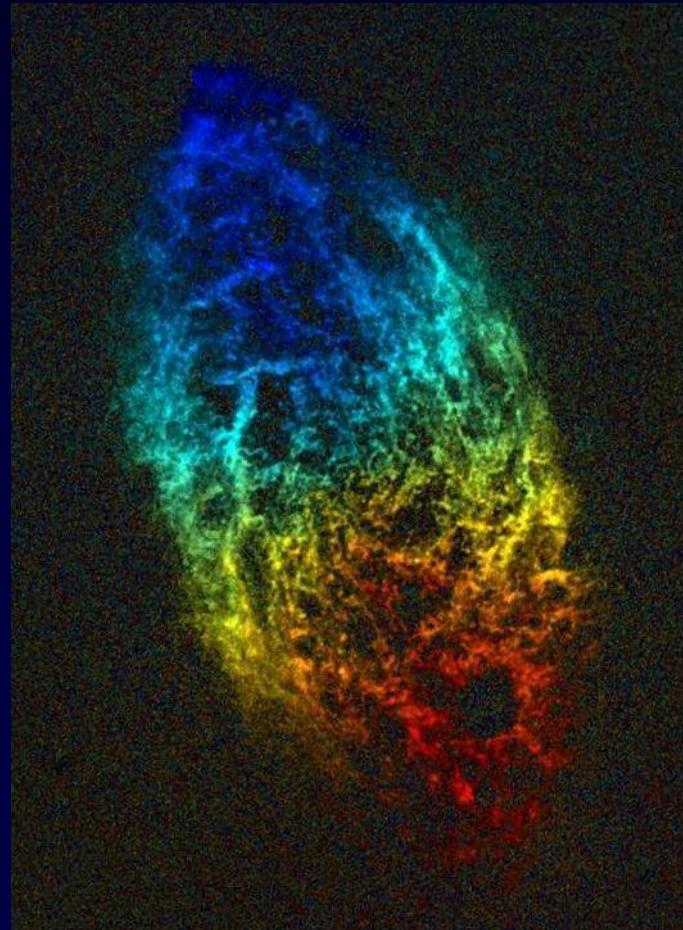
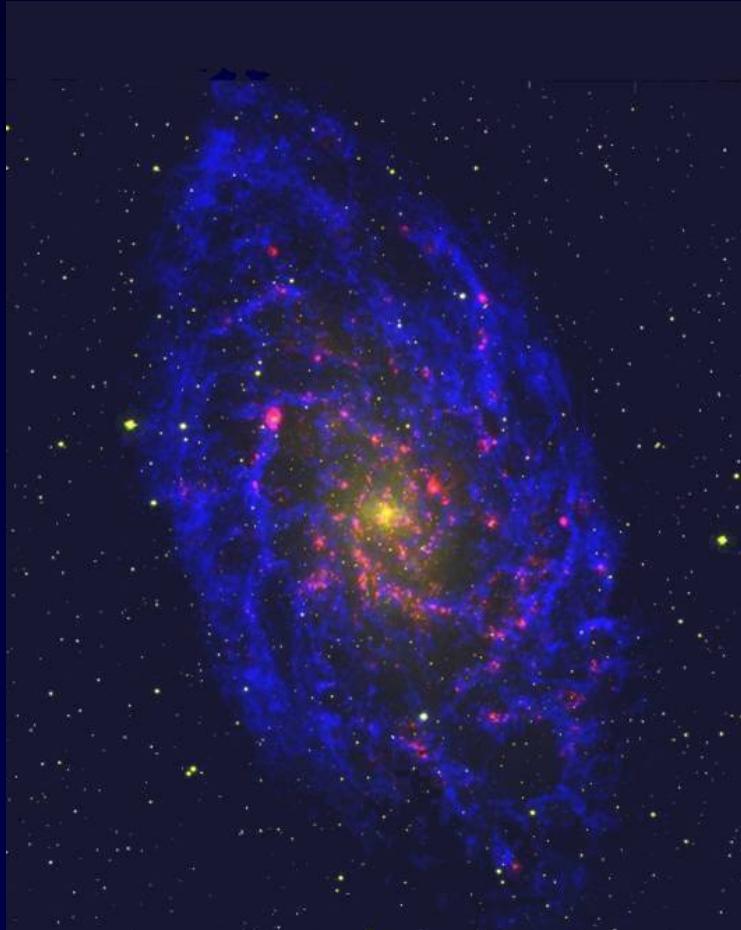


Structure and Kinematics of Galaxies



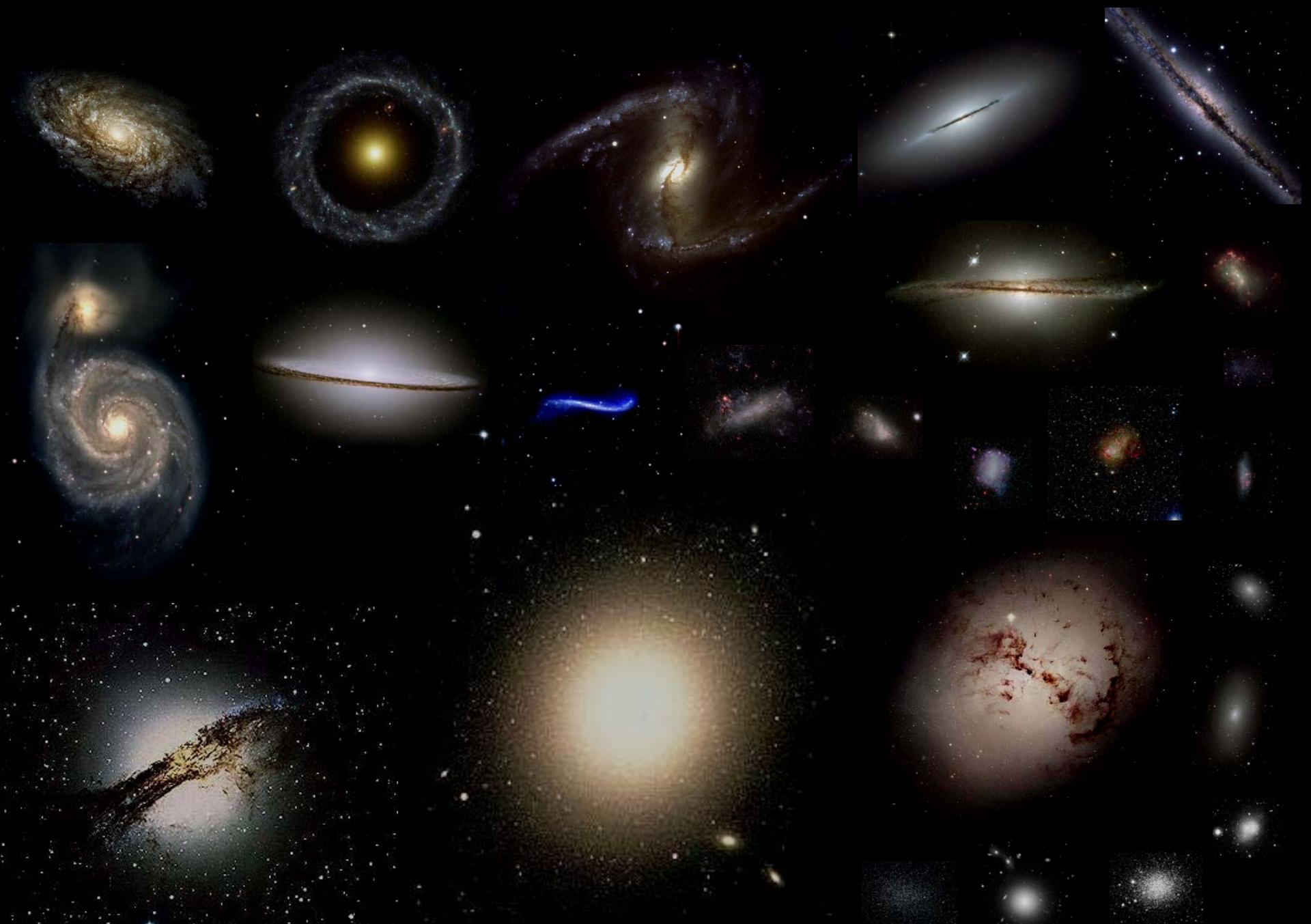
U. Klein



Outline

1. Galaxy zoo
2. The structure of disk galaxies
3. Photometry
4. Kinematics of disk galaxies
5. Relation to magnetic fields

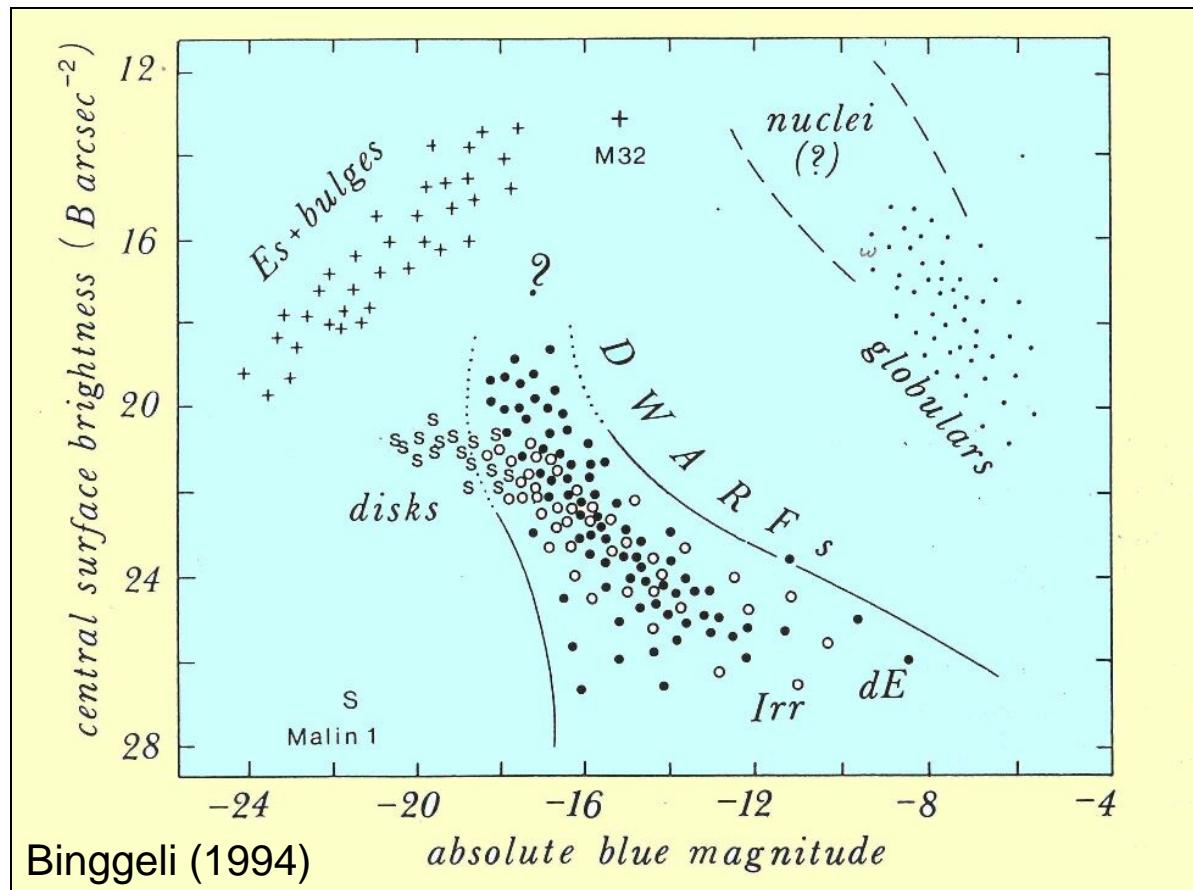




Kingberg, 19 July 2011

Galaxy zoo

Galaxy types: disk galaxies (Sa, Sb, Sc, Sd, Sm, dIrr)
S0s ('interlude'), SBa ... have bars
elliptical galaxies (E0 ... E7, dE, dSph)



disk galaxies:

- stellar bulge & disk
- gas disk ($\text{HI} + \text{H}_2$)
- hot gaseous corona
- ordered circular rotation of stellar and gaseous disk



elliptical galaxies:

- spherical or elliptical in projection
(prolate, oblate, triaxial?)
- entire gas in hot gaseous corona
- dE, dSph: no gas at all
- stars move on random elliptical orbits, no ordered rotation



disk galaxies:

- all prerequisites for B-field generation and sustainment

cold gas with ionized component

(differential) rotation, turbulence via SF and SNe

ellipticals:

- may possess B-fields (high conductivity), but

no SF \Rightarrow no relativistic particles \Rightarrow no synchrotron radiation \Rightarrow no detection

no SF \Rightarrow no turbulence

dE, dSph: no gas \Rightarrow no SF \Rightarrow no ...

so here focus on disk galaxies!

Constituents of spiral galaxies[†]

Component	Mass	dynamically
• stellar		
- thin disk	$4.7 \cdot 10^{10} M_{\odot}$	significant
- thick bulge	$6.2 \cdot 10^{10} M_{\odot}$	significant
• gaseous disk		
- atomic neutral hydrogen (HI)	$3.1 \cdot 10^{10} M_{\odot}$	significant
- molecular hydrogen (H_2)	$7.5 \cdot 10^9 M_{\odot}$	significant (?)
- ionized/hot gas (HII)	$5.0 \cdot 10^8 M_{\odot}$	insignificant
- dust	$4.0 \cdot 10^8 M_{\odot}$	insignificant
• relativistic plasma	$10 - 50 M_{\odot}$	insignificant
• dark halo	$5.0 \cdot 10^{11} M_{\odot}$	dominant

† e.g. NGC 7331

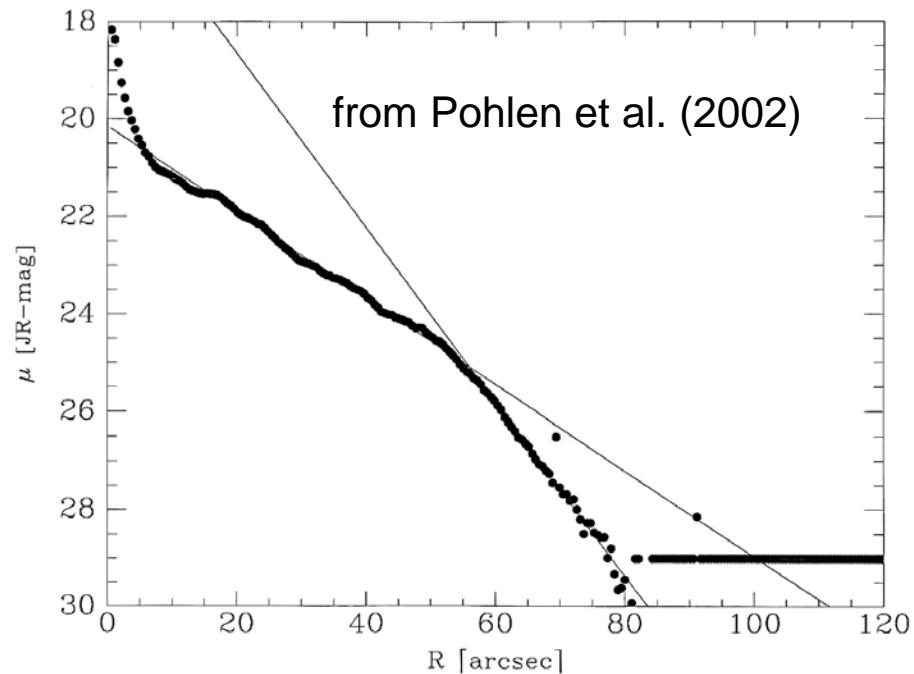
Structure of disk galaxies

stellar disk: exponential decline of brightness

$$I(R) = I_0 \cdot e^{-R/R_d}$$

$I(R)$ and I_0 have units of mag/③"

conversion to $L_\odot \text{ pc}^{-2}$ for optical band X via



$$I_X = 4.25 \cdot 10^{8+0.4\left[\left(\frac{M_{\odot,X}}{\text{mag}}\right)-\left(\frac{\mu_X}{\text{mag/G''}}\right)\right]} \cos i \quad L_\odot \text{ pc}^{-2}$$

conversion to mass surface density then via mass-to-light ratio for that band:

$$\left(\frac{\Sigma_X(R)}{M_\odot \text{ pc}^{-2}} \right) = K_X \cdot \left(\frac{I_X(R)}{L_\odot \text{ pc}^{-2}} \right)$$

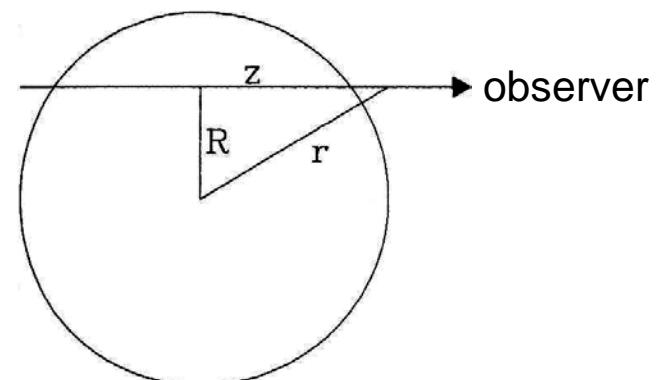
likewise for mass and luminosity density, respectively:

$$\left(\frac{\rho_X(r)}{M_\odot \text{ pc}^{-3}} \right) = K_X \cdot \left(\frac{j_X(r)}{L_\odot \text{ pc}^{-3}} \right)$$

use Poisson equation to convert to circular velocities (see kinematics)

note:

we use R for observed radial
brightness and r for intrinsic
galacto-centric distance



edge-on view:



truncated disk with finite thickness (Casertano 1983):

