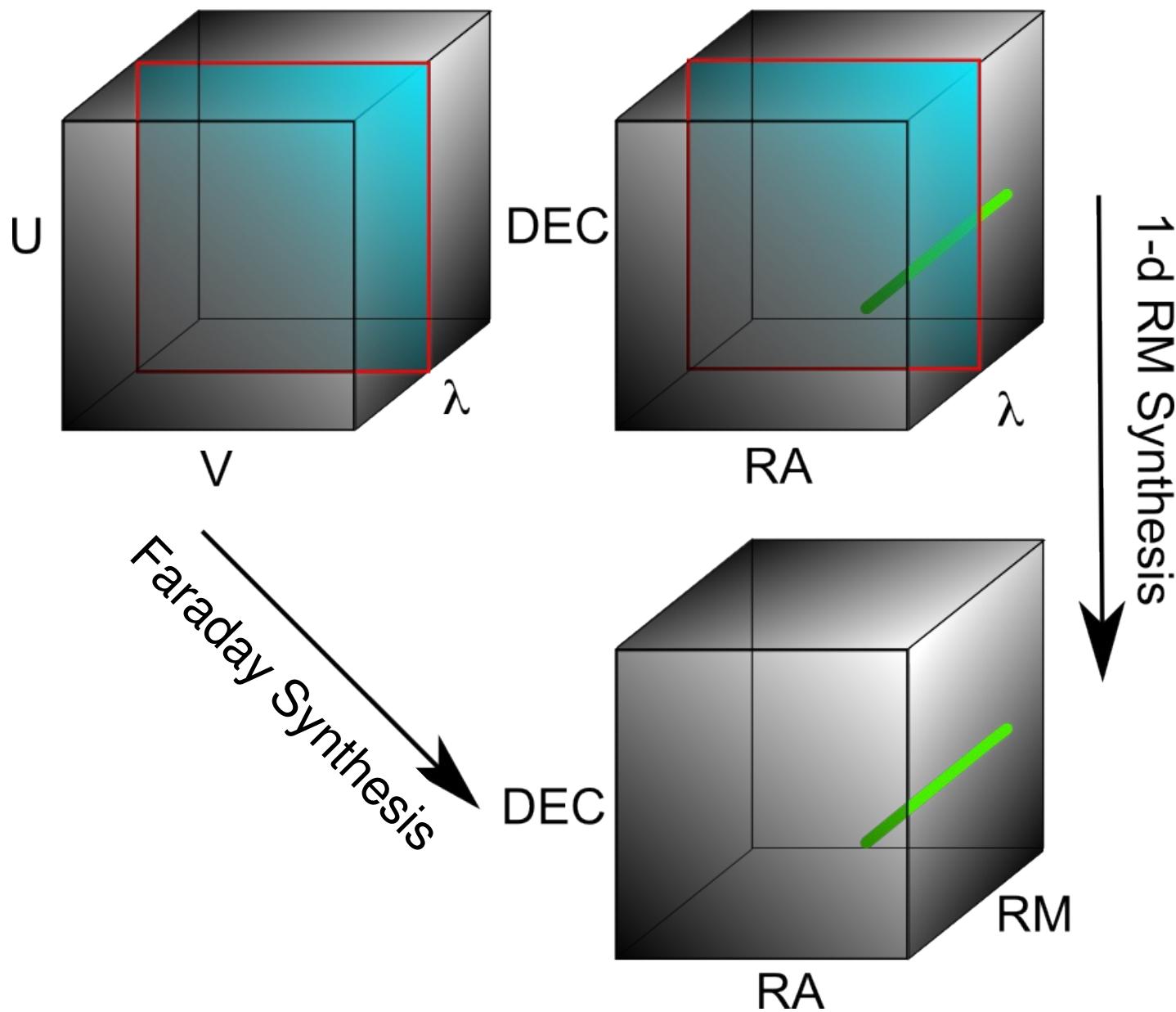
2-d Image Synthesis

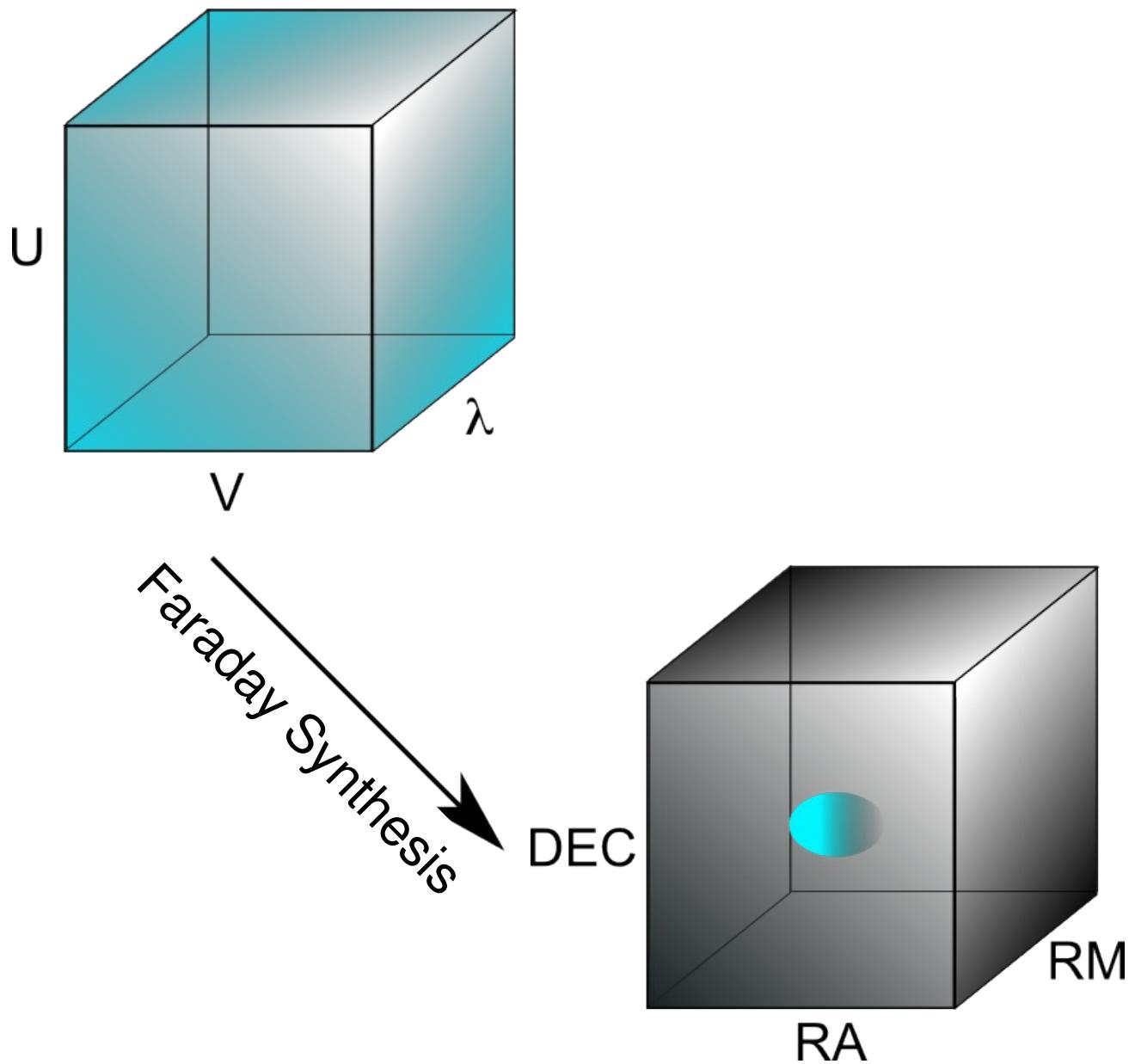


1-d RM Synthesis

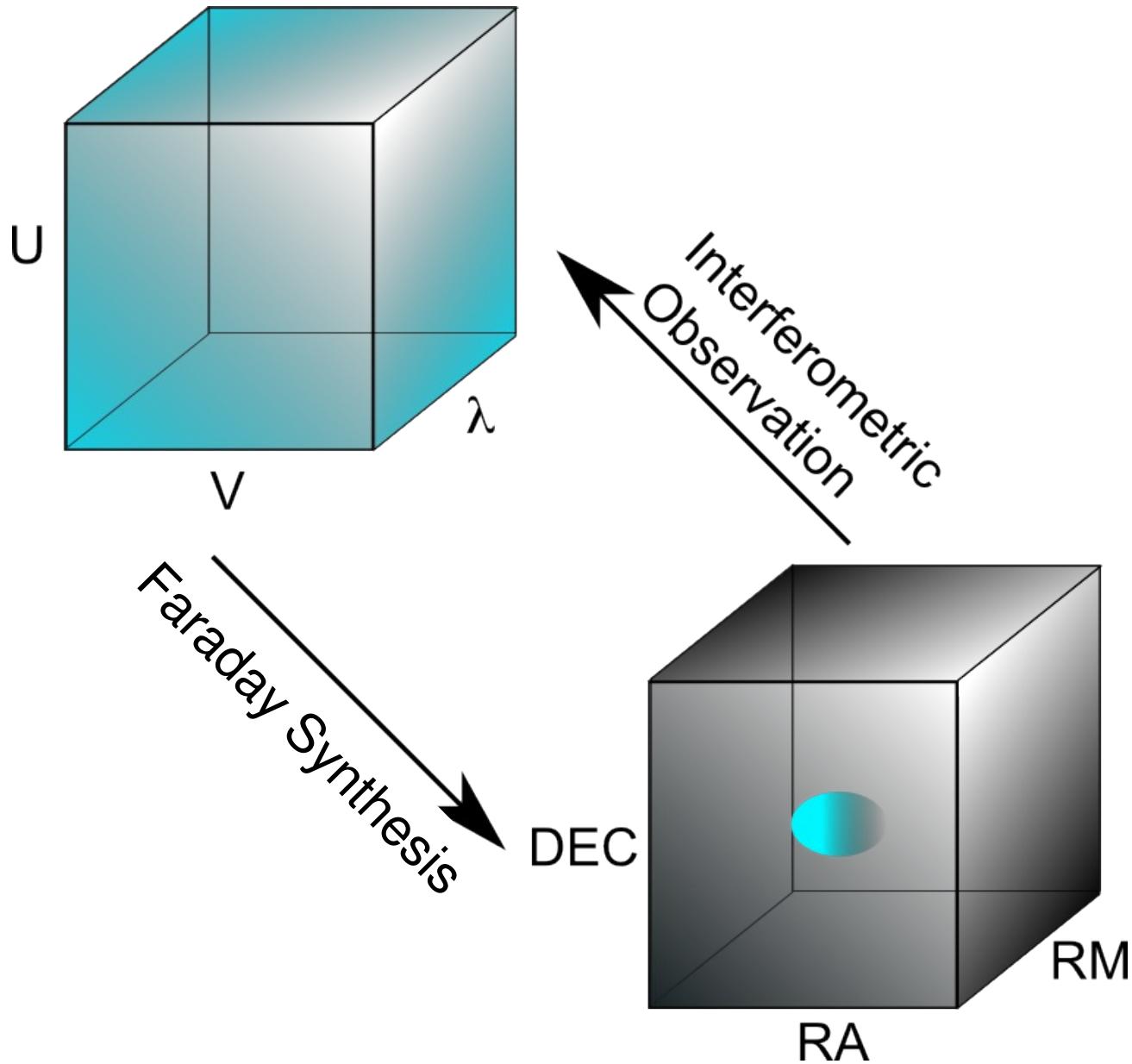


2-d Image Synthesis