$$I(R, z) = I_0 e^{-\frac{R}{R_d}} \cosh^{-2} (z/z_0)$$

$\sim \exp[-(z/z_0)^2]$ for small z

with underlying density

$$\rho(R, z) = \rho_0(R) \cosh^{-2} (z/z_0)$$

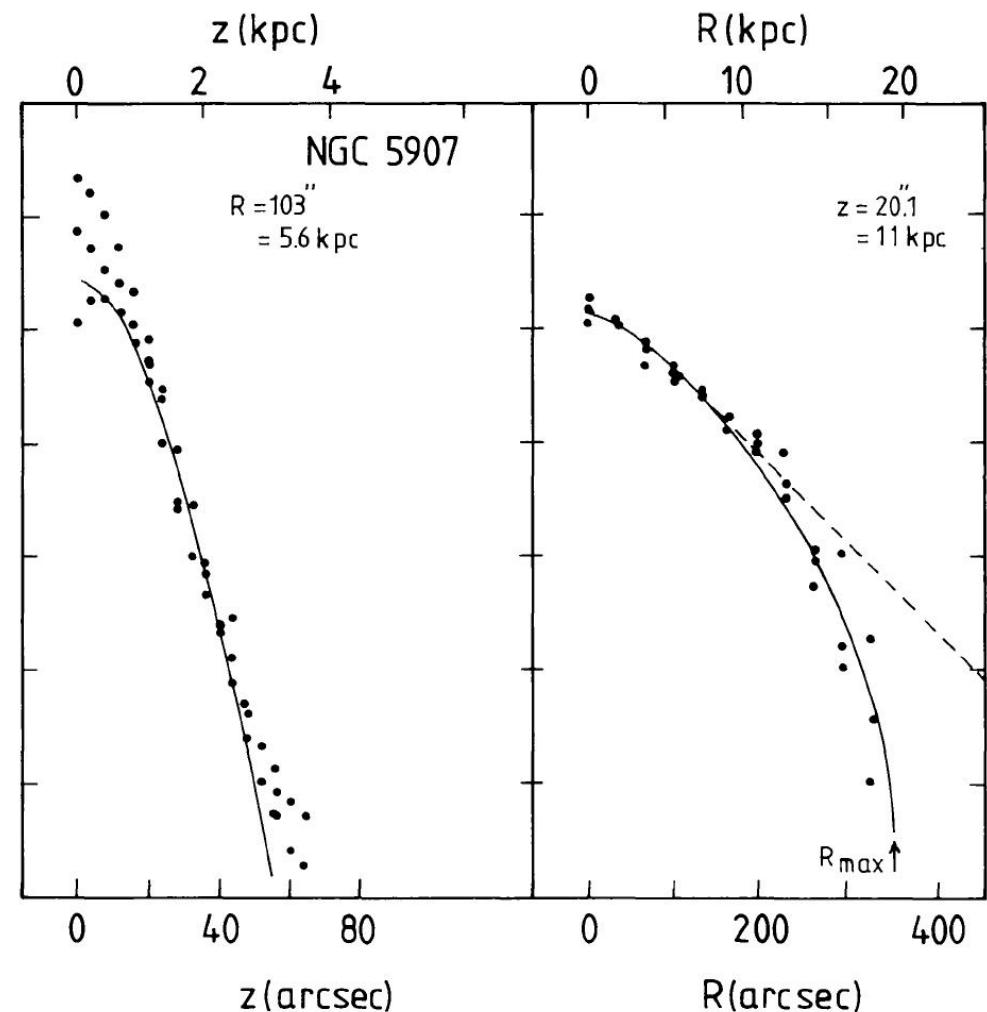
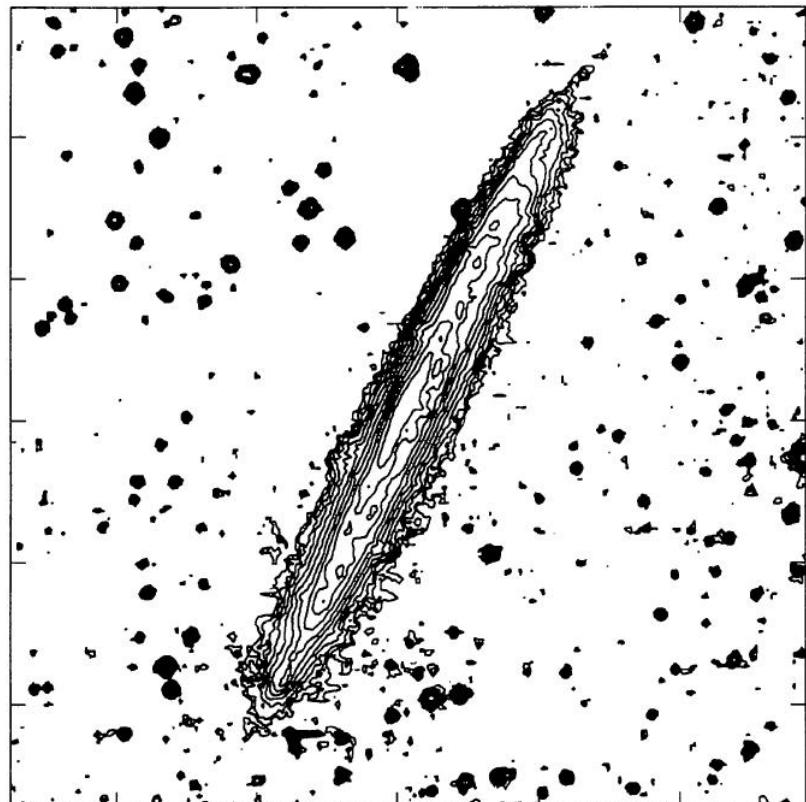
where

$$\rho_0(R) = \begin{cases} \rho_{00} e^{-R/R_d} & (R \leq R_t) \\ \rho_{00} e^{-R/R_d} [1 - (R - R_t)/\delta] & (R_t \leq R \leq R_t + \delta) \\ 0 & (R_t + \delta \leq R) \end{cases}$$

R_t = truncation radius, δ = soft-cutoff region

note: $\operatorname{sech}(x) = \cosh(x)^{-1}$

e.g. NGC5907 (van der Kruit & Searle 1982):



bulge: intensity follows de Vaucouleurs (1948) law

$$I(R) = I_e \cdot e^{-7.67 \left[(R/R_e)^{1/4} - 1 \right]}$$

or, its generalized form, a Sersic law

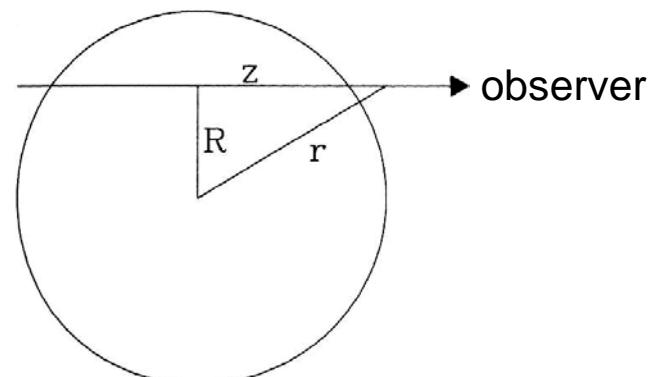
$$I(R) = I_e \cdot e^{-b_n \left[(R/R_e)^{1/n} - 1 \right]}$$



where R_e is the effective radius, implying that one-half of the total light is emitted interior to R_e .

Intensity distribution of a spheroid needs to be deprojected (Binney & Tremaine 1987; Binney & Merrifield 1998):

$$I(R) = \int_{-\infty}^{+\infty} j(r) dz = 2 \int_R^{+\infty} \frac{j(r) r dr}{\sqrt{r^2 - R^2}}$$



this Abel integral is readily inverted to yield the luminosity density

$$j(r) = -\frac{1}{\pi} \int_r^{+\infty} \frac{dI}{dR} \frac{dR}{\sqrt{R^2 - r^2}}$$

convert luminosity density into matter density of bulge

$$\rho_x(r) = K_x \cdot j_x(r)$$

and calculate circular velocity using Poisson equation for the spherically symmetric case (see kinematics).

gaseous disks:

e.g. Leroy et al. (2008):

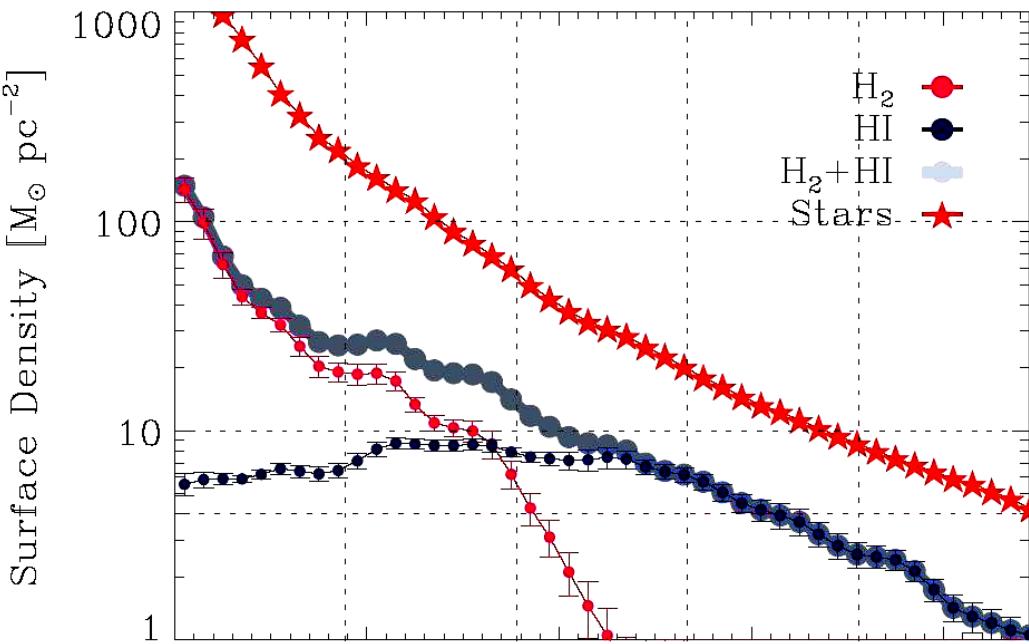
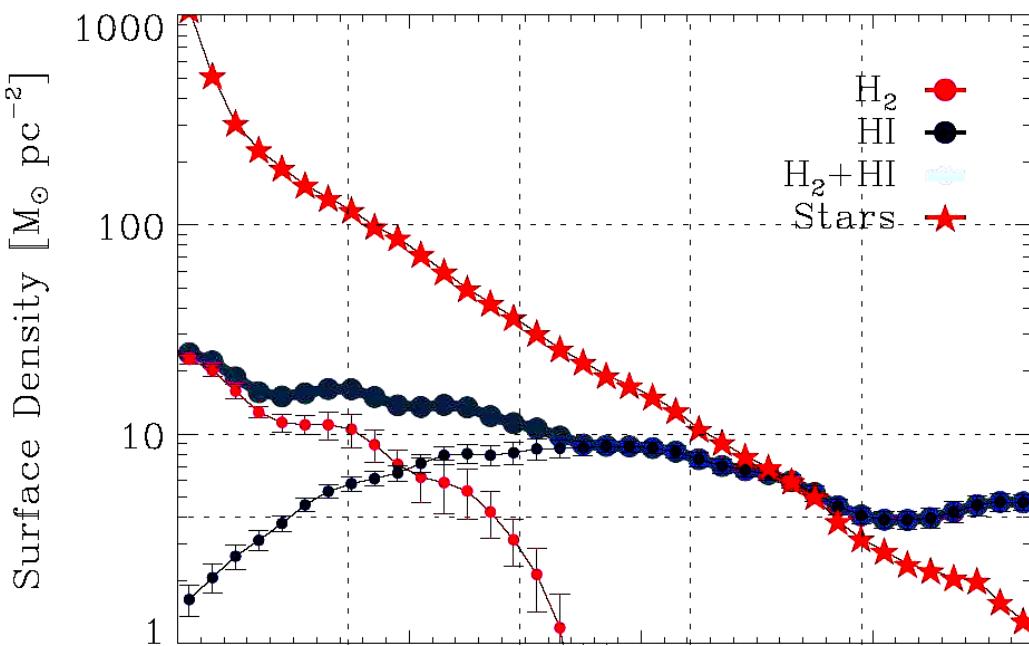
total gas and SFE from

- HI (THINGS)
34 galaxies, 6" resolution
- CO (BIMA SONG)
44 galaxies, 44" resolution

distribution of molecular gas:

inferred H_2 leads to nearly exponential decline

fills the HI gaps in the centres



Atomic gas

neutral hydrogen

formation: in the first 3 minutes ... (BBNS)

21 cm line radiation of neutral hydrogen at frequency

$$\nu_{I0} = 1.42040575178(6) \text{ GHz}$$

hyperfine transition, interaction of electron and nuclear spin magnetic dipole radiation with

$$A_{I0} = 2.86888 \cdot 10^{-15} \text{ s}^{-1}$$

column densities easily derived via

$$N_{HI}(\xi, \eta) = 1.822 \cdot 10^{18} \int_{V_1}^{V_2} \left[\frac{T_b(\xi, \eta)}{K} \right] \left(\frac{dV}{km \text{ s}^{-1}} \right) \text{ atoms cm}^{-2}$$

NGC 5457 (M 101)

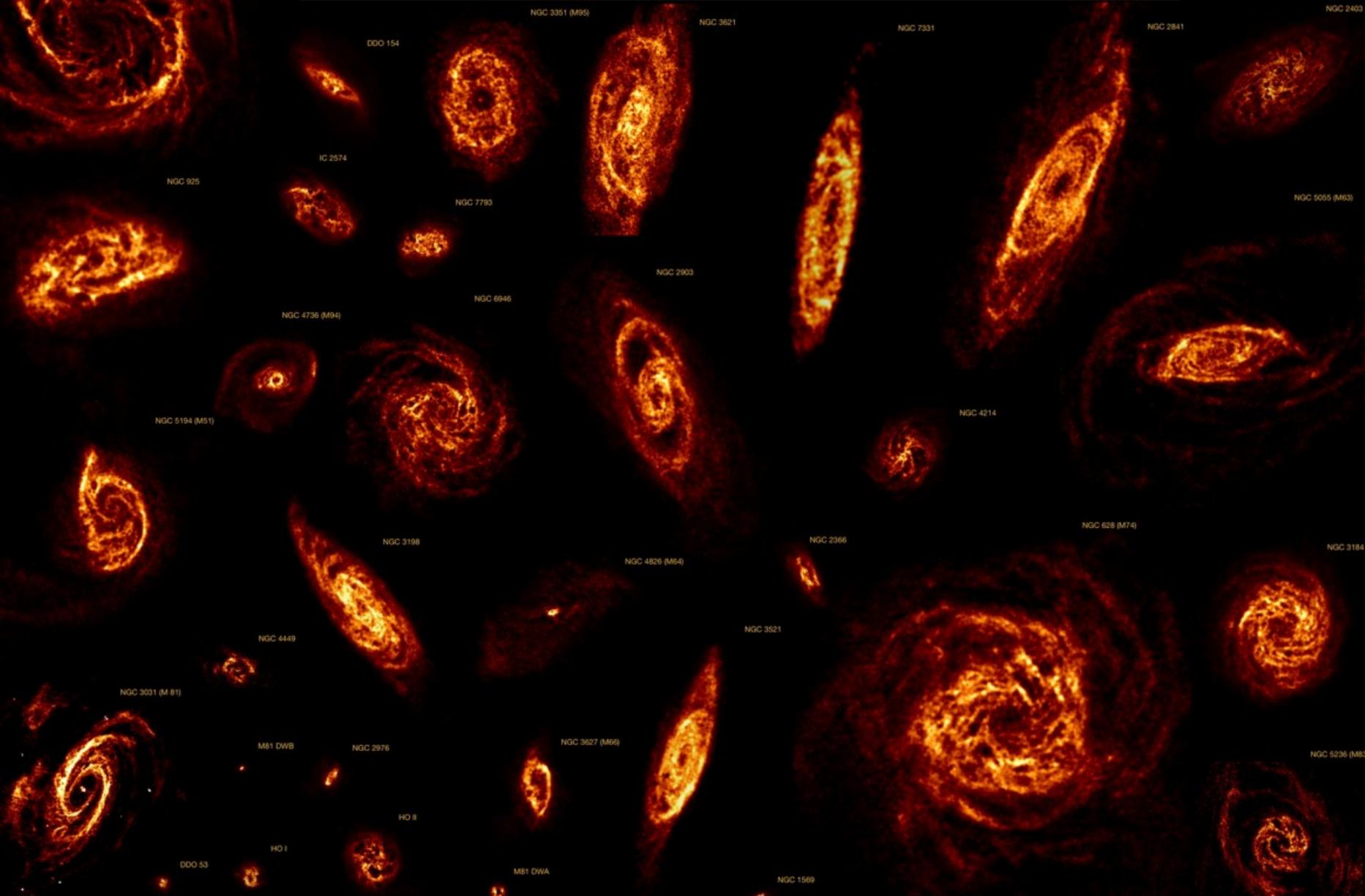


The *H*I Nearby Galaxy Survey (THINGS)



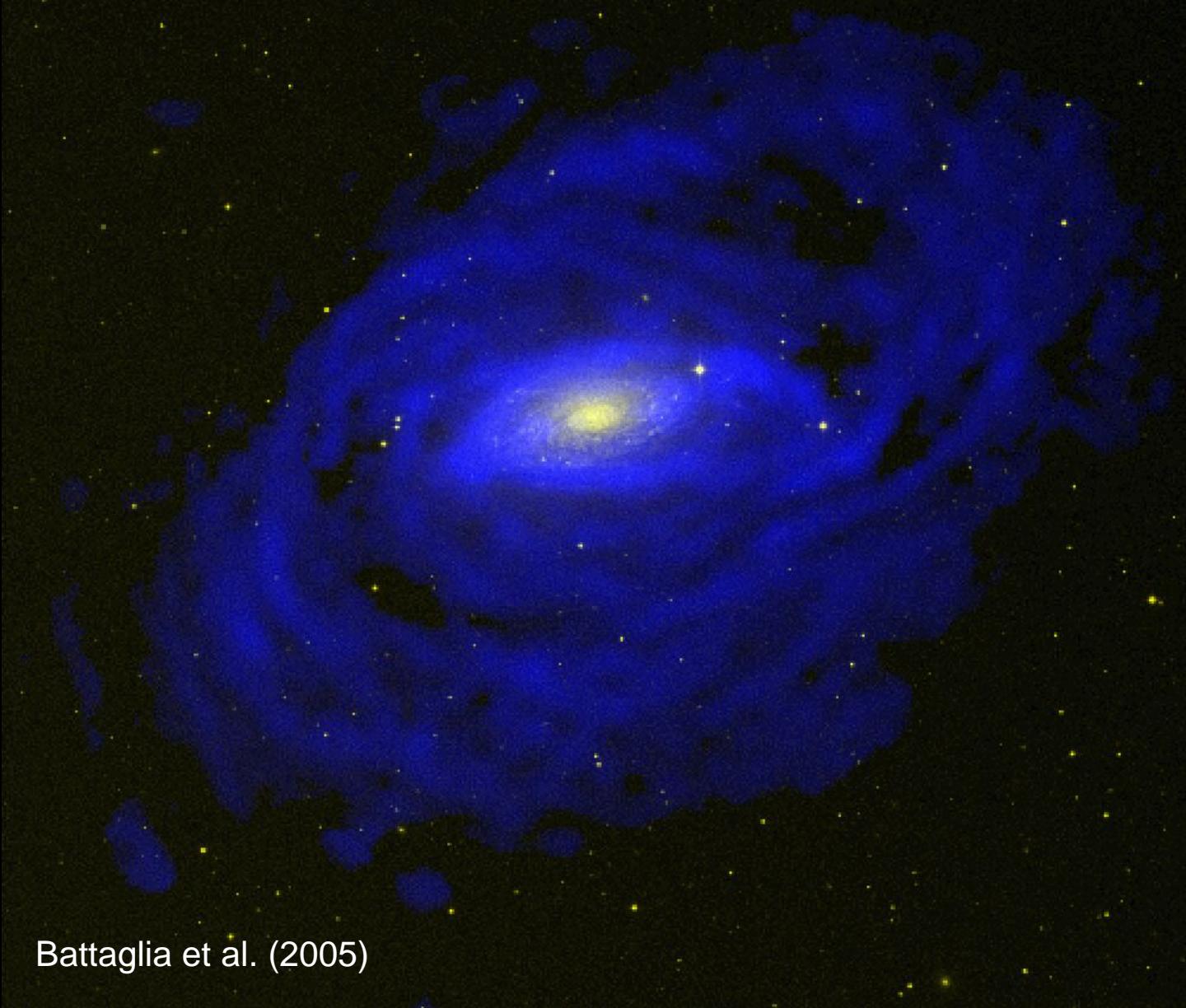
NGC 3077

F. Walter, E. Brinks, E. de Blok, F. Bigiel, M. Thornley, R. Kennicutt



in general: HI disks much larger than stellar ones!