# Faraday Synthesis

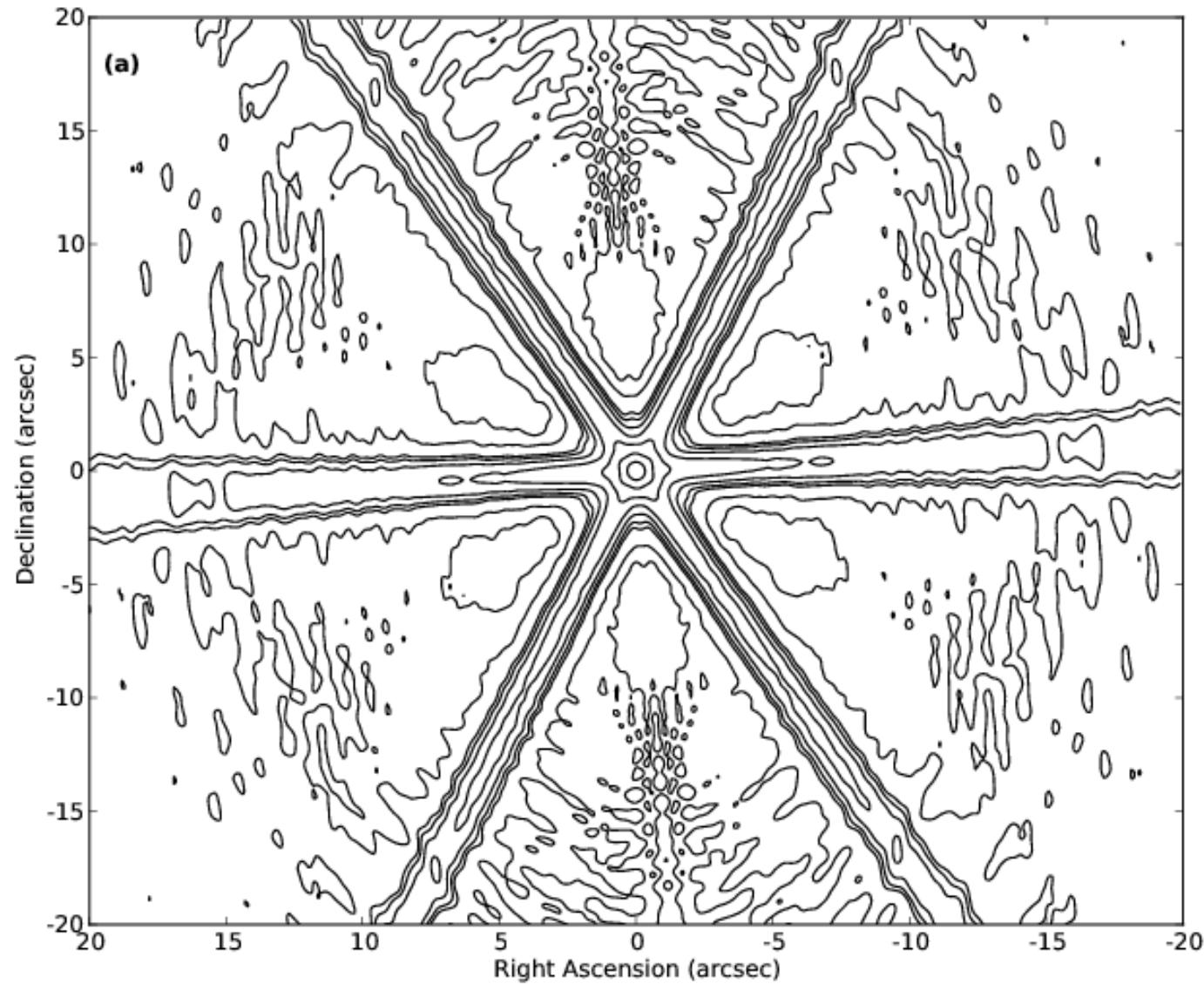


# Faraday synthesis

$$\text{PSF}_{\text{3D}} \stackrel{?}{=} \text{PSF}_{\text{sky}} * \text{PSF}_{\text{RM}}$$