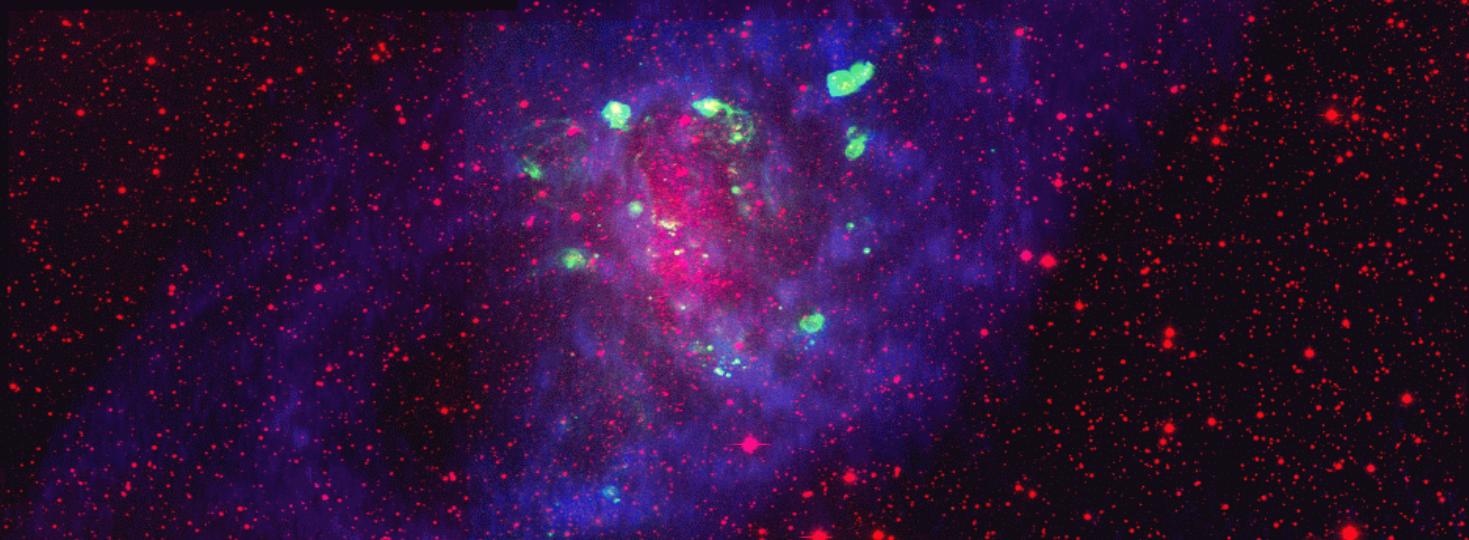
e.g. NGC 5055



Battaglia et al. (2005)

19 July 2011

de Blok & Walter (2003)

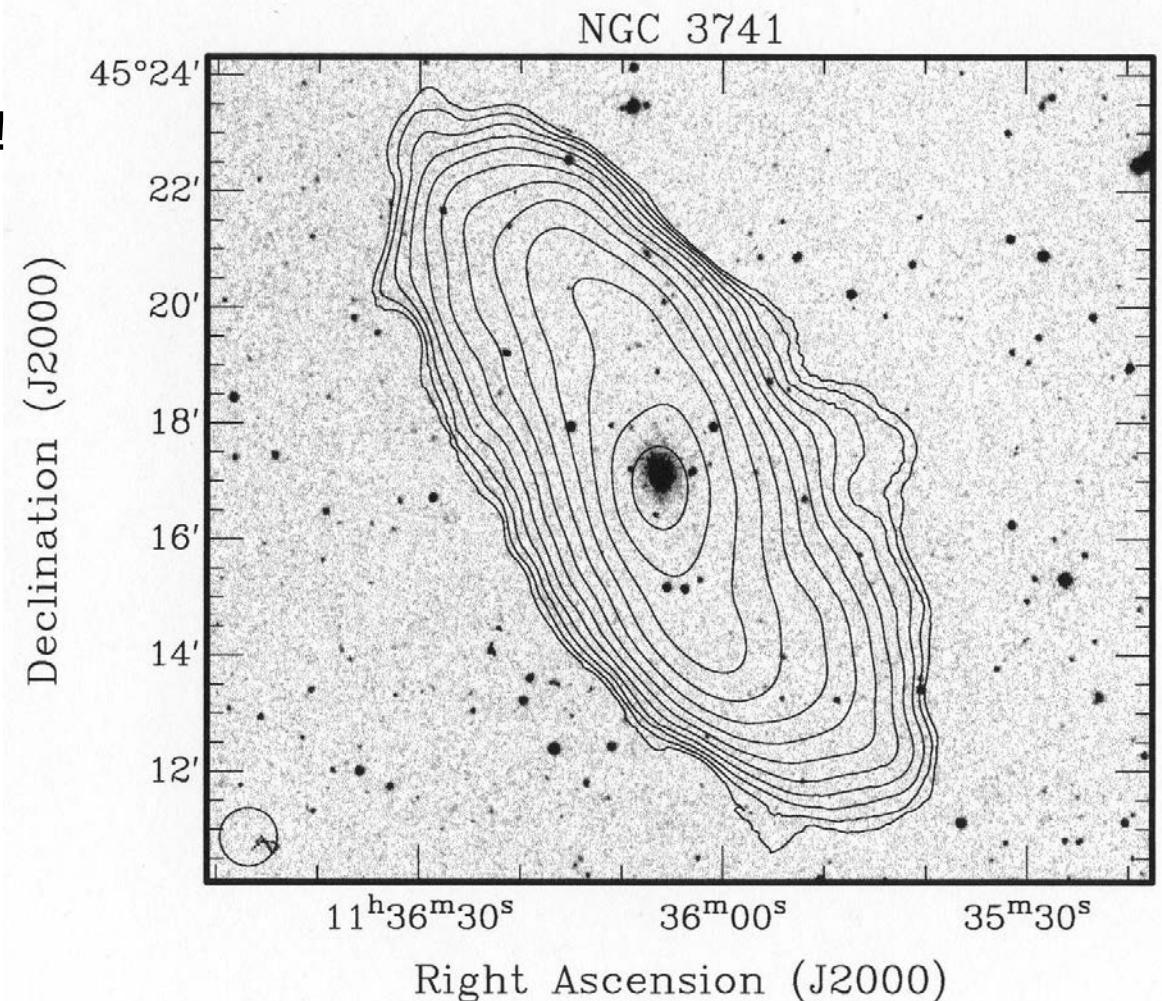


NGC 6822
de Blok & Walter
R-band *HI* *H α*

... and another one: NGC 3741 (Gentile et al. 2007):

WSRT observations; $15'' \times 12''$ beam $\Rightarrow 220 \text{ pc} \times 170 \text{ pc}$

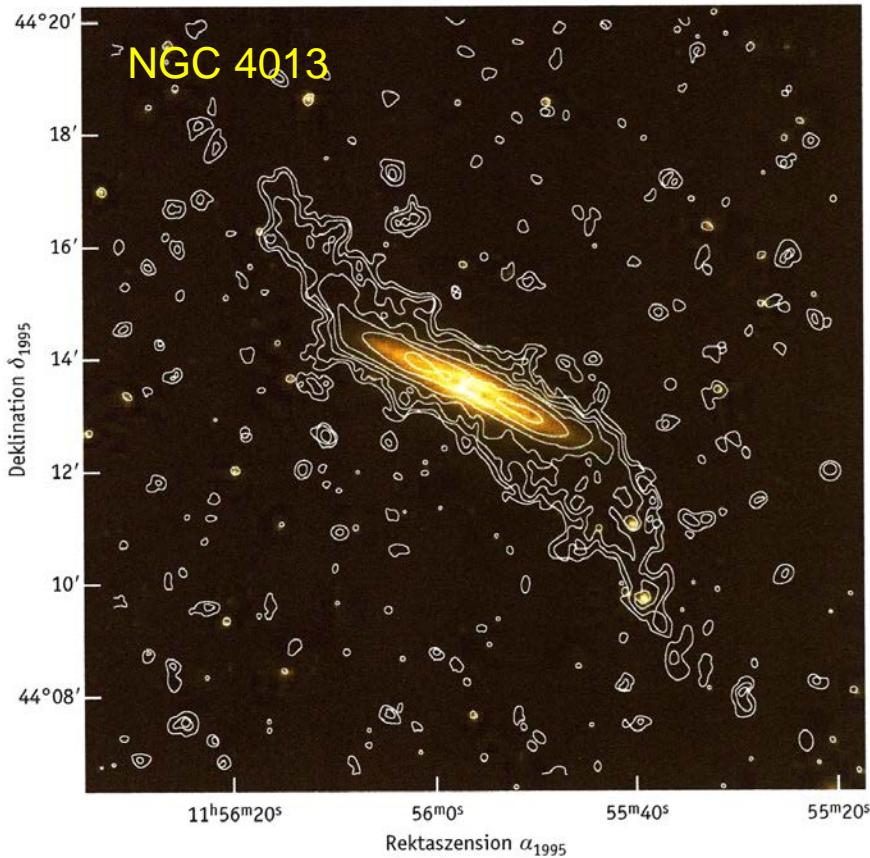
- largest HI disk so far
- out to $\sim 15 \times R_{25}$,
= 42 B-band scale-lengths!



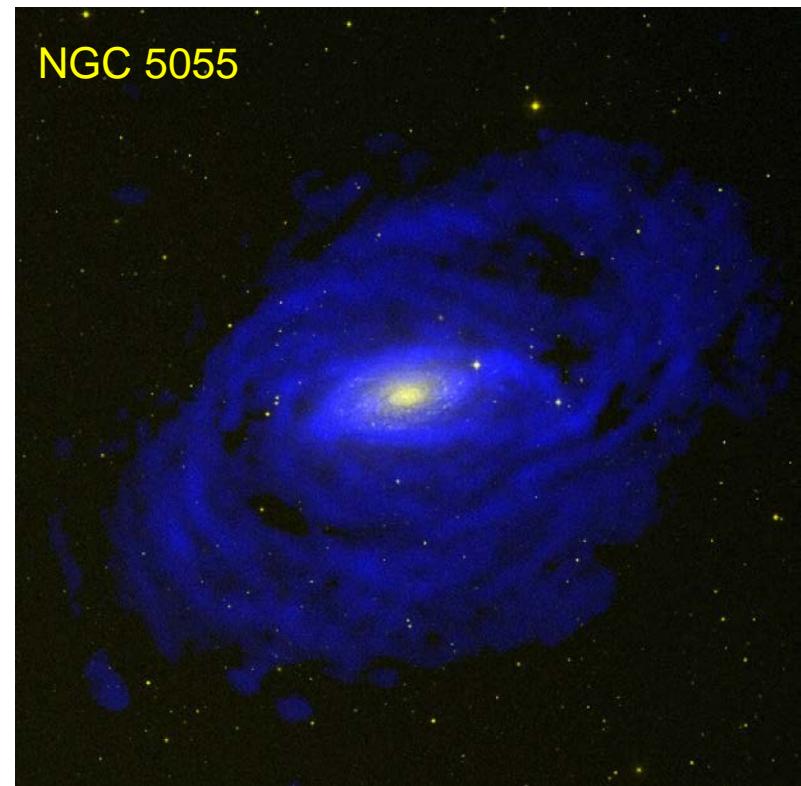
warps:

- most pronounced in HI line
- first seen in edge-on systems (Sancisi 1976; 1983)

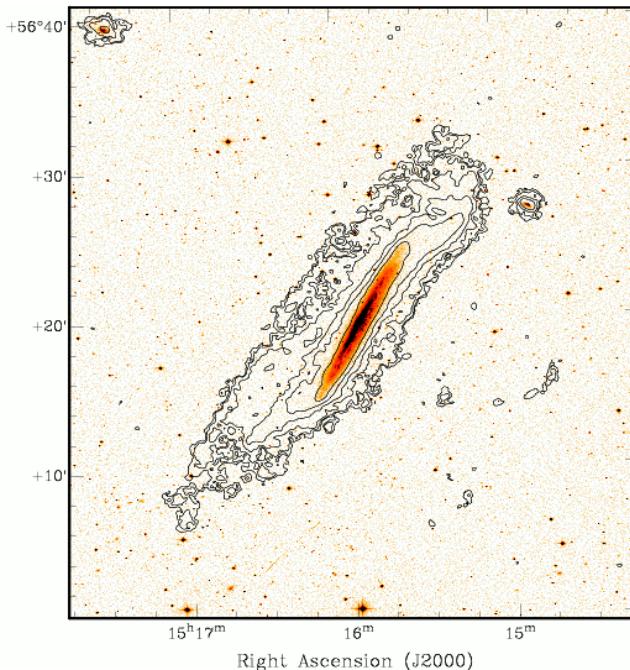
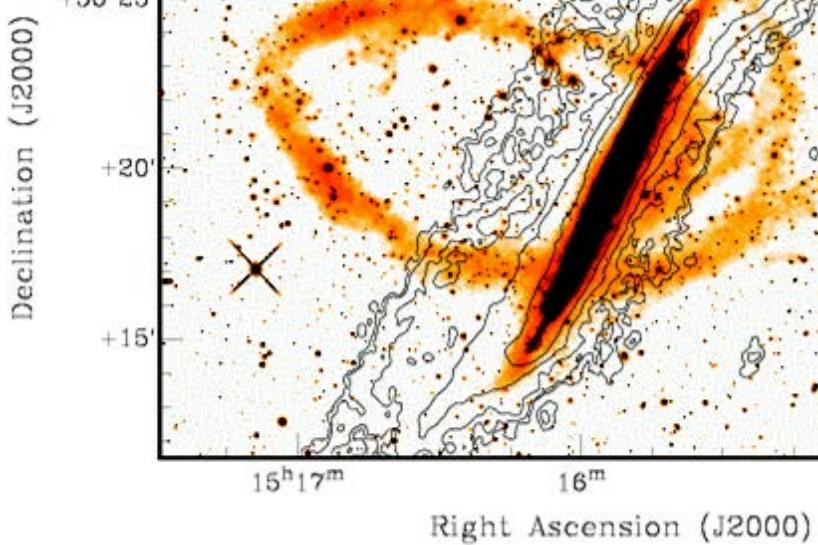
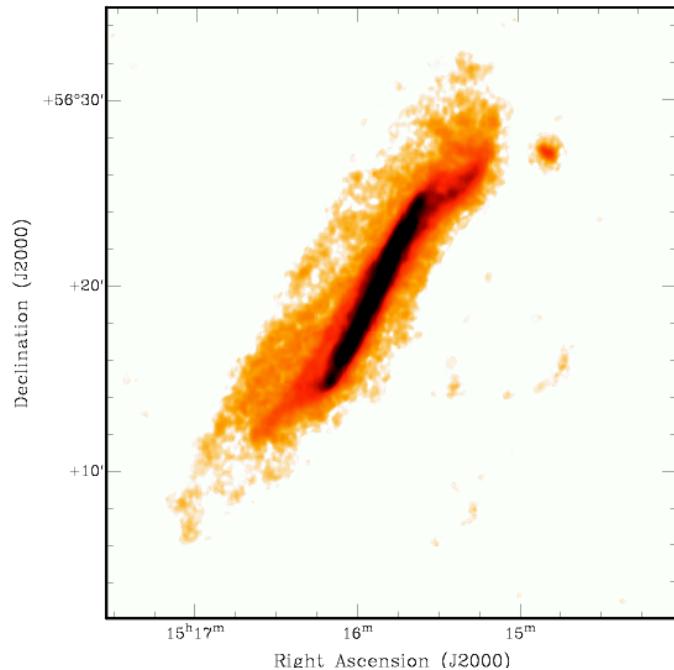
cause: external or internal torques



Bottema et al. (1996)



Battaglia et al. (2006)



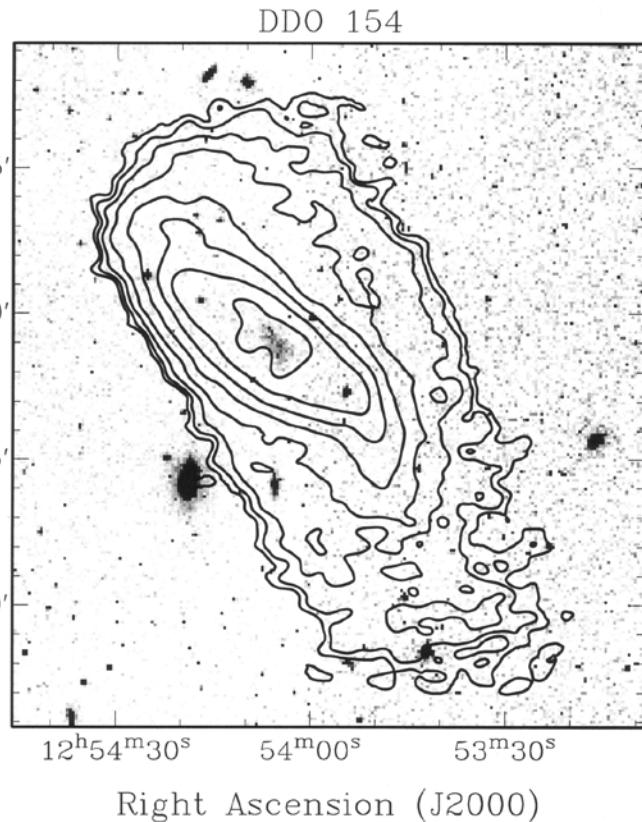
NGC 5907

Józsa et al., in prep.

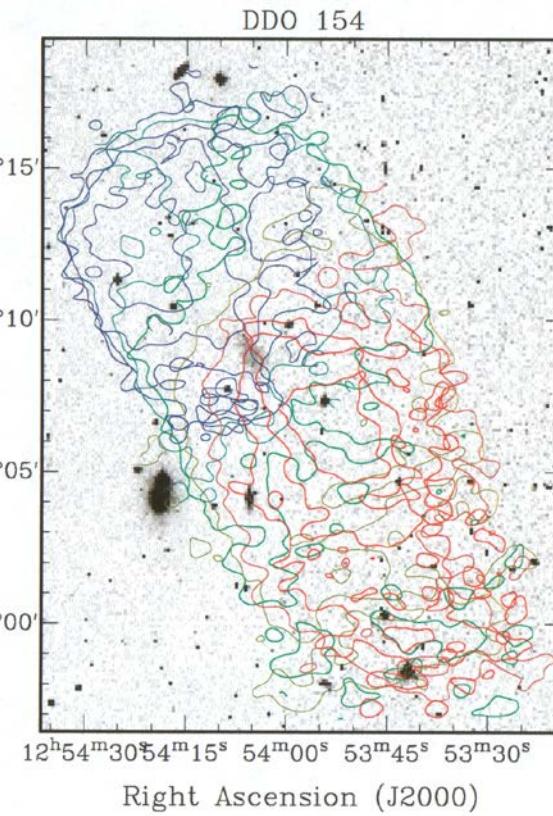
Ringberg, 19 July 2011

DDO 154: HI out to $\sim 15 \times R_{25}$ (B band)

Declination (J2000)



Declination (J2000)



Gentile et al. (in prep.)

Ringberg, 19 July 2011

DDO 154: the 3-D gaseous structure (?)