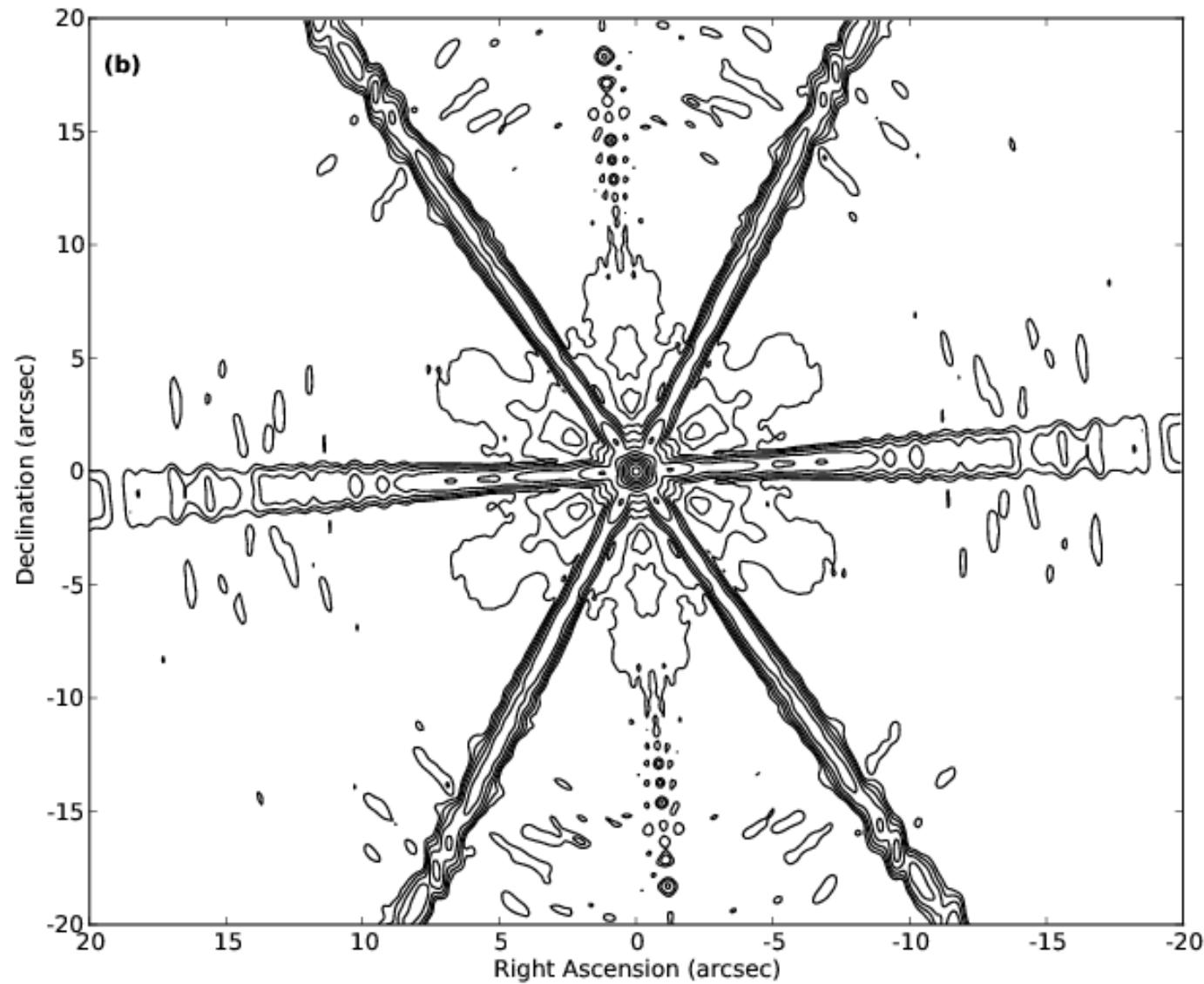
# 3D Dirty Beam

Image plane, Faraday depth = 0 rad/m<sup>2</sup>



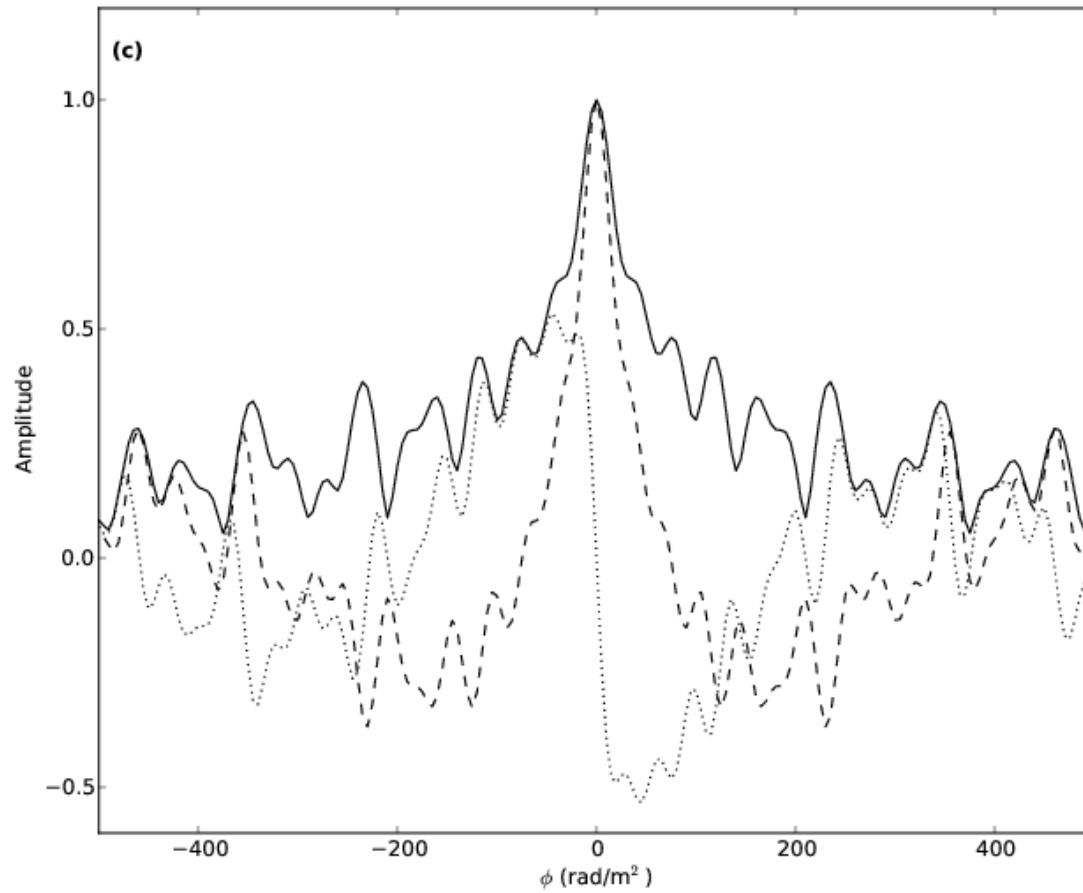
# 3D Dirty Beam

Image plane, Faraday depth = 50 rad/m<sup>2</sup>



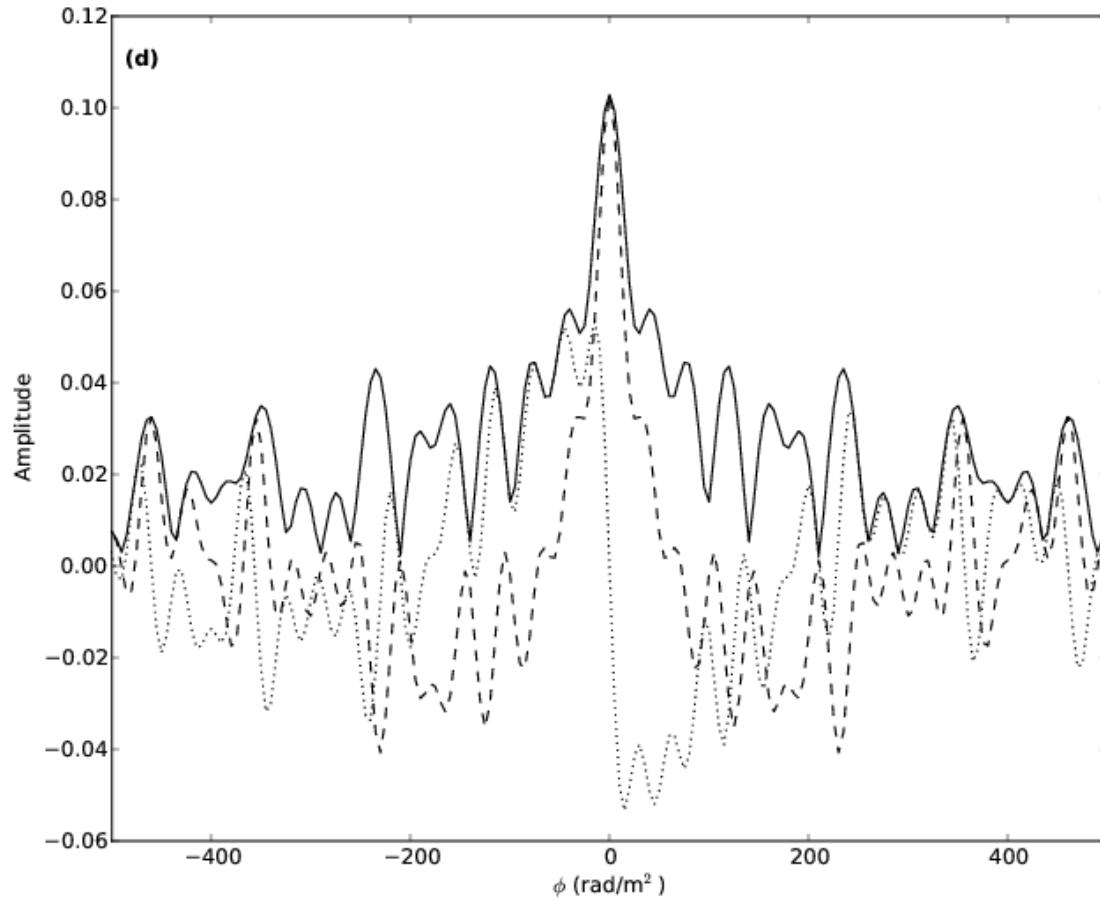
# 3D Dirty Beam

## Faraday depth axis, phase center

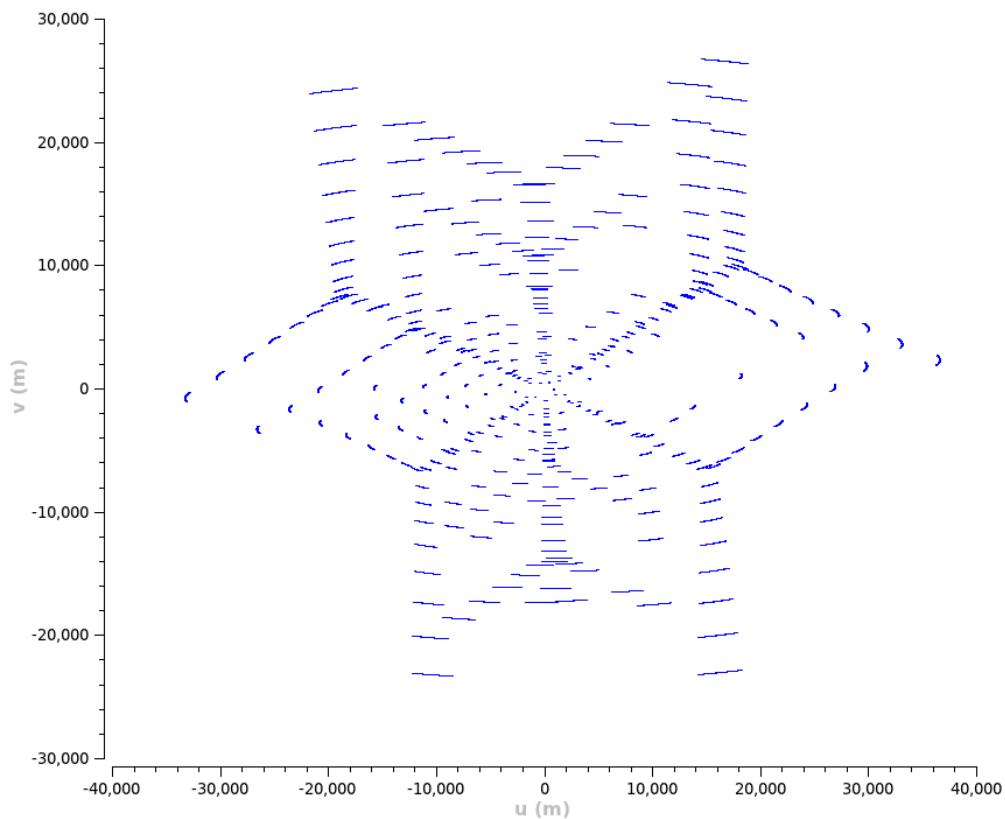


# 3D Dirty Beam

## Faraday depth axis, off-center



# Mock Observations

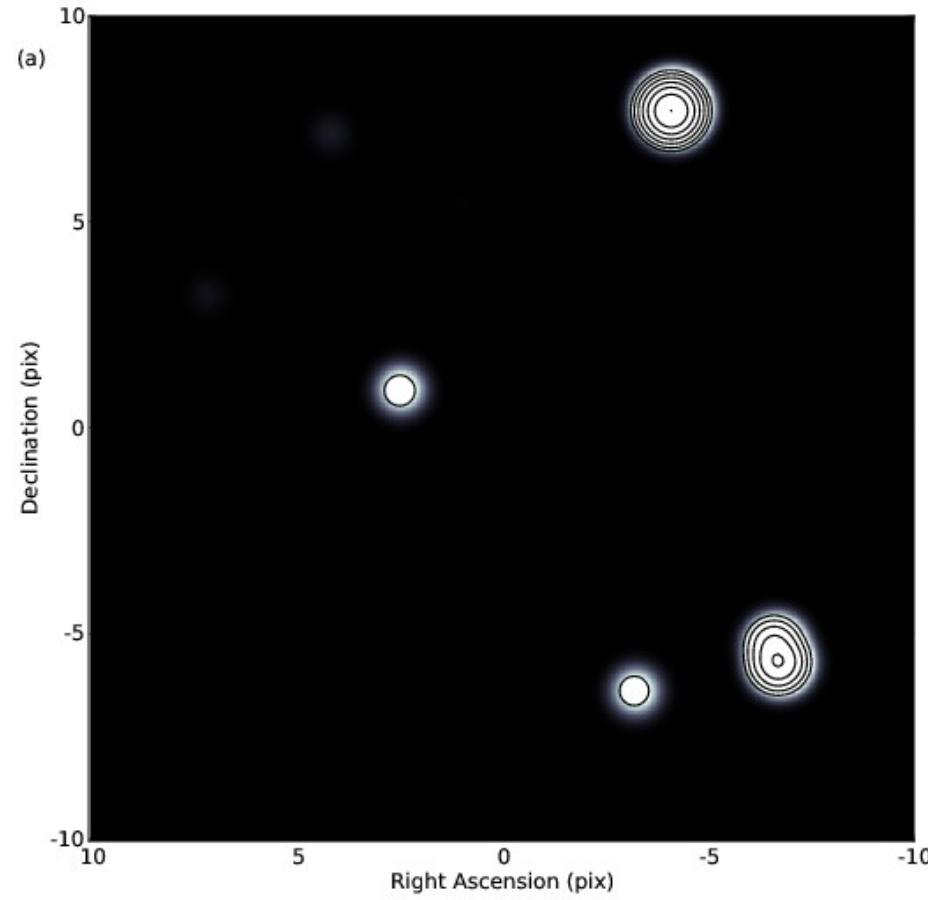


30 point sources  
random locations  
random fluxes (0.06 - 64 Jy)

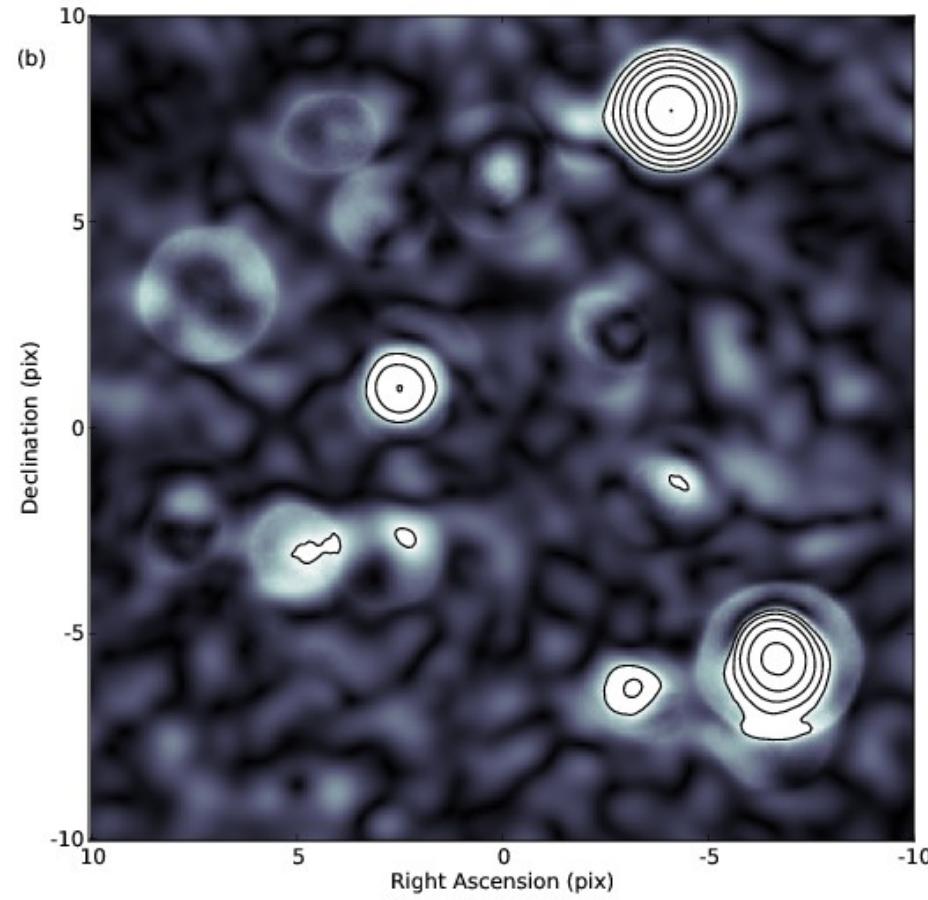
“observed” with the VLA  
1-4 GHz (x64 channels)