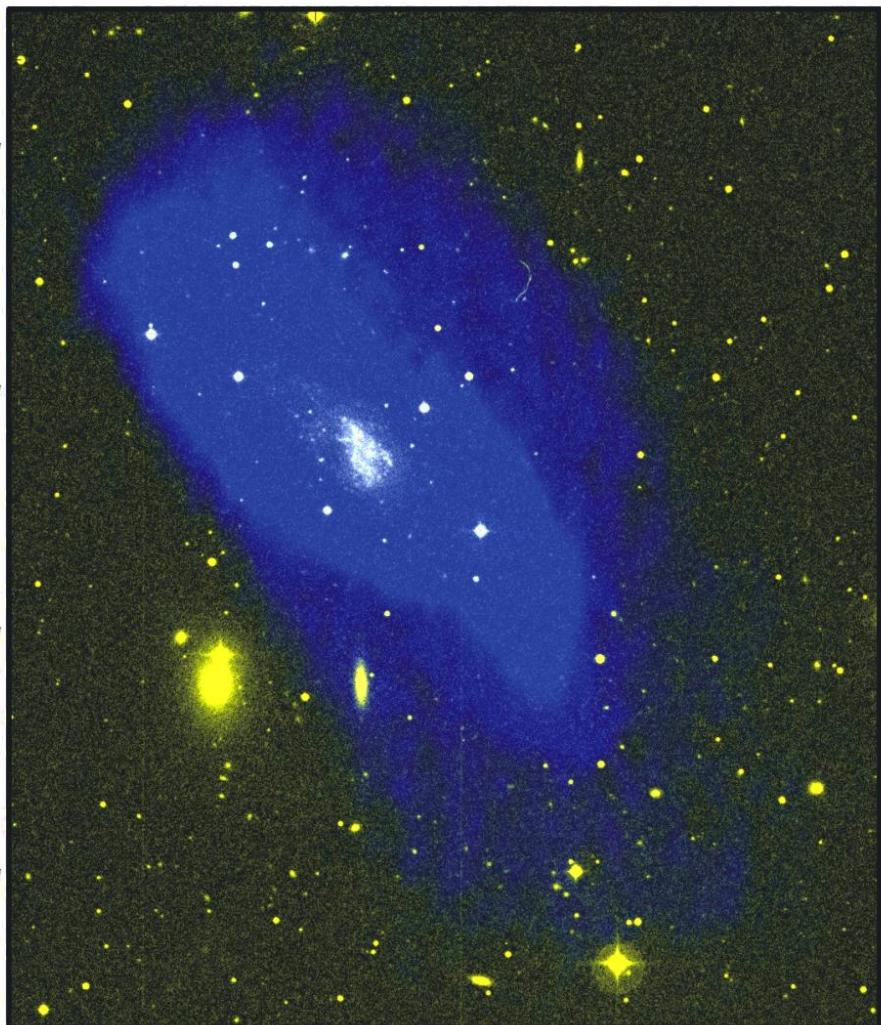
Declination (J2000)

27°15'

27°10'

27°05'

27°00'



12^h54^m30^s 54^m15^s 54^m00^s 53^m45^s 53^m30^s

Right Ascension (J2000)



Józsa et al. (in prep.)

Ringberg, 19 July 2011

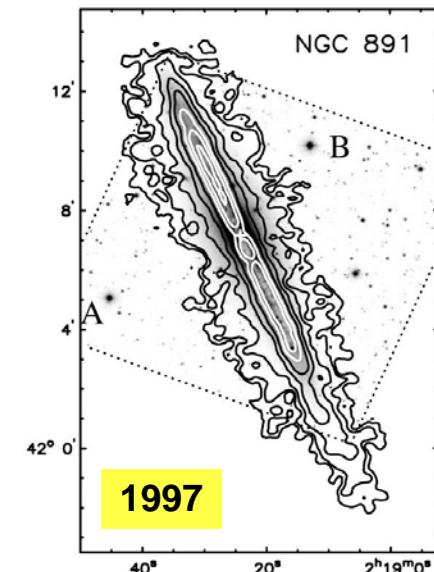
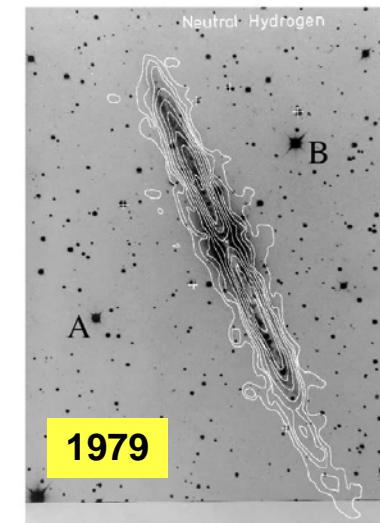
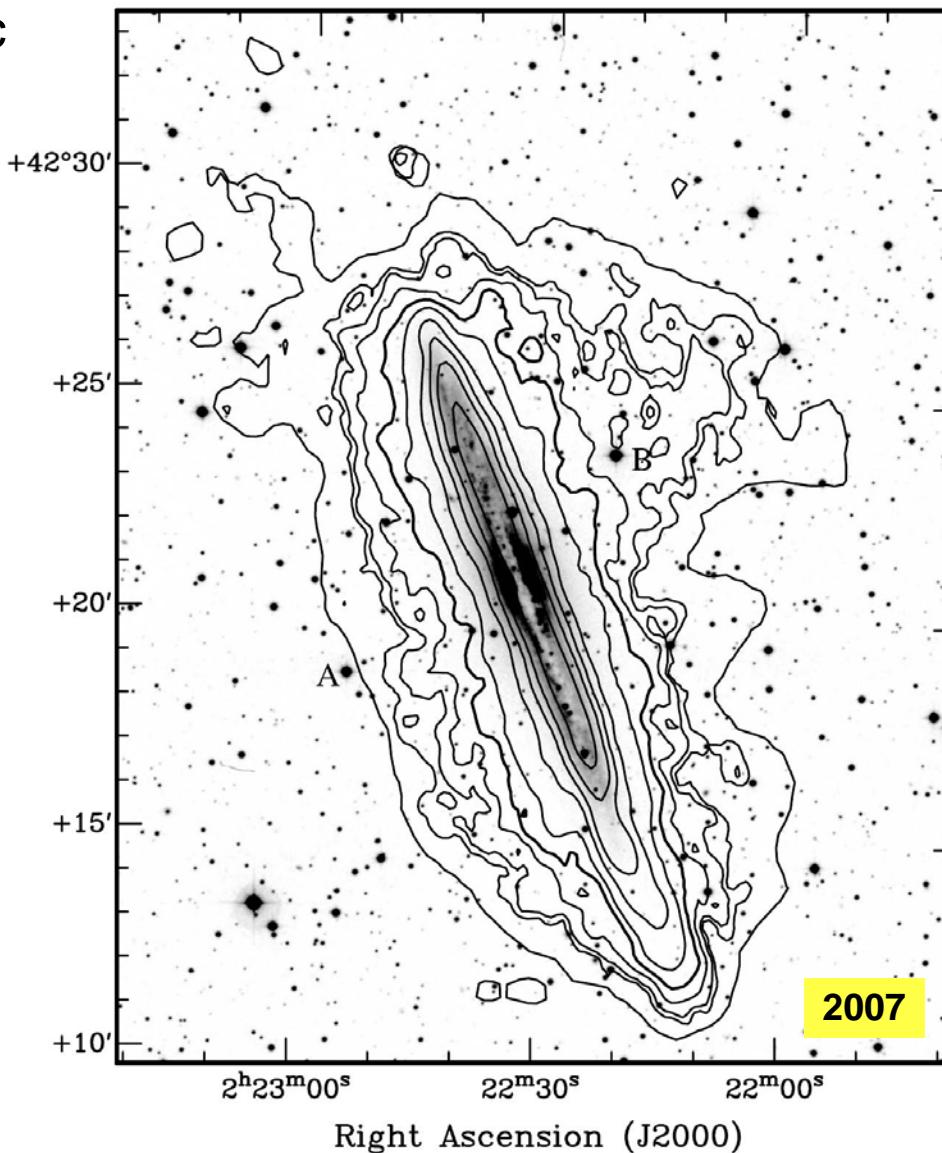
cold halo gas: e.g. NGC 891, a matter of sensitivity ...

Oosterloo et al. (2007)

H I out to $z = 22$ kpc

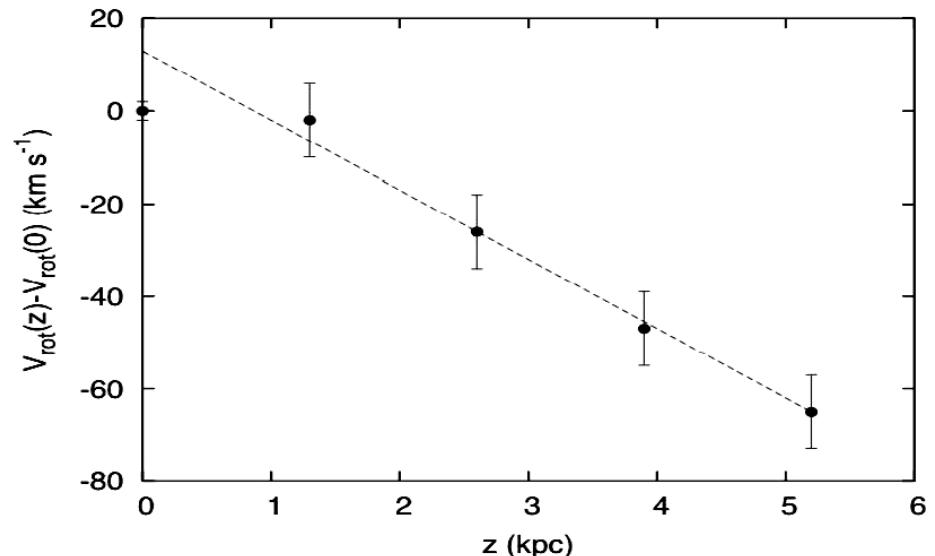
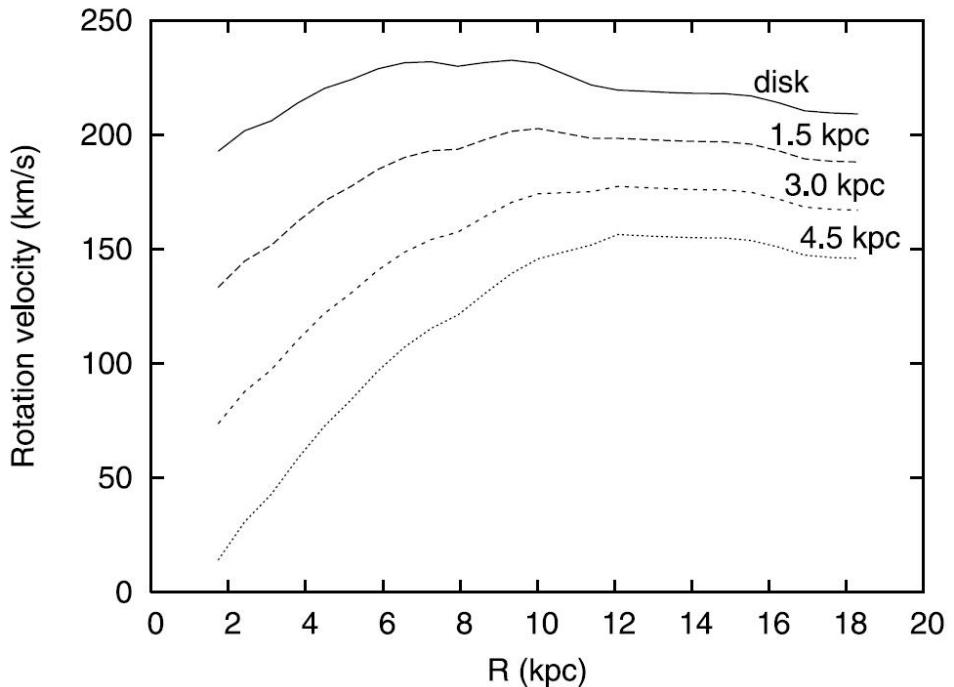
$$M_{HI} = 1.2 \cdot 10^9 M_{\odot}$$

$\approx 30\%$ of total H I!



rotation of halo gas:

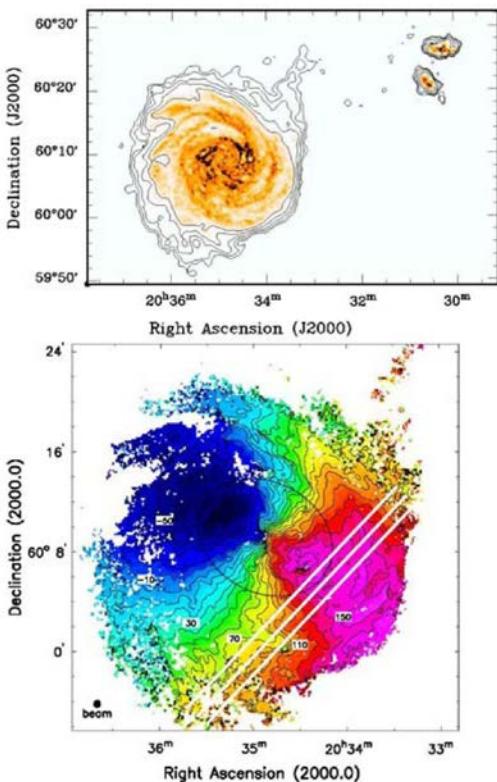
$$dV_z/dz = 15 \text{ km s}^{-1} \text{ kpc}^{-1}$$



further support for accretion scenario: HI with anomalous velocities

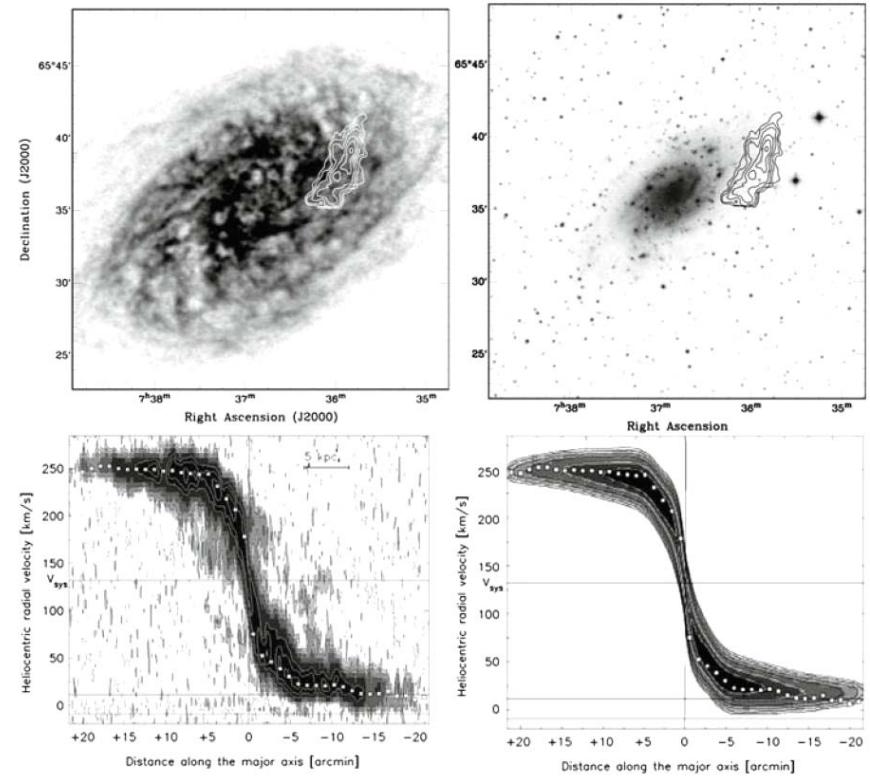
NGC 6946

Boomsma (2007)



NGC 2403

Fraternali et al. (2002)



holes and shells in the ISM

Bagetakos et al. (2010):

- found > 1000 holes (*THINGS*)

$$\emptyset = 100 \dots 1000 \text{ pc}$$

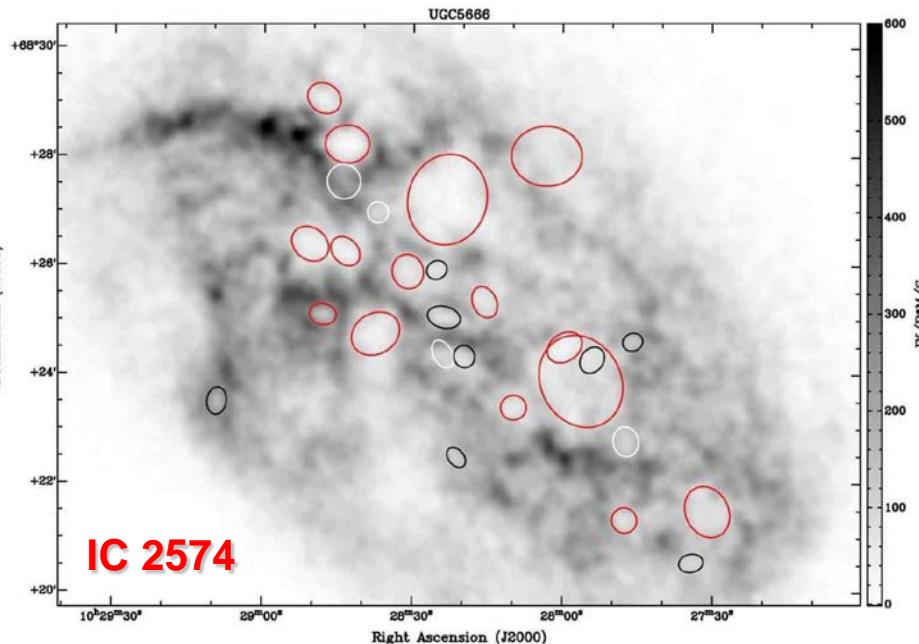
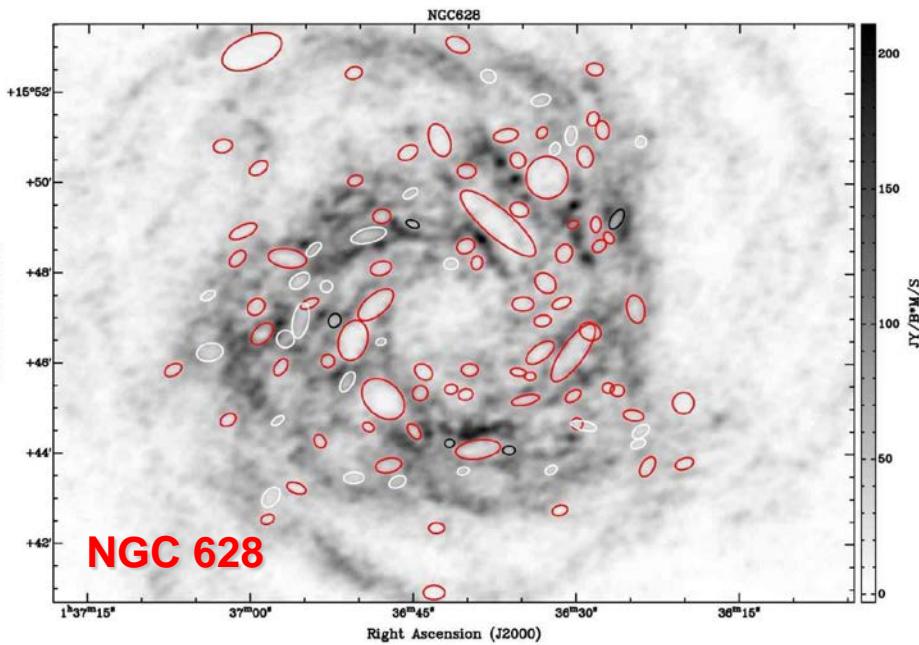
$$v_{\text{exp}} = 4 \dots 34 \text{ km s}^{-1}$$

$$\tau_{\text{kin}} = 3 \dots 150 \text{ Myr}$$

- larger and round holes in dwarfs

origin:

- star formation
- turbulence (Dib & Burkert 2005)



influence of environment:

HI Atlas of VIVA Sample

VLA Imaging of Virgo galaxies in Atomic gas

extended H I tails, almost all pointing away from the cluster center

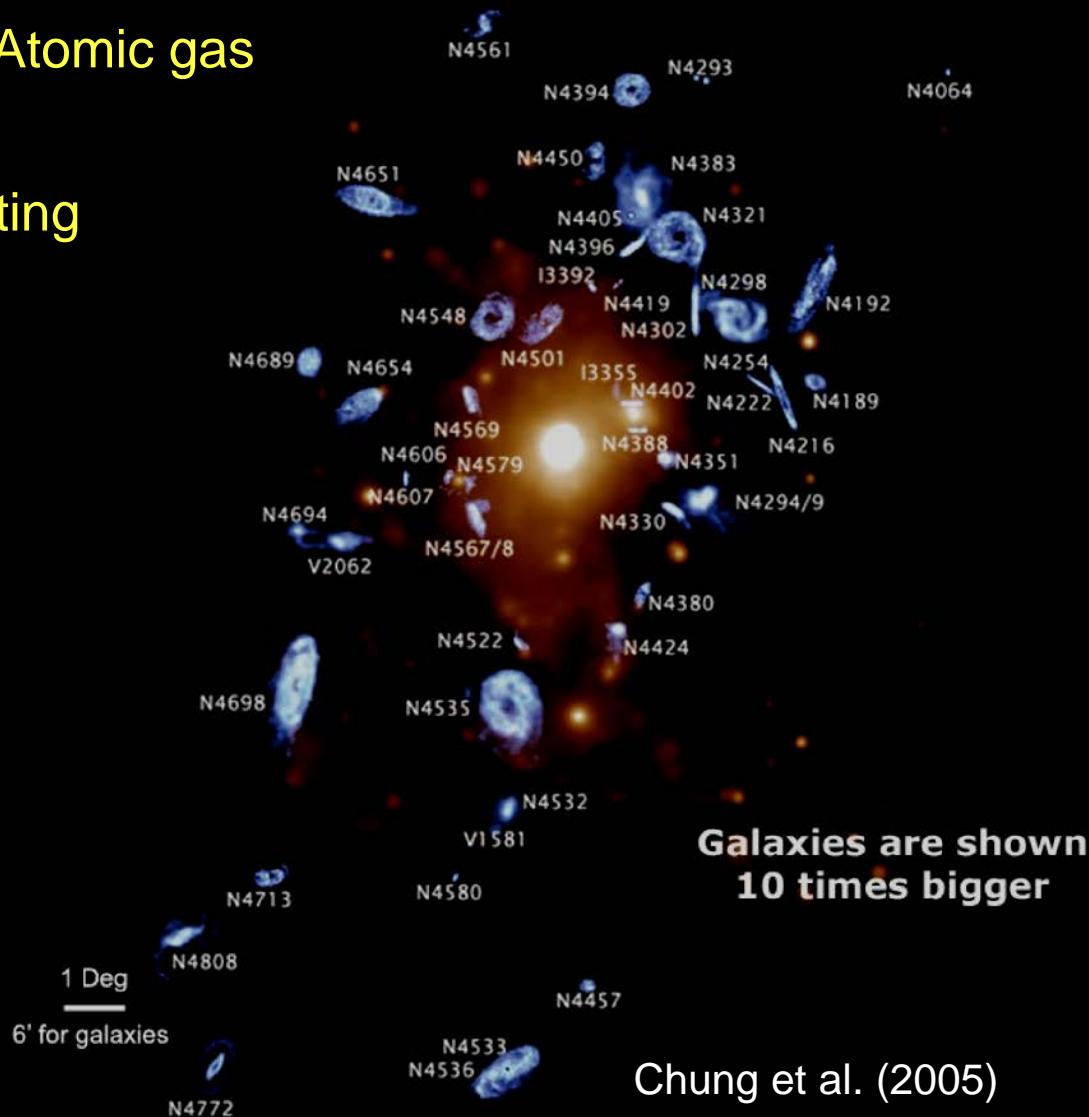
truncated H I disks

near cluster center compression
gas on one side

some of the HI extra-planar

variety of environmental effects:

- ICM-ISM interactions
- harassment
- tidal interactions
- mergers



Chung et al. (2005)

molecular gas:

most abundant: H_2 molecule

determination of N_{H_2} much more difficult than N_{HI}

lacks dipole moment

→ quadrupole transitions with $\Delta J = 2$ ($J = 2 \rightarrow 0$)

requires high gas temperatures ($\Delta E / k = 509$ K)

→ not representative for general ISM (only hot molecular gas)

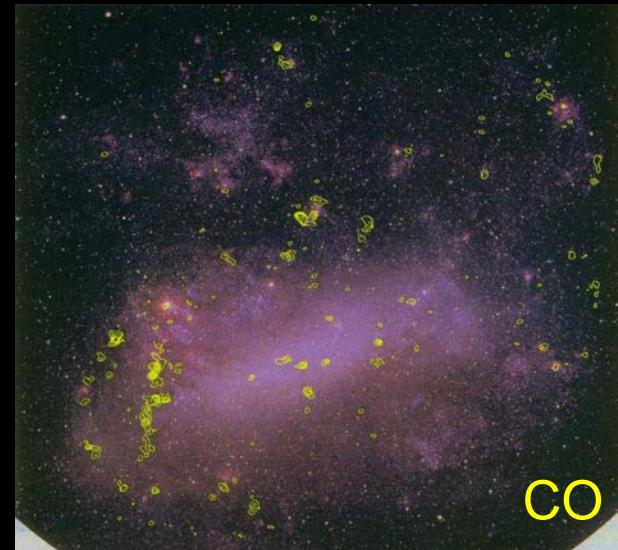
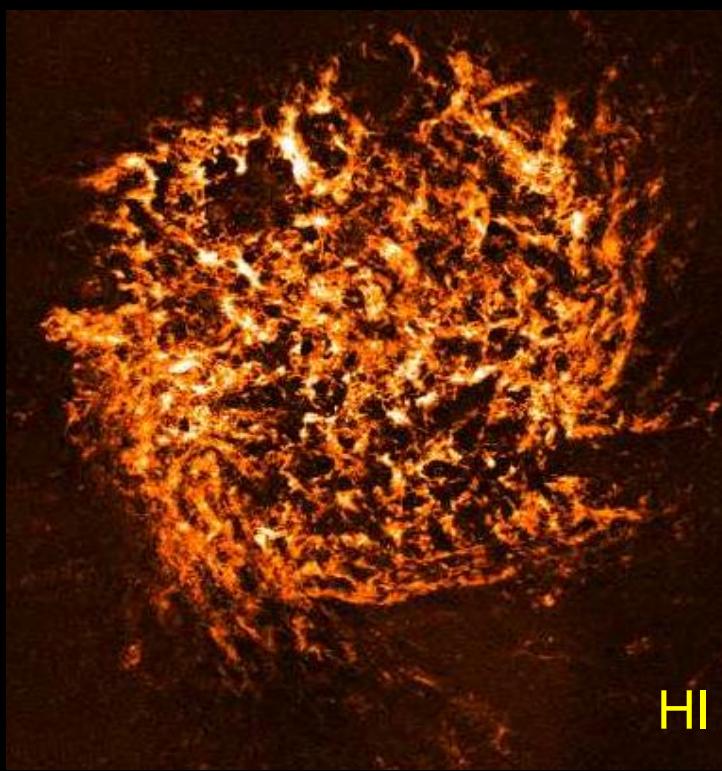
CO molecule:

second-most abundant molecule

frequent collisions with $\text{H}_2 \rightarrow$ information about H_2 (column) density

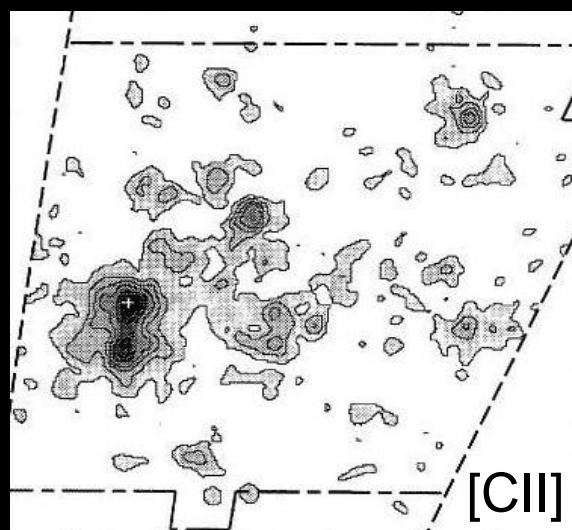
quite stable: $E_{diss} = 11.09$ eV $\Rightarrow \lambda_{diss} \leq 1118$ Å

e.g. LMC:



HI

CO



[CII]



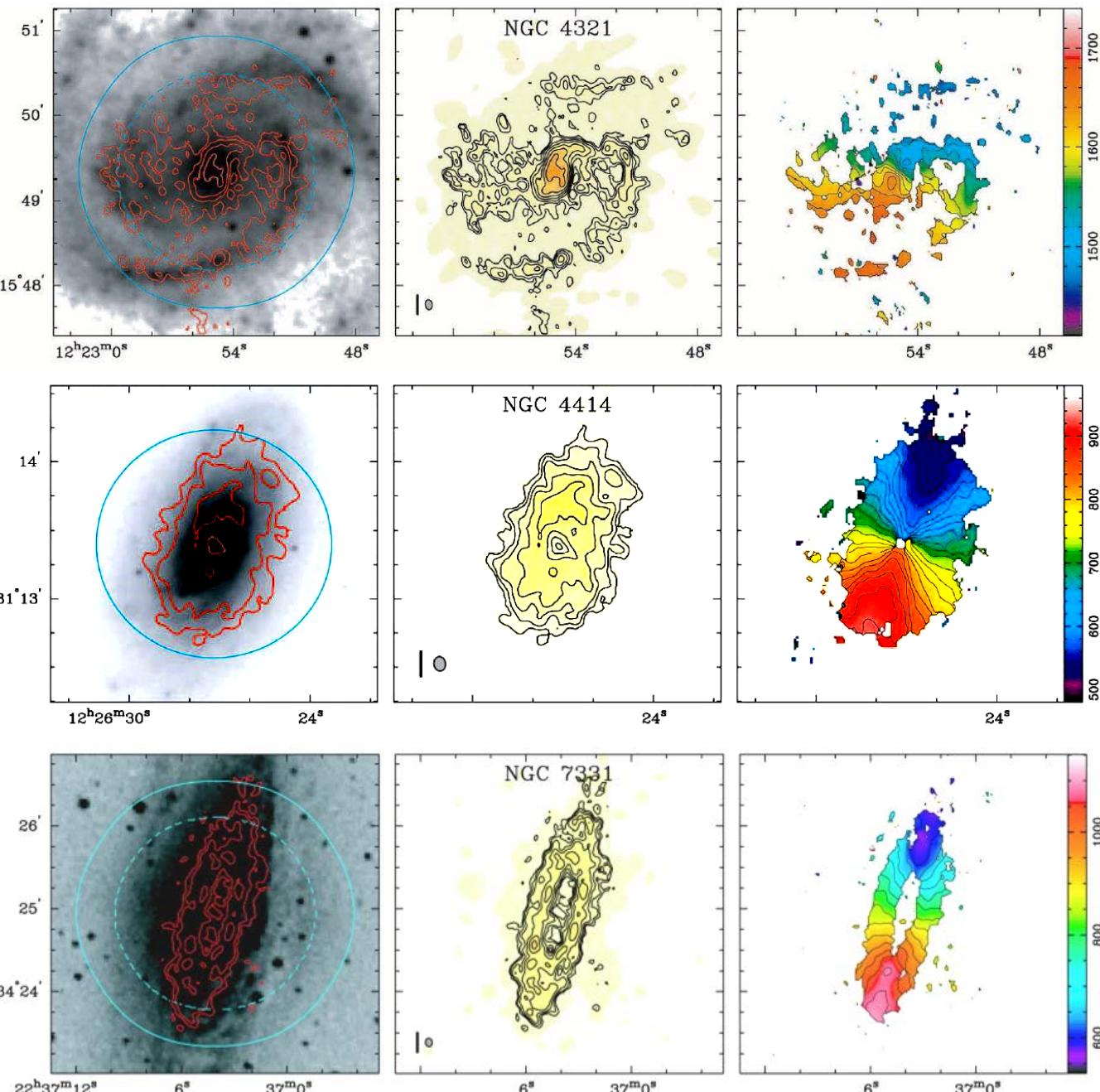
FIR

no CO for $\log(O/H) + 12 \leq 7.9$ (Taylor et al. 1998)

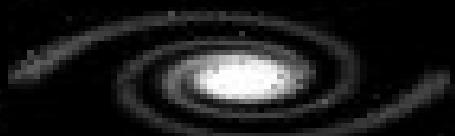
Ringberg, 19 July 2011

BIMA Survey of Nearby Galaxies (BIMA SONG)

Regan et al. (2001)
Helfer et al. (2003)



and finally the dark-matter halo:

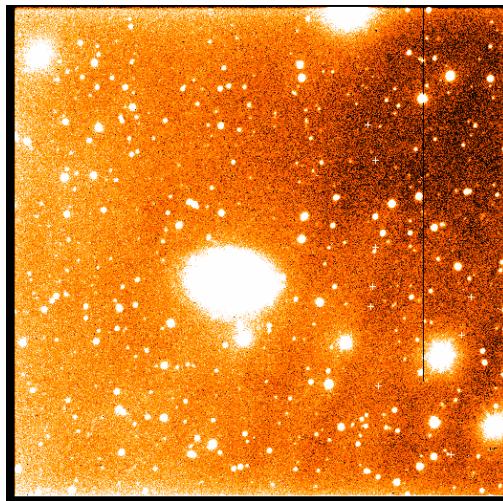


inferred from rotation curves (see kinematics)

Photometry

optical photometry \Rightarrow mass distribution of stellar component (bulge, disk)

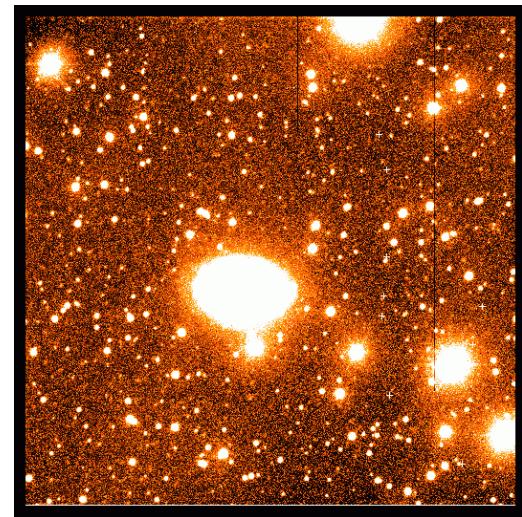
calibration is tricky, e.g. “flat-fielding”



raw image



: flat-field image



= flat-fielded image

then subtract stars and fit elliptical isophotes to galaxy image, with position angle χ and inclination i such as to obtain (projected) intensity distribution $I(R)$.

(from A. Pizzella's home page)

evaluation: e.g. profile fitting

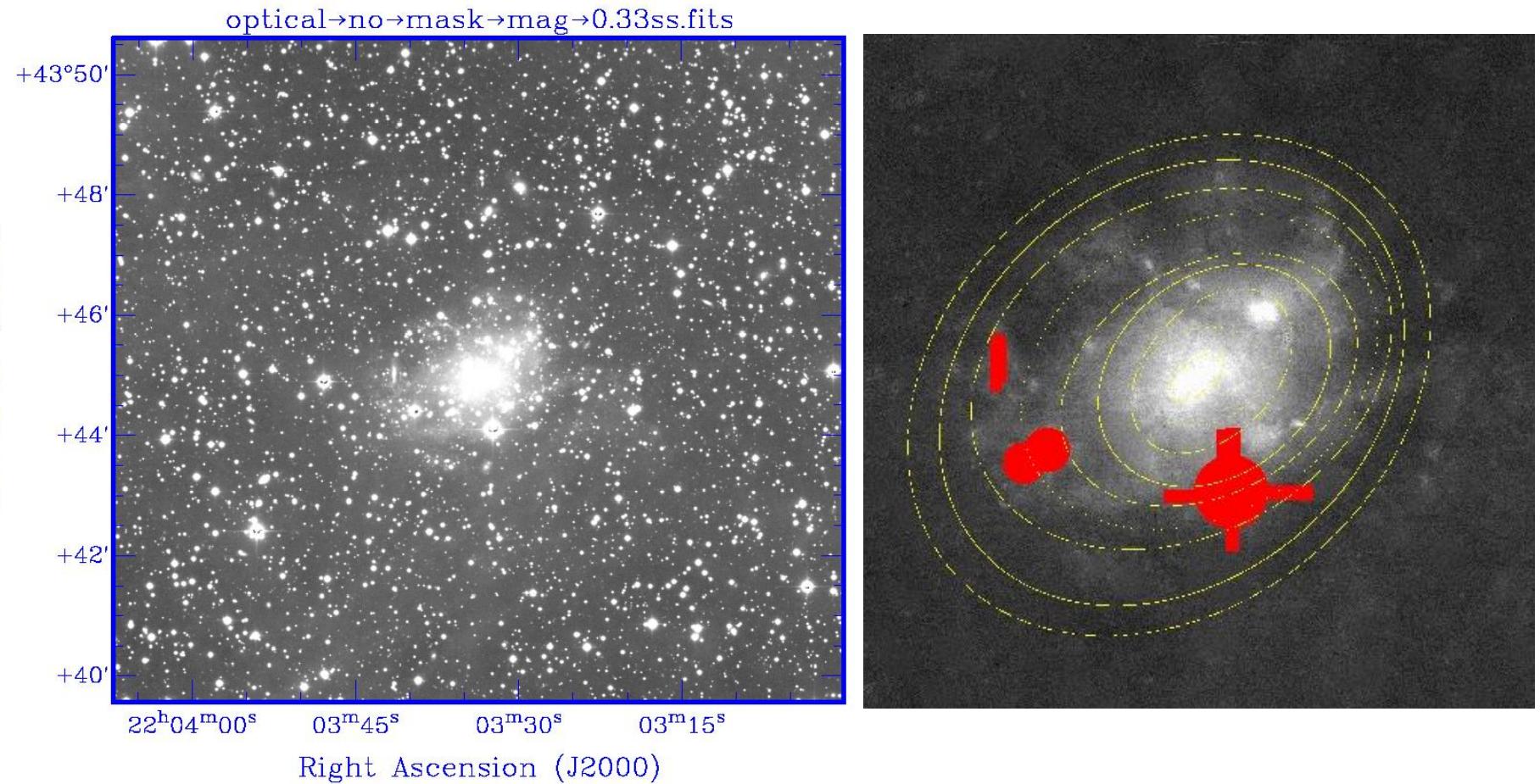
- one-dimensional: average brightness in elliptical rings and fit analytical function to it
- two-dimensional fit to the photometry

most widely used tool: GALFIT (Peng et al. 2002; 2007; 2010)

provides large set of radial fitting functions

accounts for PSF by convolving galaxy model functions with it

a weird thing: star subtraction!