Gaussian white noise, ~10Jy

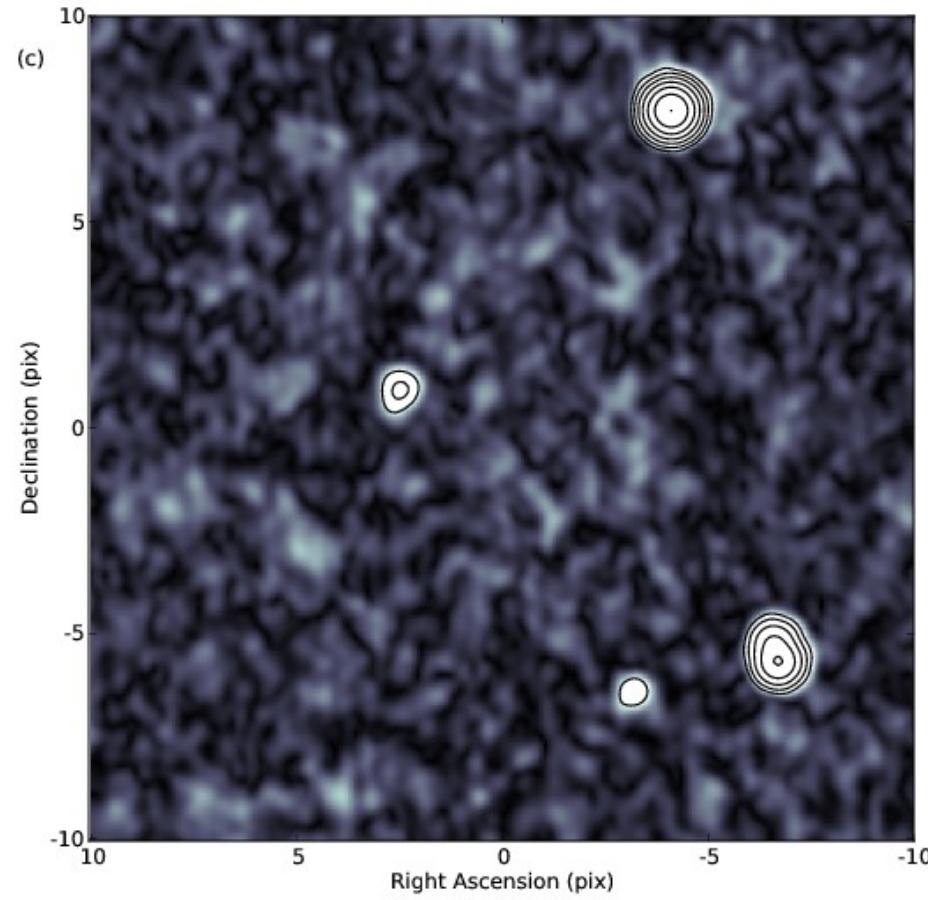
# Model



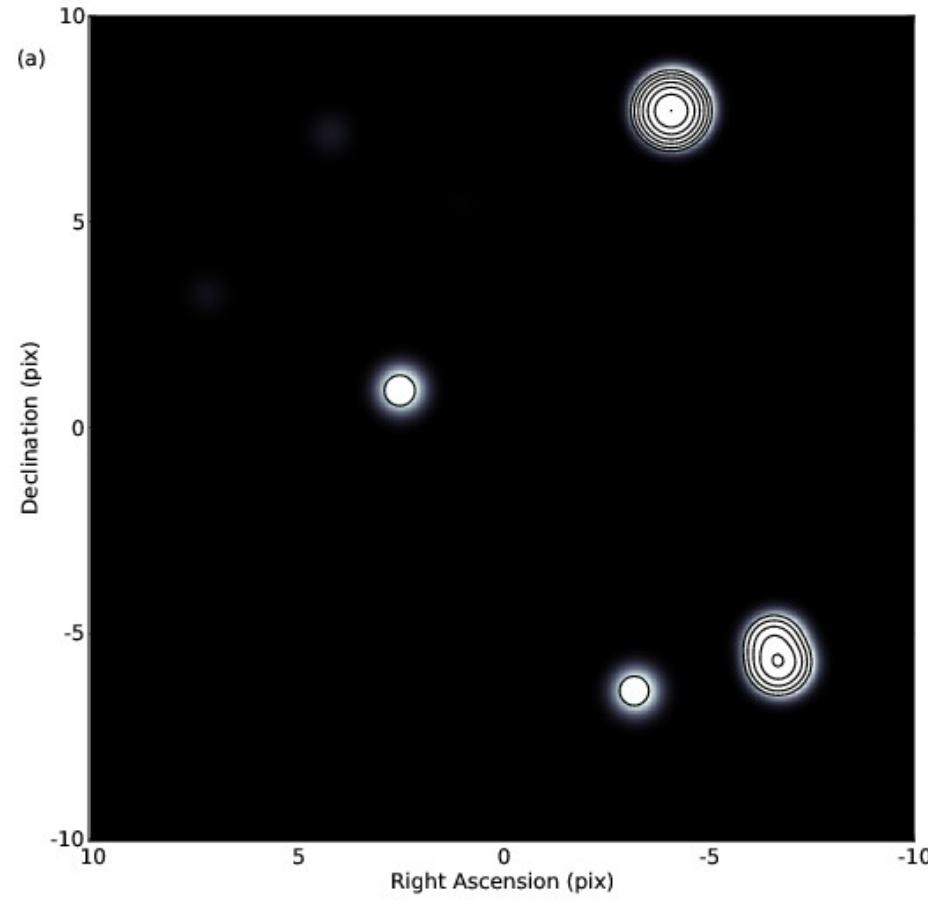
# Aperture + RM Synthesis



# Faraday synthesis



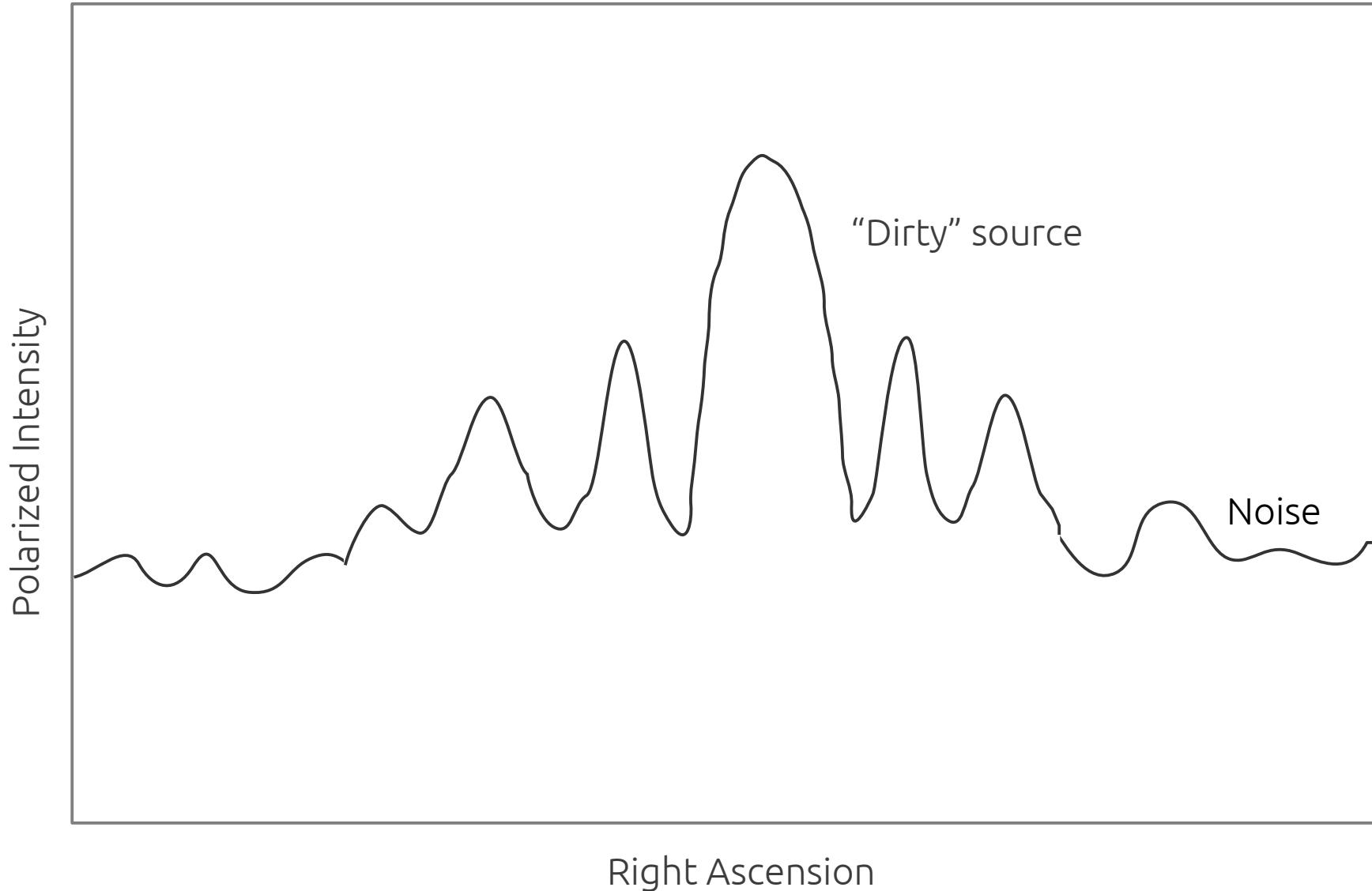