... a real challenge: e.g. UGC 11891 (a 'smudge' close to the Galactic plane)

Sersic

$$I(R) = I_e \cdot e^{-b_n [(R/R_e)^{1/n} - 1]}$$

exponential

$$I(R) = I_0 \cdot e^{-R/R_d}$$

Nuker

$$I(R) = I_b \cdot 2^{(\beta-\gamma)/\alpha} \left(\frac{R}{R_b} \right)^{-\gamma} \left[1 + \left(\frac{R}{R_b} \right)^\alpha \right]^{(\gamma-\beta)/\alpha}$$

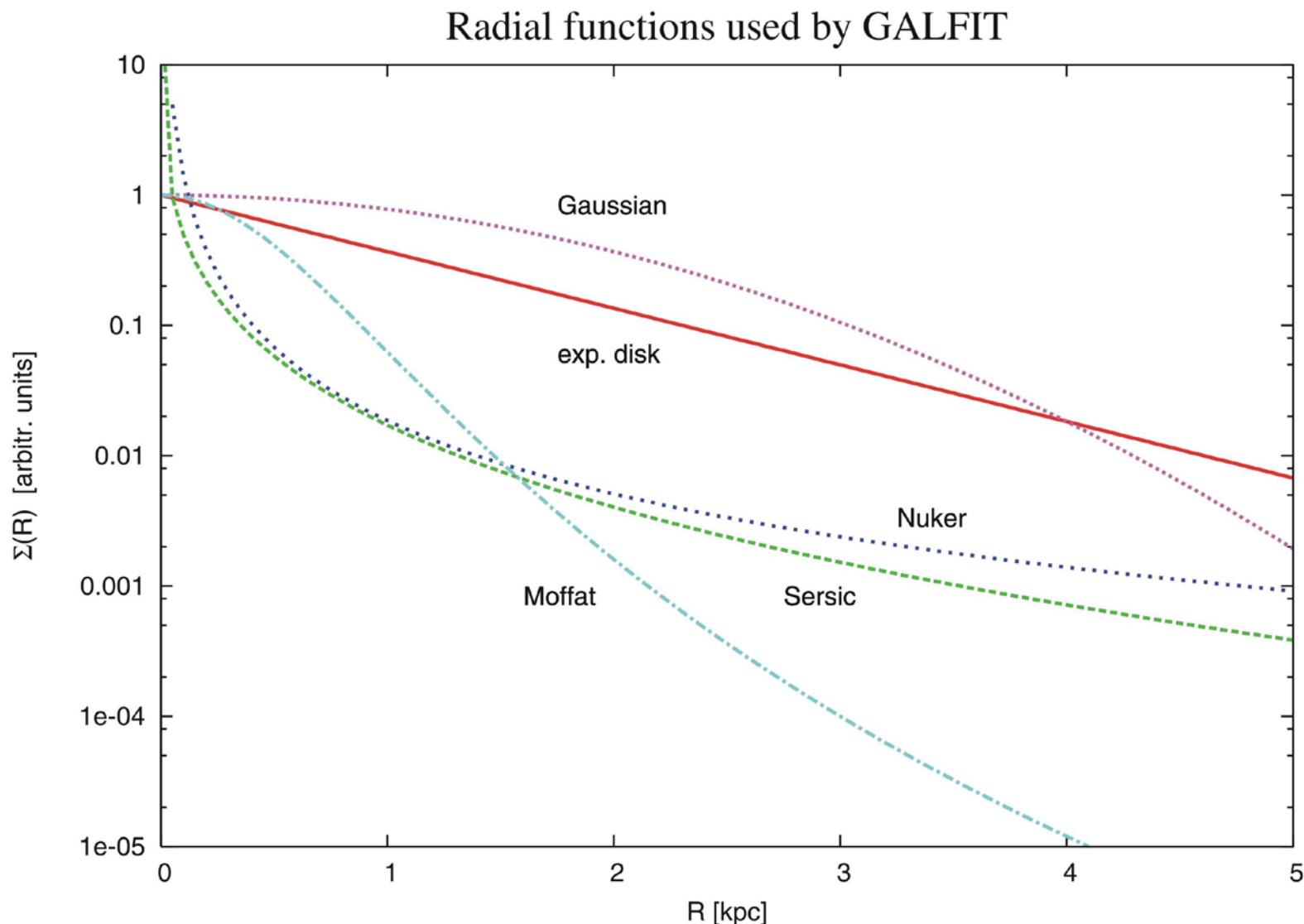
Gaussian

$$I(R) = I_0 \cdot e^{-\left(R^2/2\sigma^2\right)}$$

Moffat

$$I(R) = I_0 \cdot \left[1 + \left(R / R_d \right)^2 \right]^n$$

Graphical illustration of GALFIT functions



when principal axes of ellipse aligned with coordinate axes, the radial pixel coordinate given by

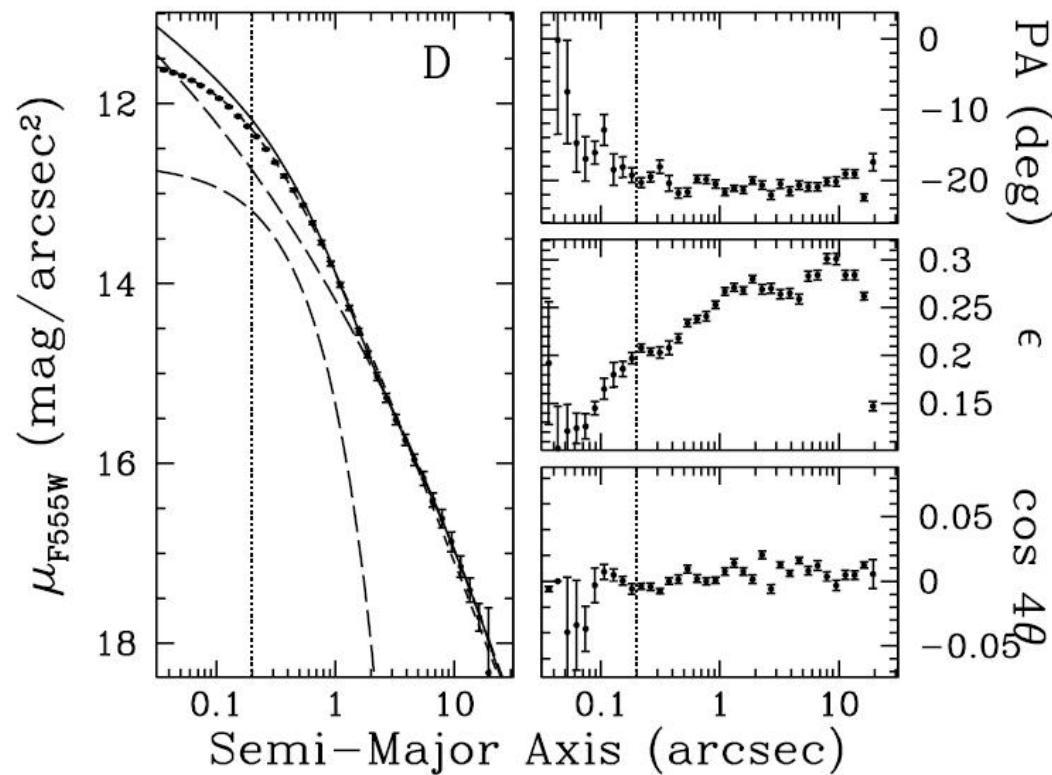
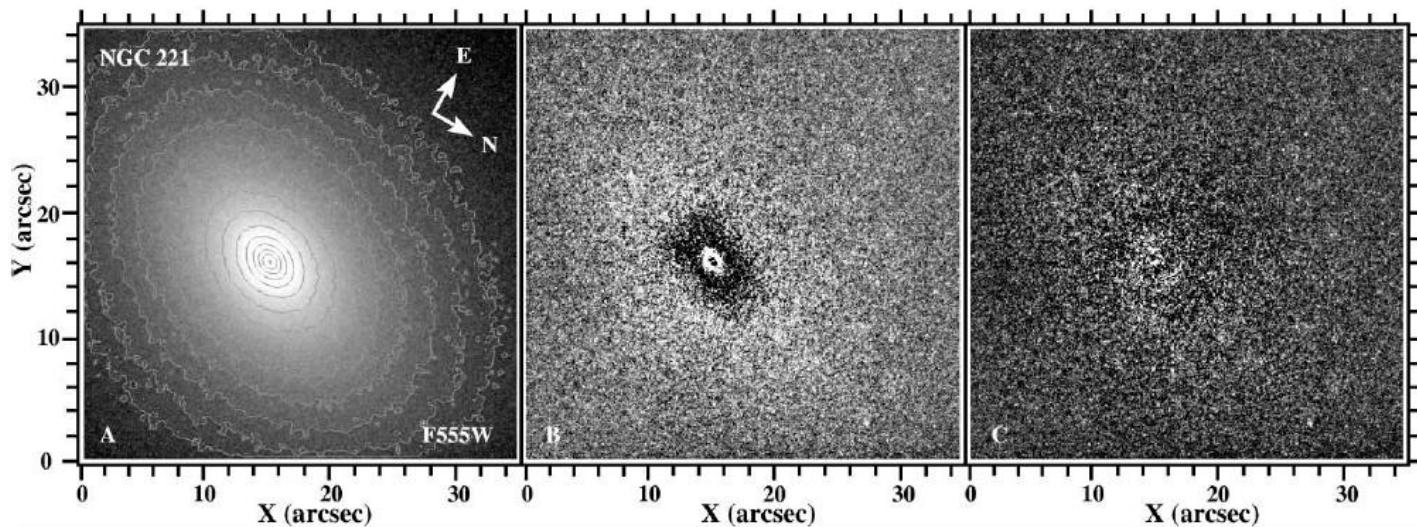
$$R = \left(|x|^{c+2} + \left| \frac{y}{q} \right|^{c+2} \right)^{\frac{1}{c+2}}$$

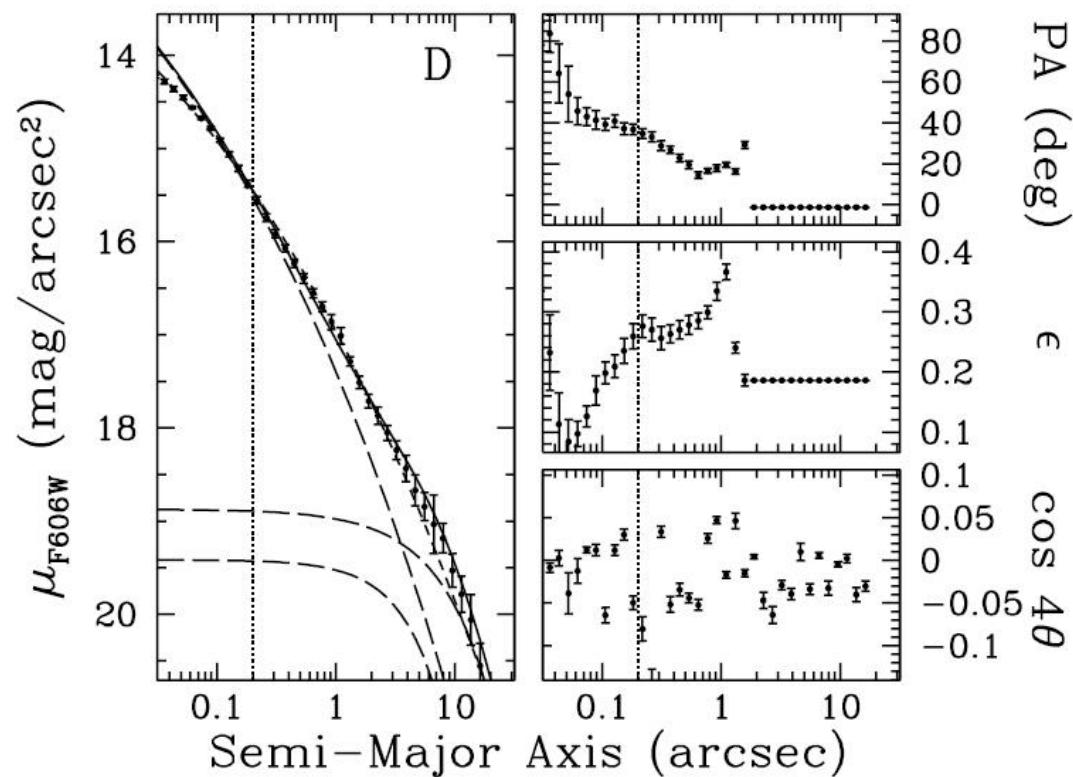
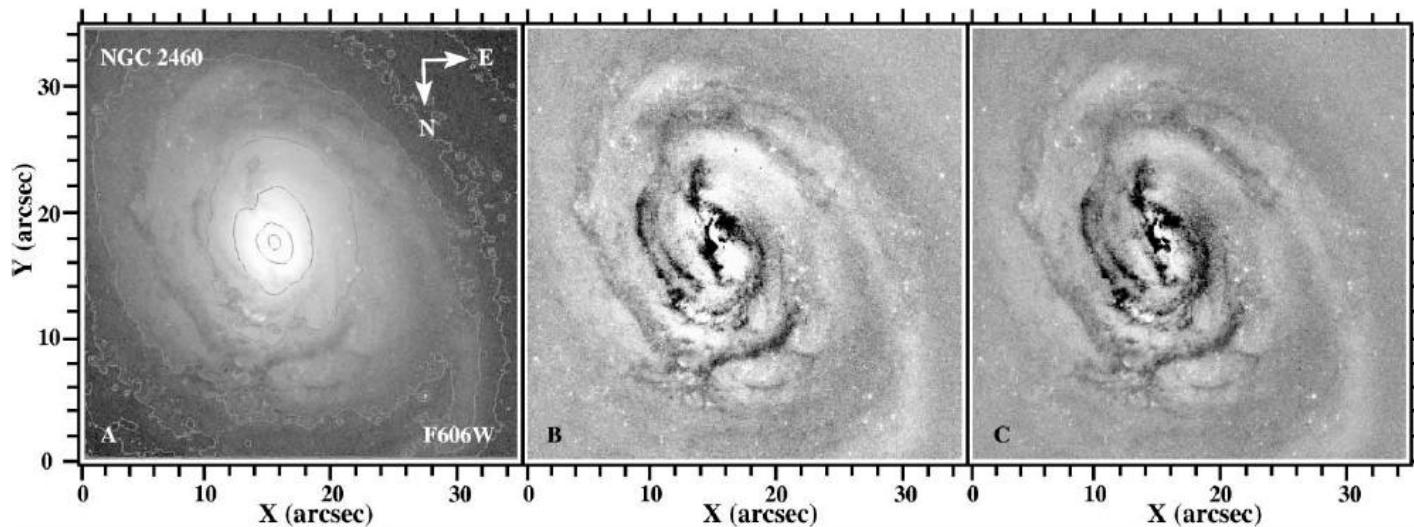
pure ellipse : $c = 0$

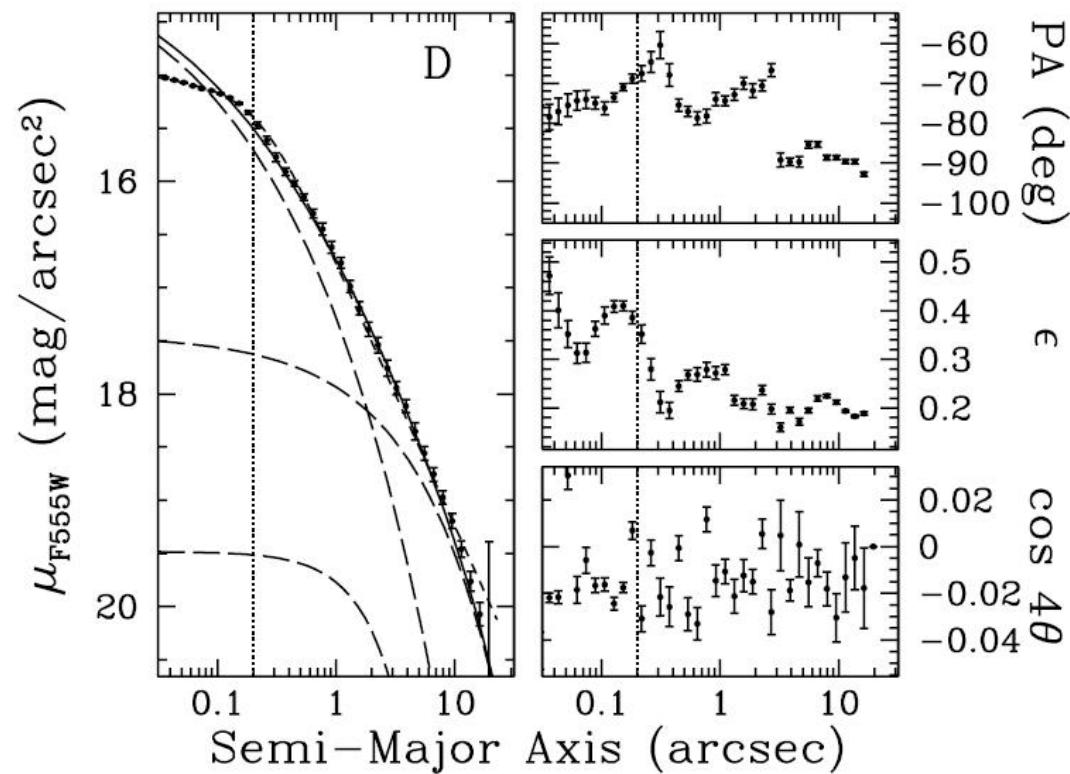
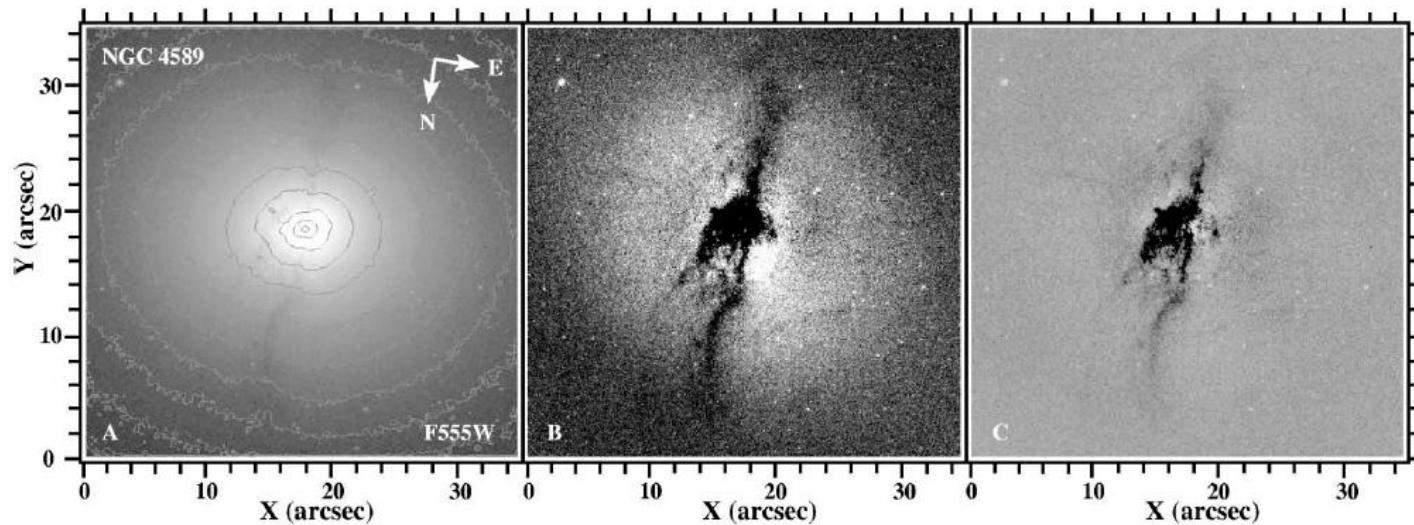
boxy : $c > 0$

disky : $c < 0$

q = minor/major axis ratio







Kinematics of disk galaxies

obtain V_{obs} from spectroscopy:

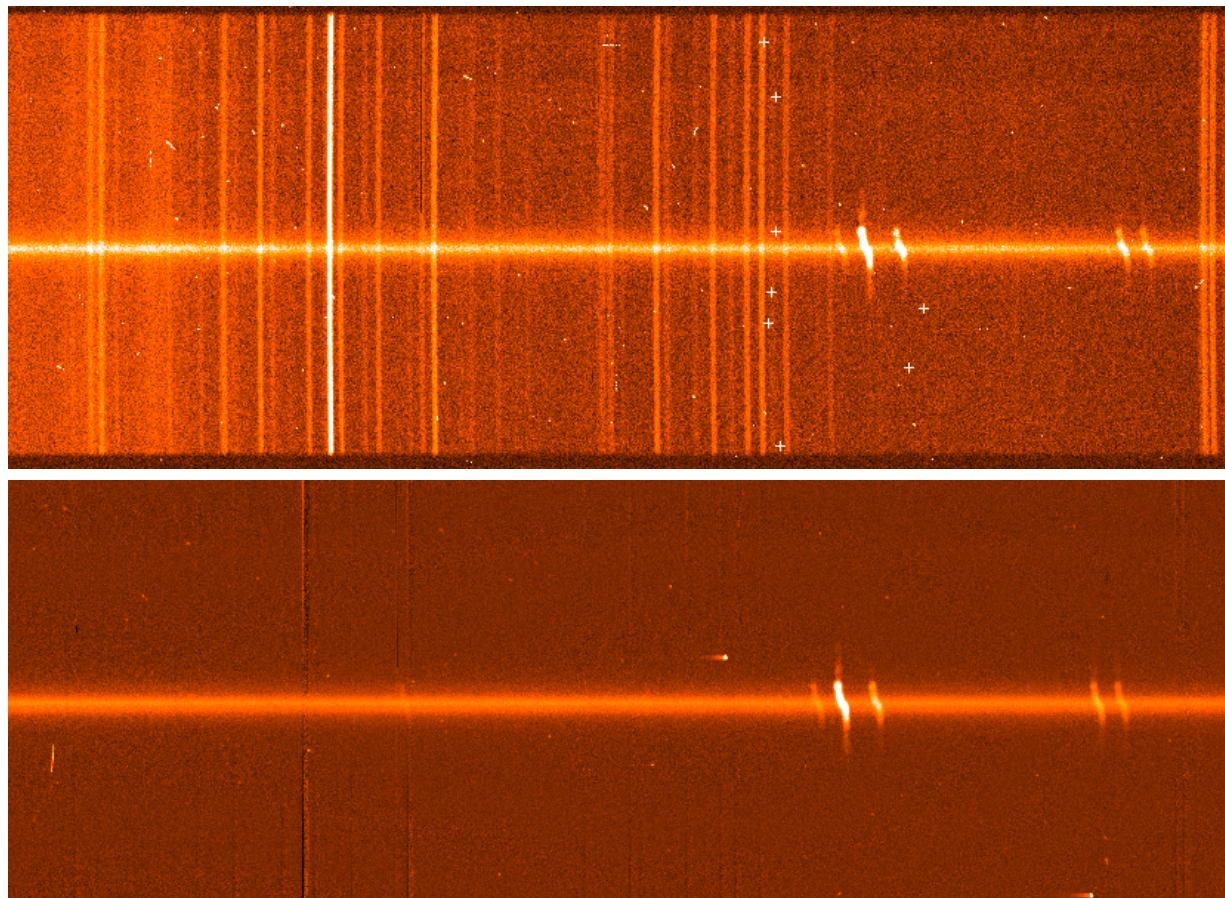
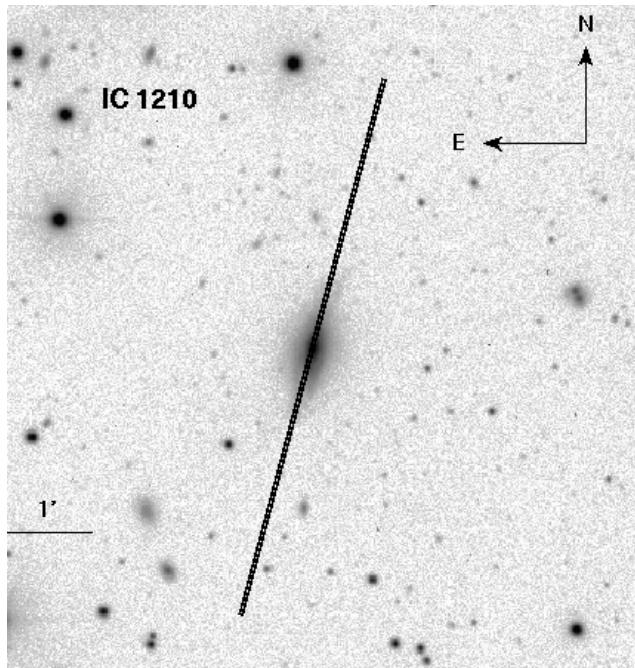
- optical emission lines ($H\alpha$ etc.)
- neutral hydrogen (HI)
- carbon monoxide (CO)

Tracer	angular resolution	spectral resolution
HI	7" ... 30"	2 ... 10 km s ⁻¹
CO	1.5" ... 8"	2 ... 10 km s ⁻¹
$H\alpha$, ...	0.5" ... 1.5"	10 ... 30 km s ⁻¹

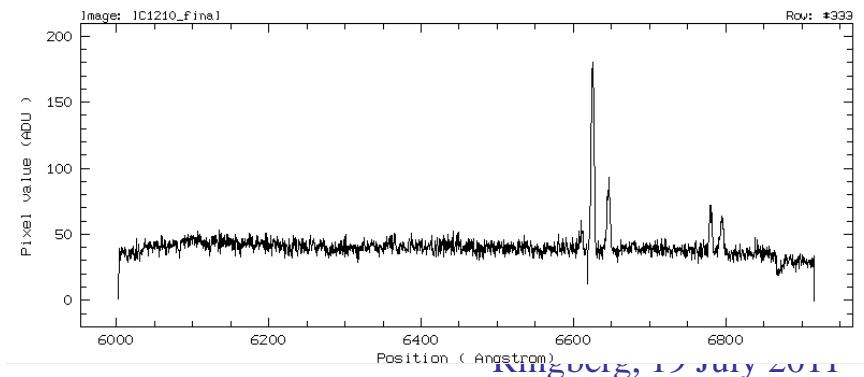


optical spectroscopy \Rightarrow kinematics of inner galaxy (bulge, disk)

long-slit spectroscopy

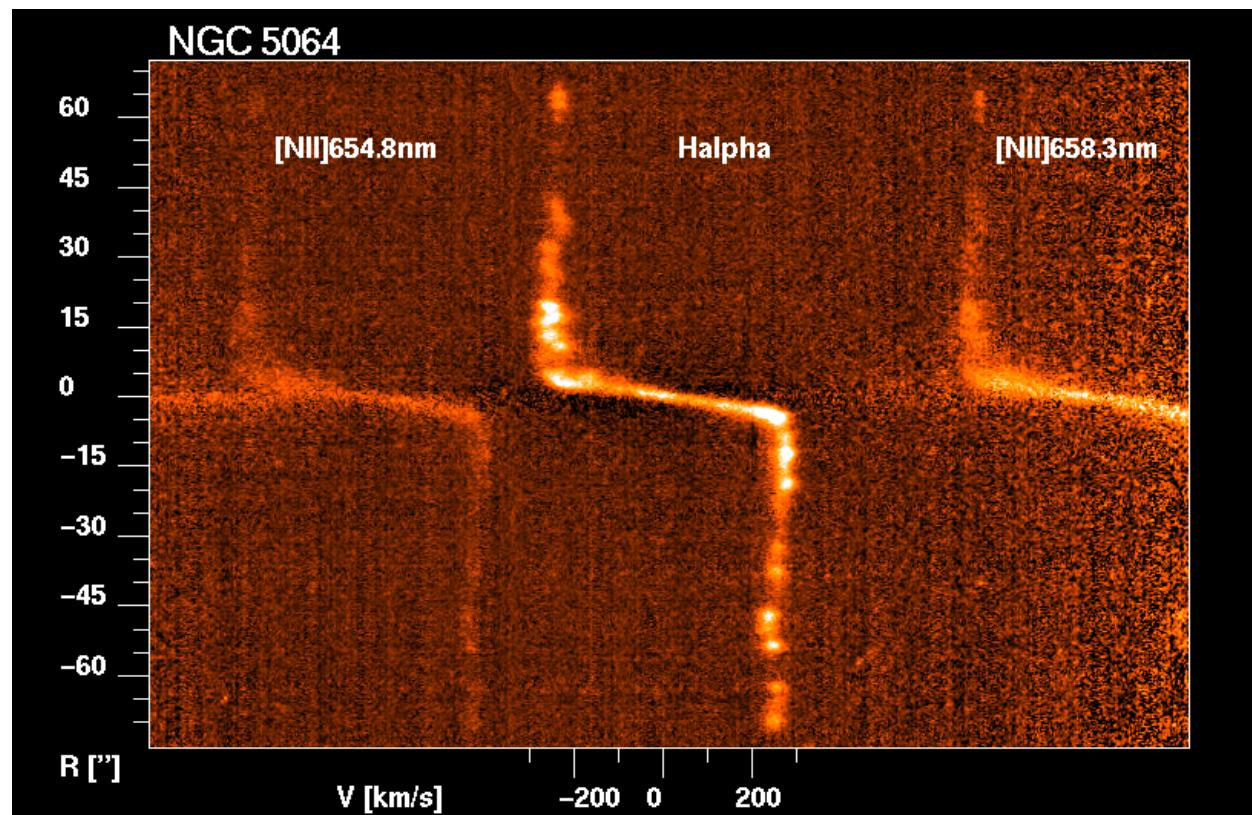


(A. Pizzella's home page)



mainly three lines:	nitrogen	$^3P_1 \rightarrow ^1D_2$	6543 Å
		$^3P_2 \rightarrow ^1D_2$	6583 Å
	hydrogen	H α	6563 Å
	sulfur	$^4S_{1/2} \rightarrow ^2D_{5/2}$	6716 Å
		$^4S_{1/2} \rightarrow ^1D_{3/2}$	6731 Å

$$V = c \frac{\lambda_{obs} - \lambda_0}{\lambda_0}$$



integral-field spectroscopy

e.g. DensePak on WIYN telescope:

91 fibers (7 fiber x 13 fiber rectangle)

fiber diameter: 300 microns = 3 arcseconds

fiber-to-fiber spacing: 4 arcseconds

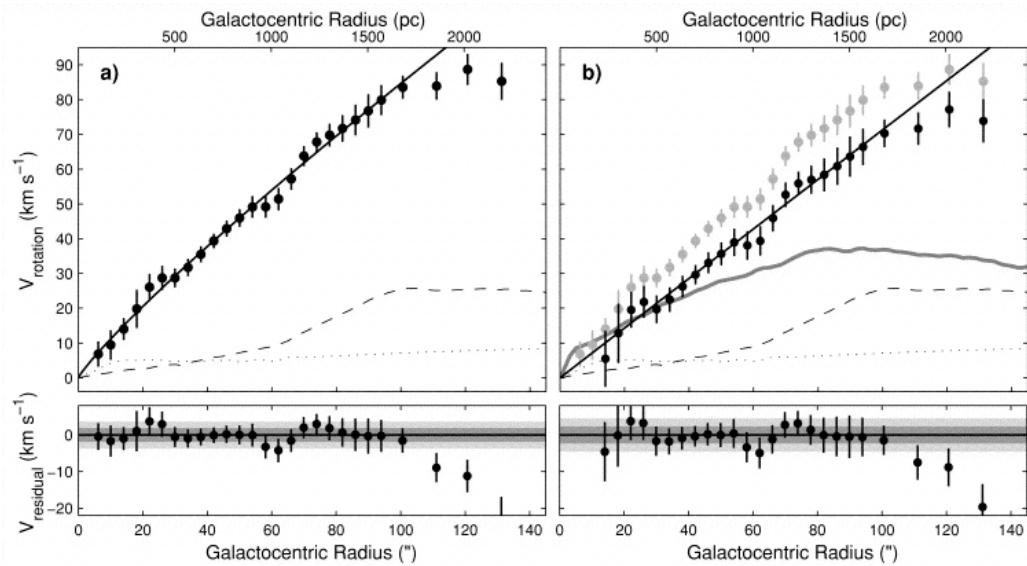
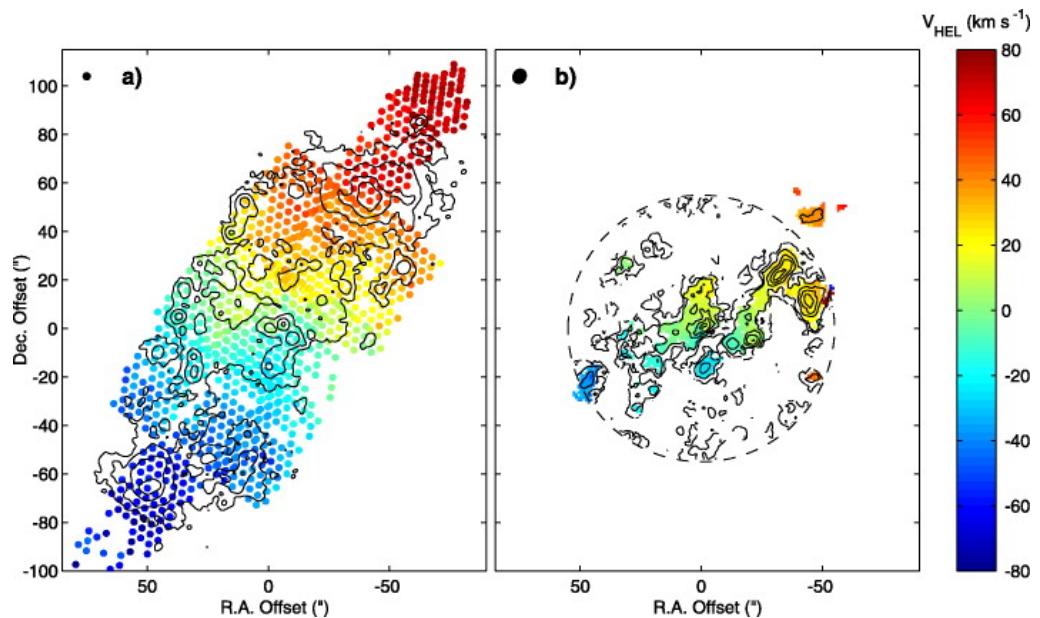
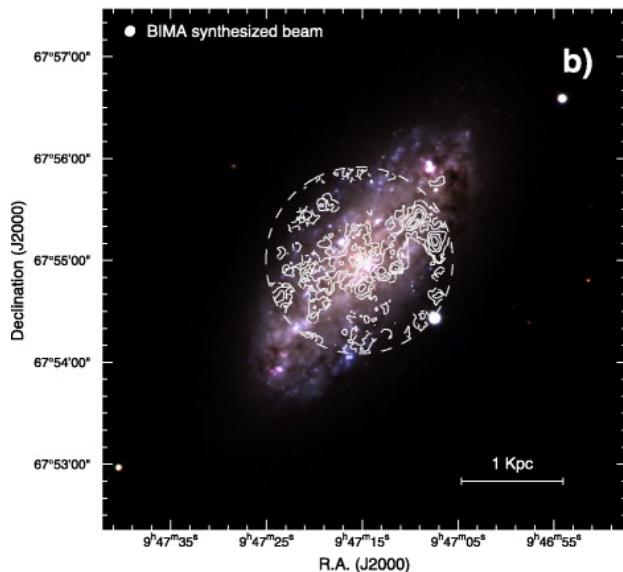
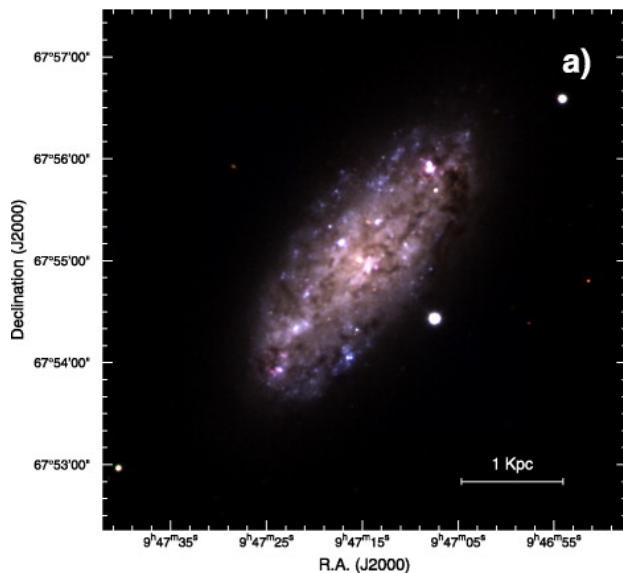
overall dimensions: 30 arcseconds x 45 arcseconds

spectral window: 3700 Å to 1.1 μm

$\Delta V = 13 \text{ km s}^{-1}$ in H α

another one: SAURON on the 4.2-m on WHT

Simon et al. (2003): dwarf spiral NGC2976, H α integral-field + CO

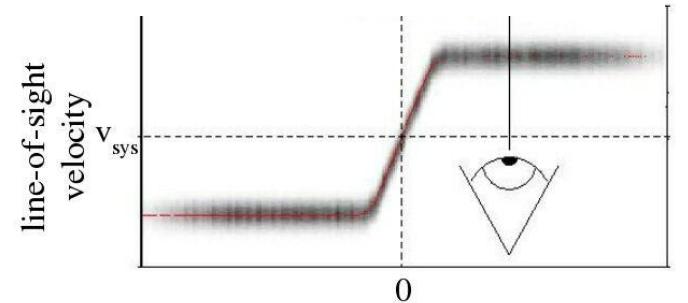
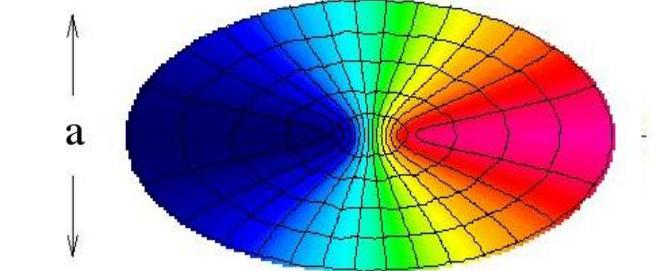


rotation curves: assume symmetric circular rotation of a disk characterized by

- sky coordinates (η_0, ξ_0) of the kinematic centre
- systemic velocity V_{sys} , i.e. the velocity of the galaxy's centre w.r.t. the sun
- circular velocity $V(R)$
- position angle χ of the major axis (clockwise from north)
- inclination angle i between normal to galaxy plane and l.o.s., i.e.