# Model





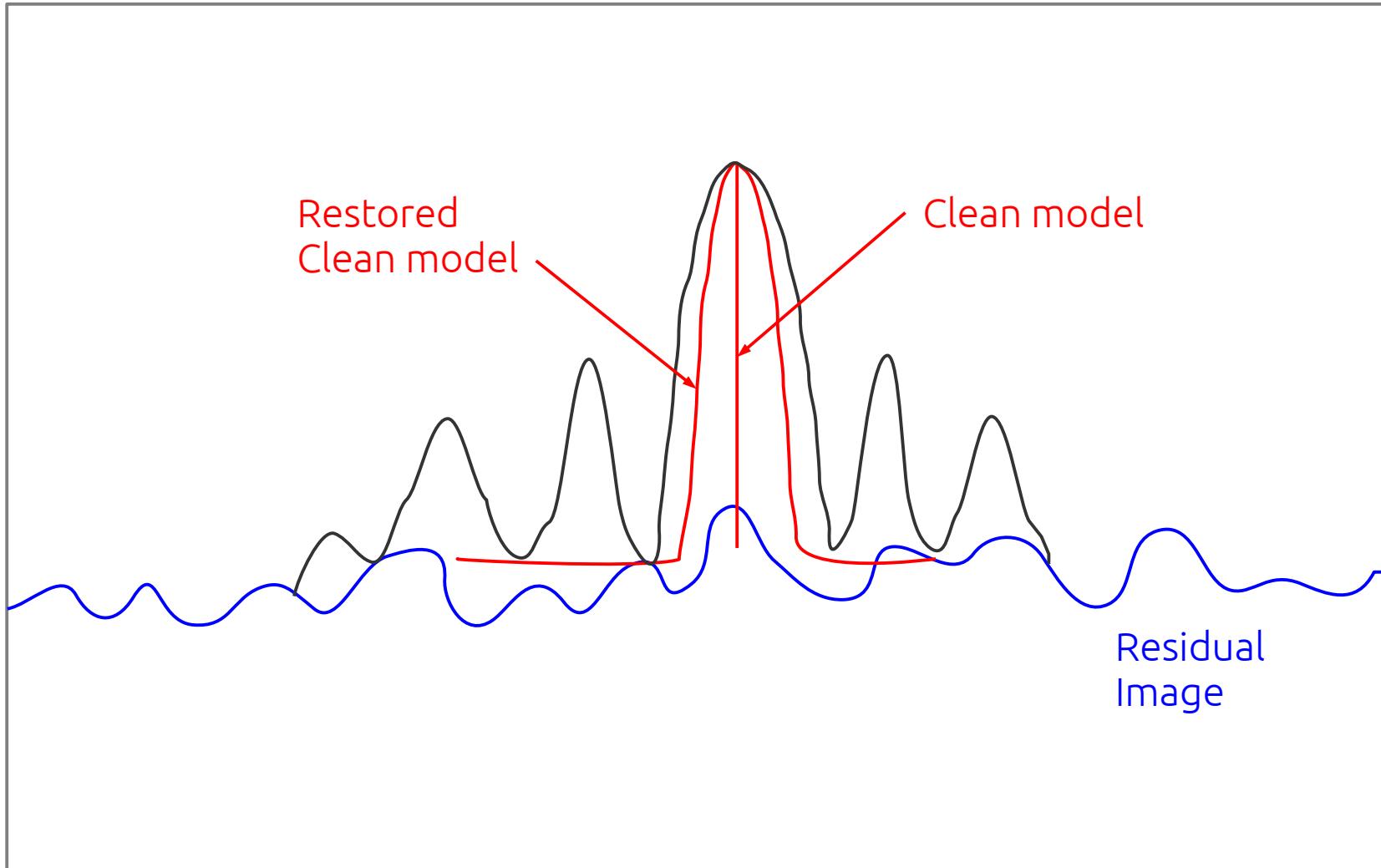
# Why the artifacts?

## 1D Dirty image



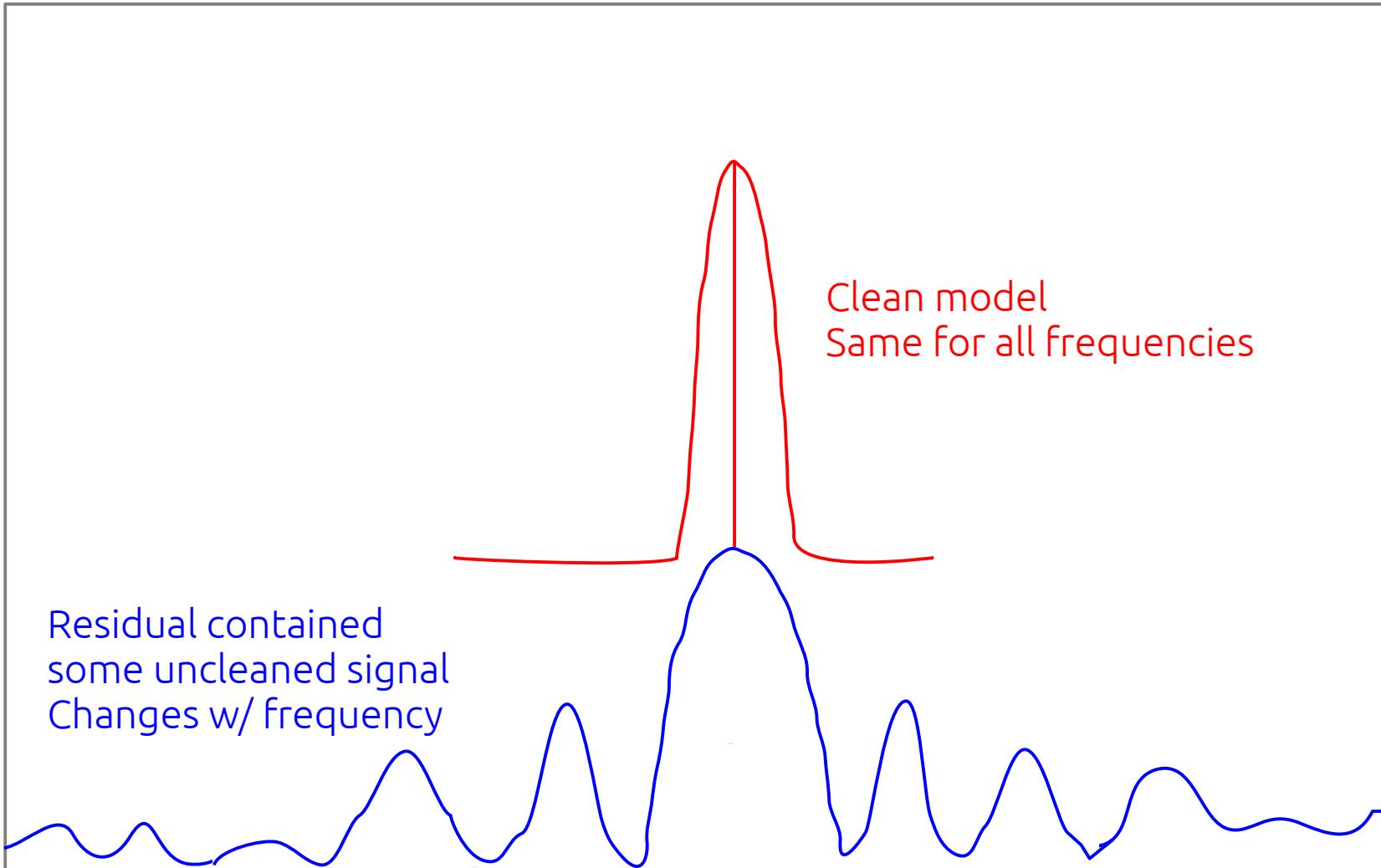
# Why the artifacts?

Cleaning a single frequency



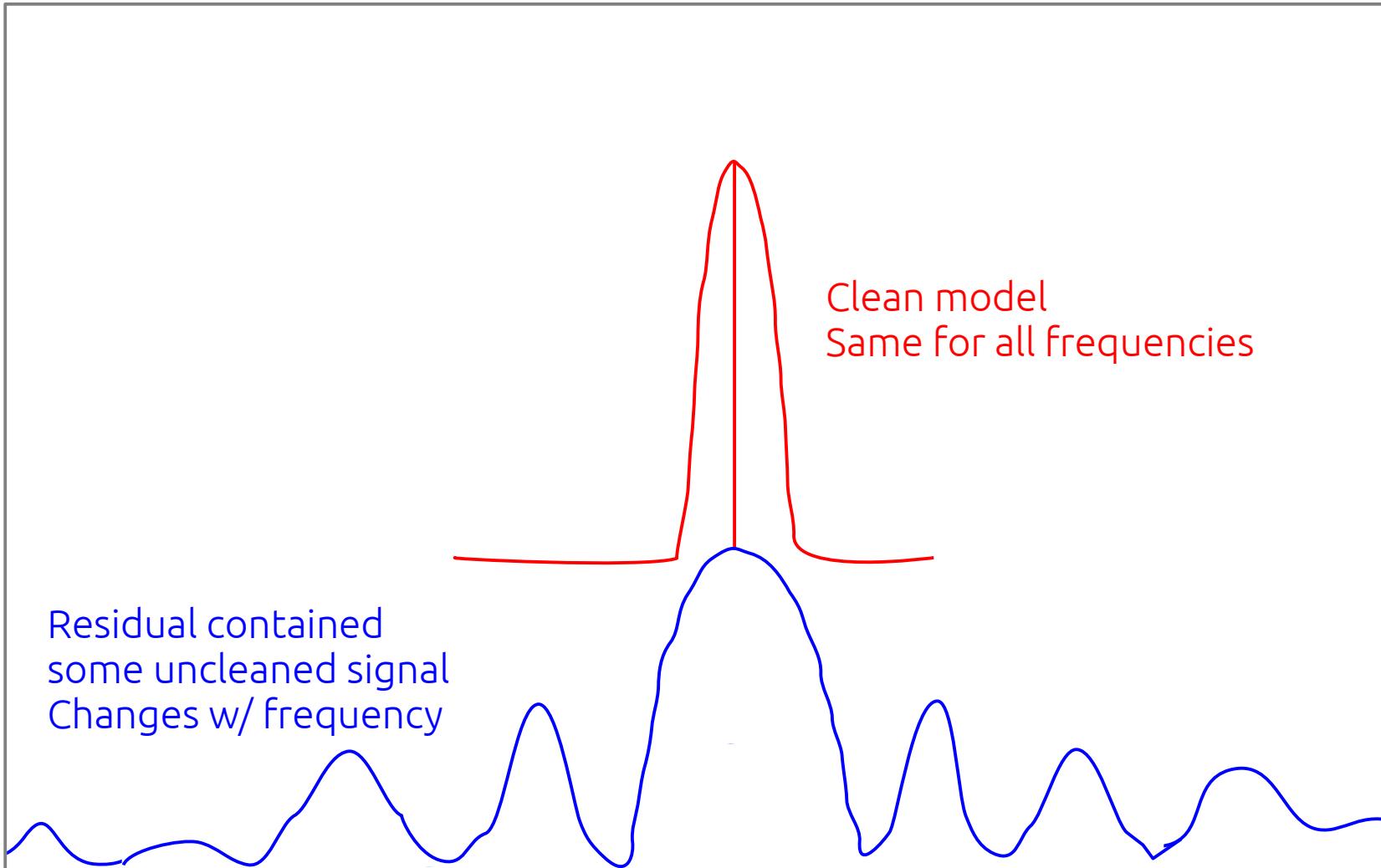
# Why the artifacts?

After combining multiple frequencies

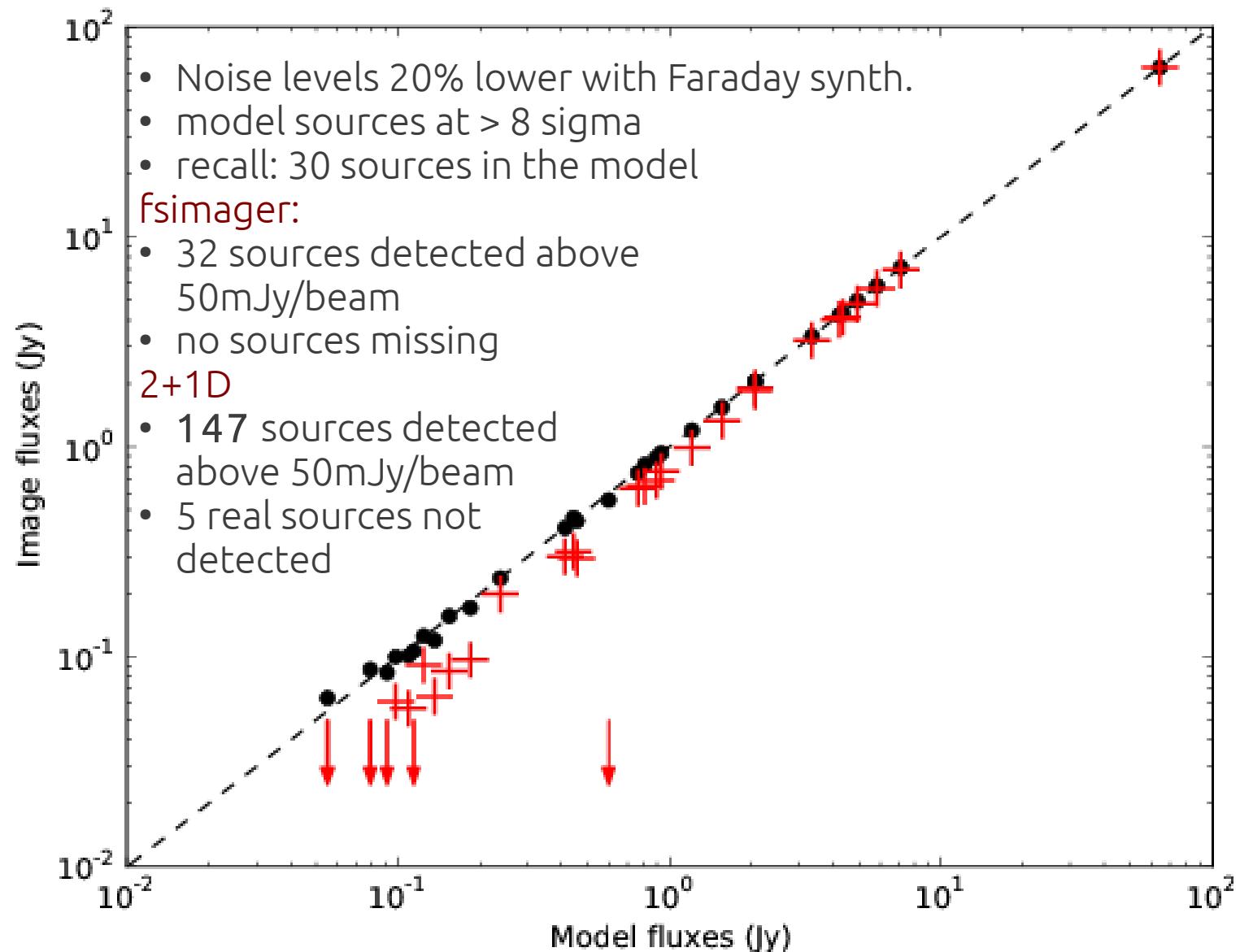


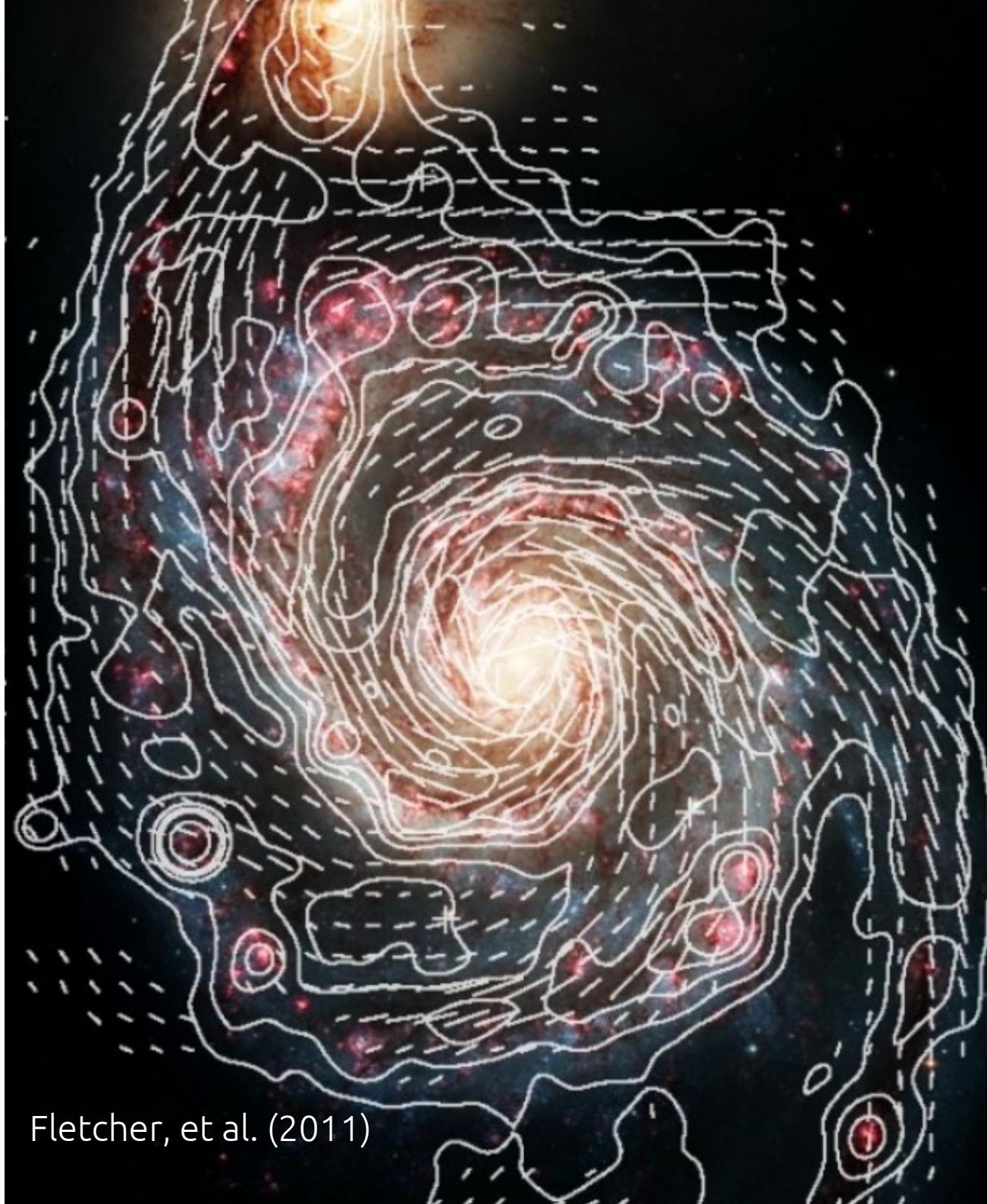
# Why the artifacts?

After combining multiple frequencies

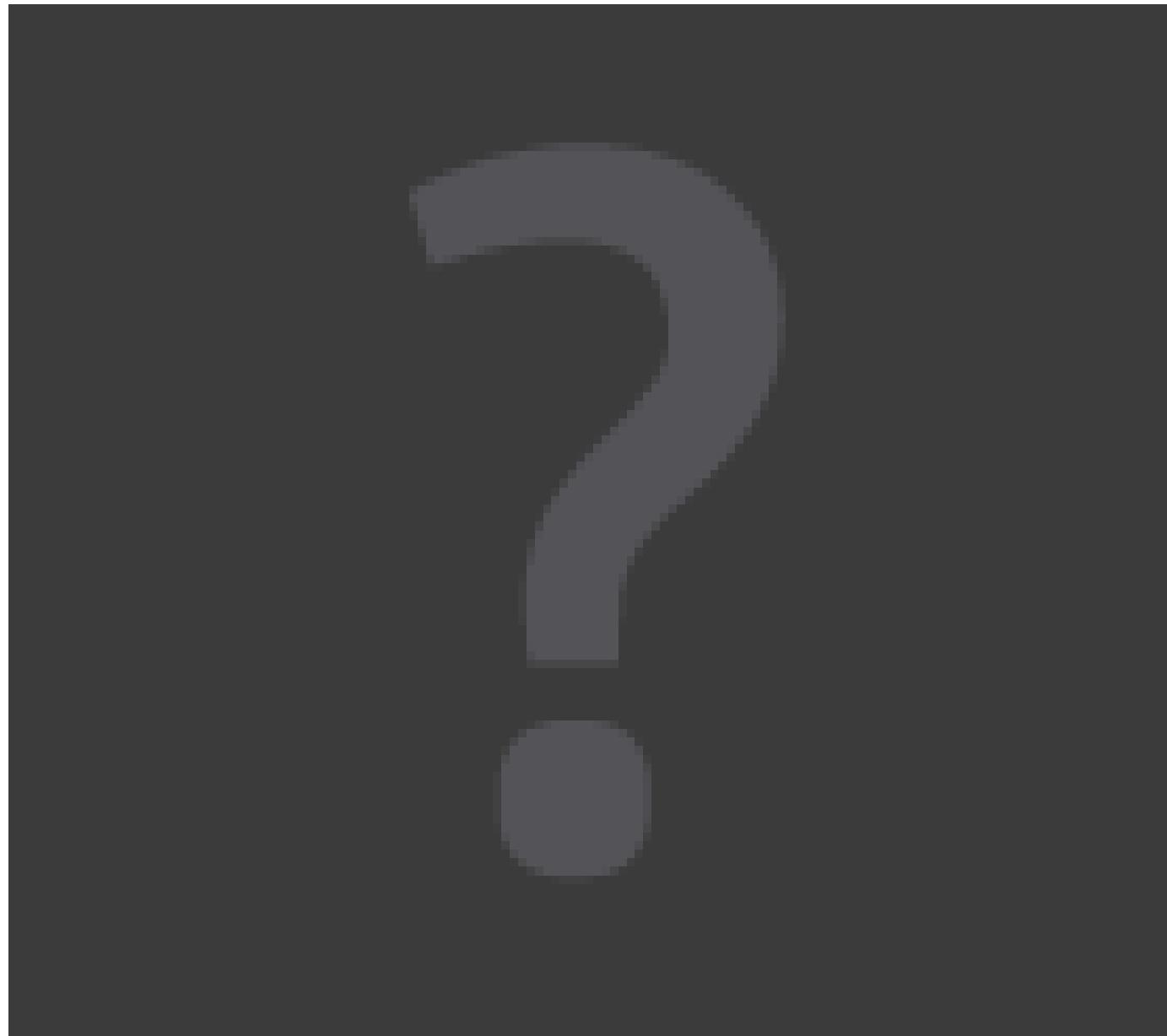


# Flux recovery





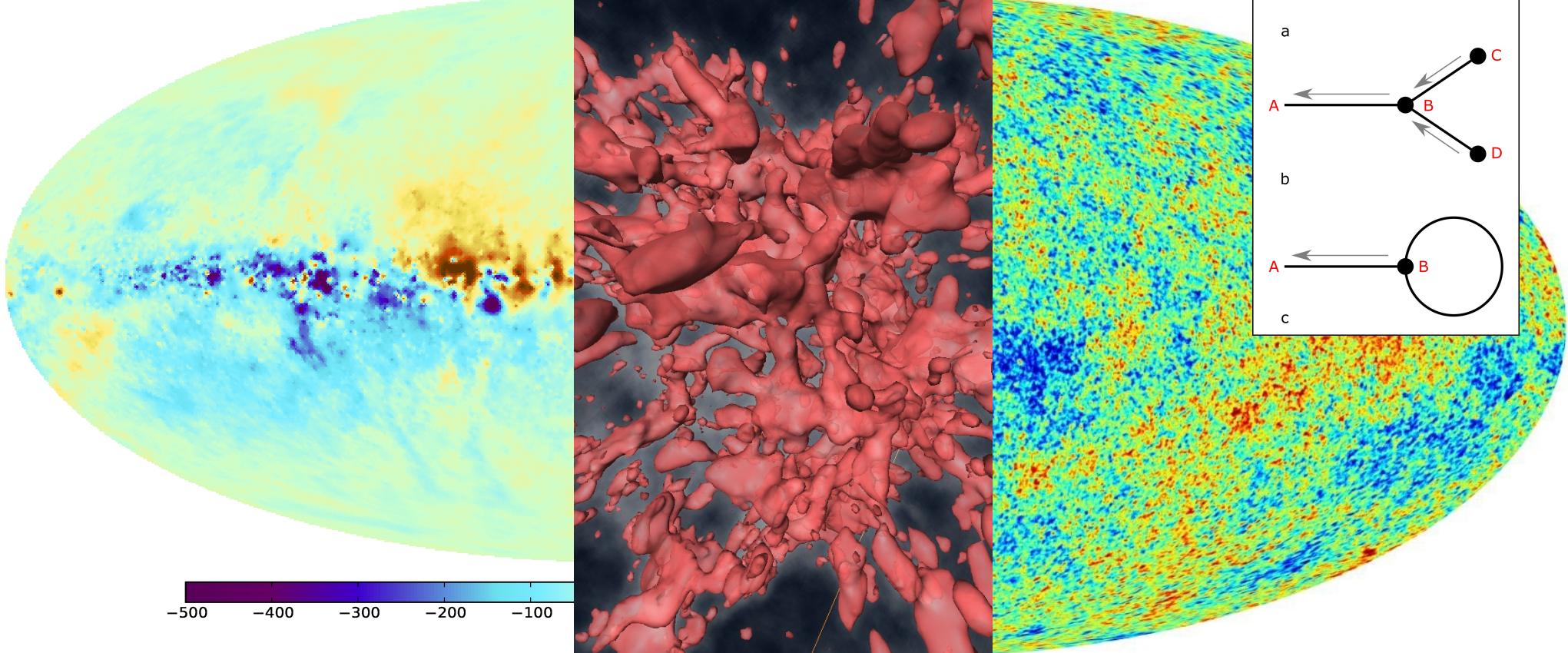
Fletcher, et al. (2011)



de Bruyn & Brentjens (2005)

# Information Field Theory

Extended critical filter and more...



[www.mpa-garching.mpg.de/ift](http://www.mpa-garching.mpg.de/ift)

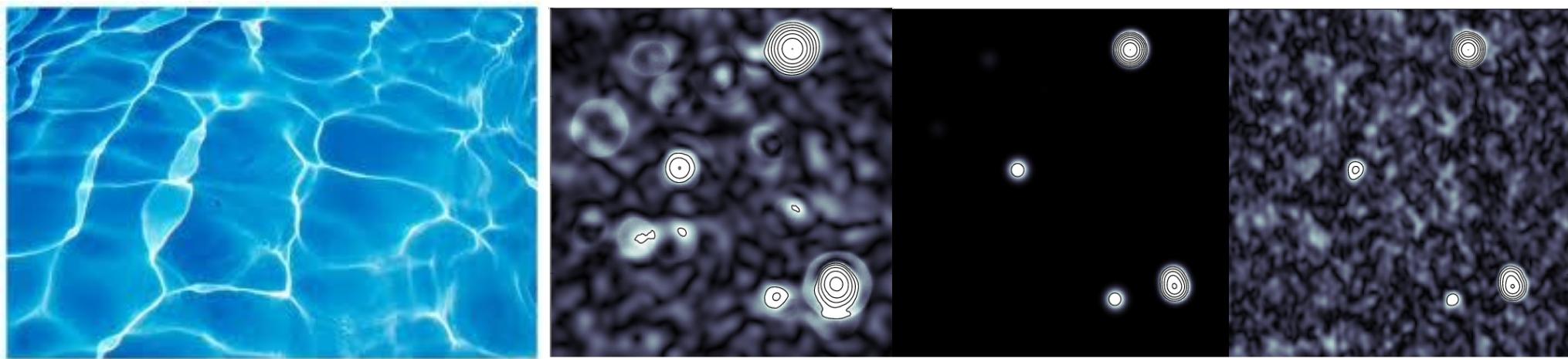
# Faraday Caustics Summary

- Strong “spikes” in Faraday spectra
- Mark reversals of LOS B-field
- Are sheets in 3D Faraday spectrum
- Reveal properties of magnetic turbulence

# Faraday synthesis summary

- Improves upon aperture + RM synthesis
  - Better fidelity
  - Less noise and better noise statistics
  - Higher resolution
  - Computationally cheaper (in principle)
- Provides a solid framework for building 3D imaging algorithms
- Being considered for POSSUM & CHANGES

# Thank you!



**Faraday caustics:** Singularities in the Faraday spectrum and their utility as probes of magnetic field properties  
Bell, Junklewitz & Enßlin, A&A 535, A85 (2011)

**Faraday synthesis:** The synergy of aperture and rotation measure synthesis  
Bell & Enßlin A&A 540, A80 (2012)