$$i = \arccos\left(\frac{a}{b}\right)$$

now subdivide projected (elliptical) galaxy image into elliptical rings of width ΔR .



radio spectroscopy \Rightarrow data cubes

e.g. 21-cm line:

brightness temperature:

$$T_b = T_b(\xi, \eta, V)$$

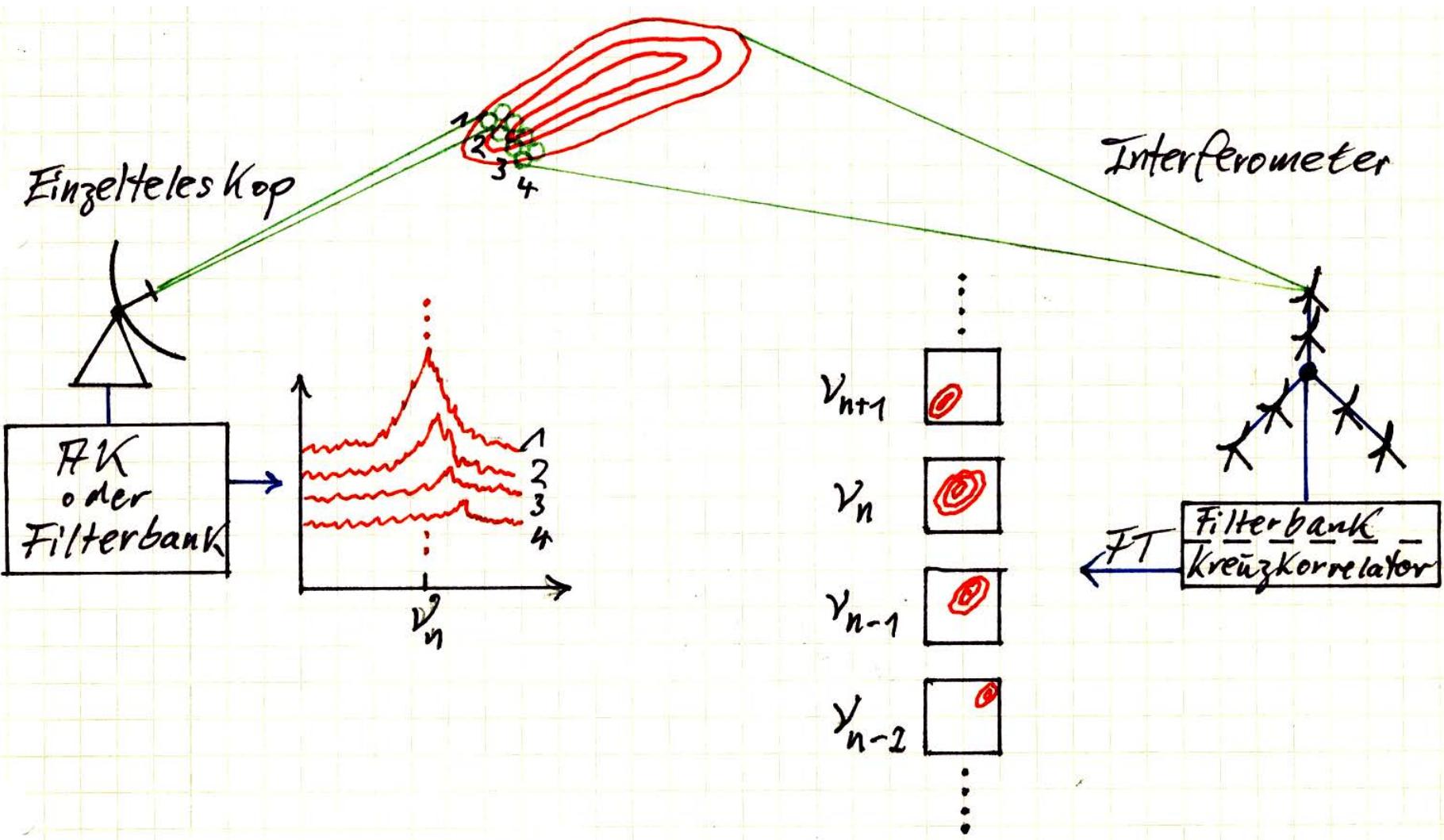
velocity:

$$\langle V(\xi, \eta) \rangle = \frac{\int_{V_1}^{V_2} T_b(\xi, \eta, V) V(\xi, \eta) dV}{\int_{V_1}^{V_2} T_b(\xi, \eta, V) dV}$$

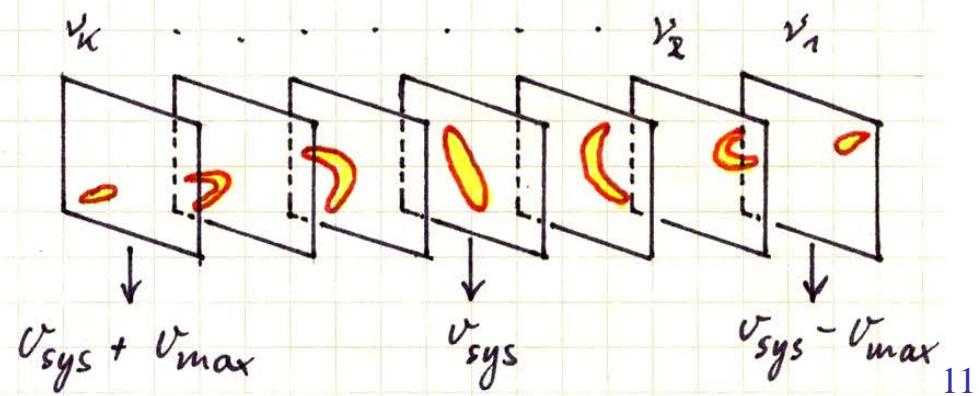
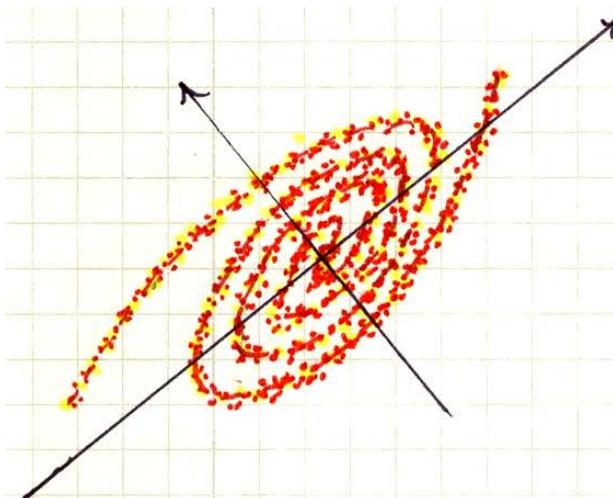
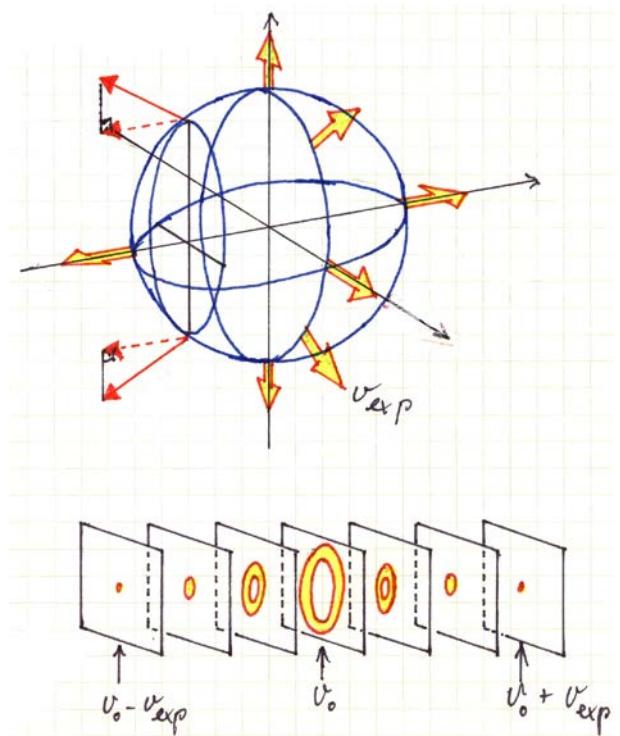
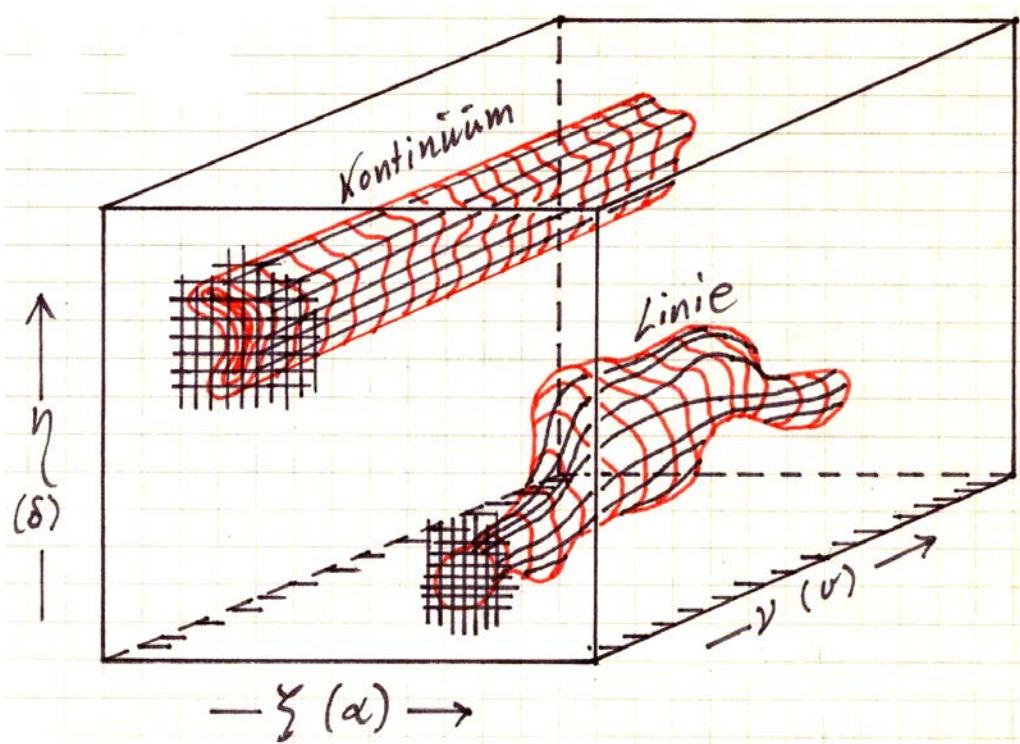
column density (e.g. HI):

$$N_{HI}(\xi, \eta) = 1.822 \cdot 10^{18} \int_{V_1}^{V_2} \left[\frac{T_b(\xi, \eta)}{K} \right] \left(\frac{dV}{km s^{-1}} \right) atoms cm^{-2}$$

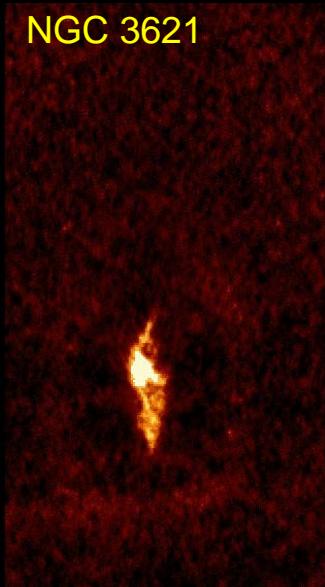
single dish vs. interferometer



data cubes



NGC 3621



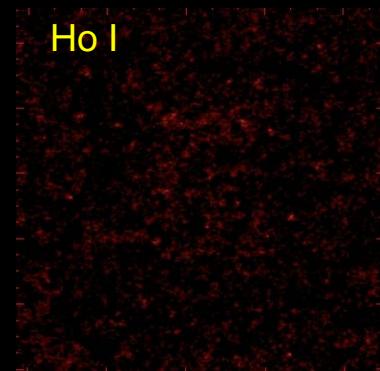
$$L_B \sim 0.5 \times L_*$$

IC 2574

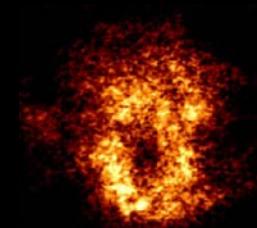
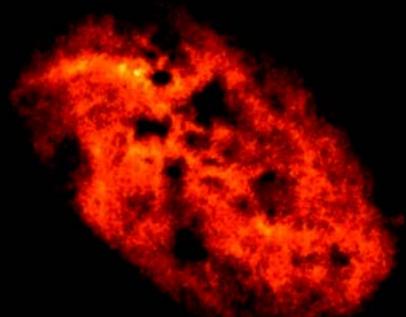
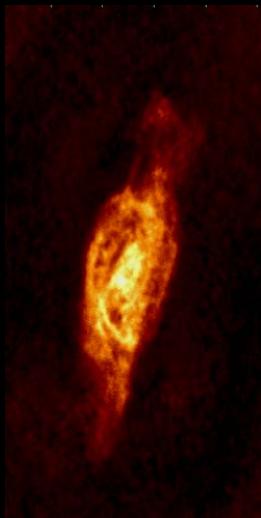


$$L_B \sim 0.06 \times L_*$$

H α I



$$L_B \sim 0.005 \times L_*$$



WSRT



ATCA



VLA



PdB Interferometer



12/1/2000

ALMA



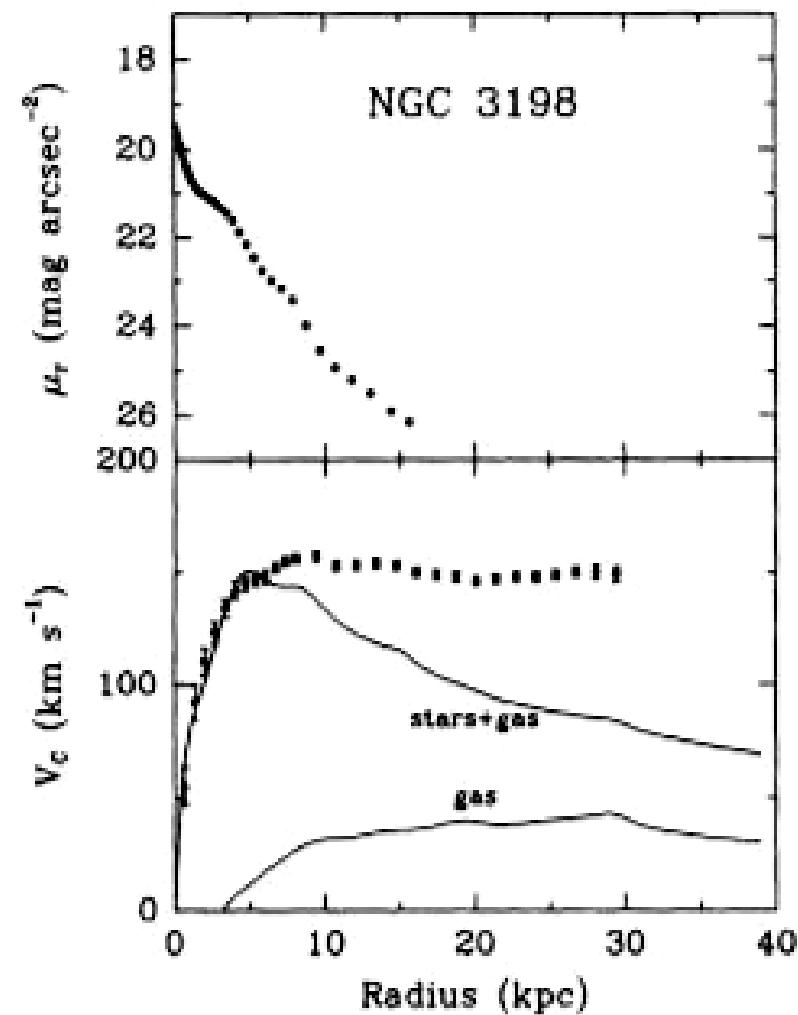
Rotation curves

needed for studies of mass distributions:

rotation curve $V(r)$

problems (see, e.g., Swaters et al. 2003):

- slit position and orientation ($\text{H}\alpha$)
- distribution of tracers (HI, CO, $\text{H}\alpha$)
- spectral smoothing
- spatial smoothing (“beam smearing”)
- finite disk thickness, edge-on galaxies
- anomalous velocities
 - non-circular motions
 - star-forming regions ($\text{H}\alpha$)
- lopsidedness
- warps



Begeman et al. (1989)

tilted-ring analysis of velocity field:

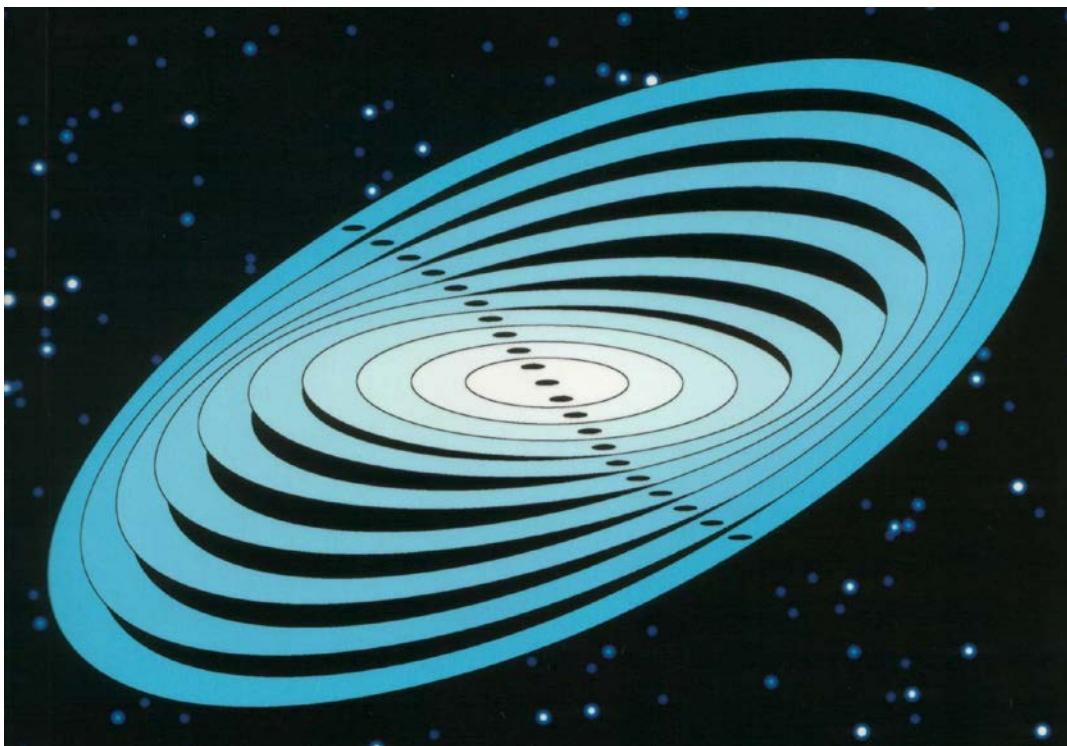
$$V_{obs}(\xi, \eta) = V_{sys} + V(r) \cos \theta \sin i$$

i = inclination angle (0° = face-on)

θ = azimuthal angle

ξ_0 , η_0 , i , χ and V are expected to vary with R

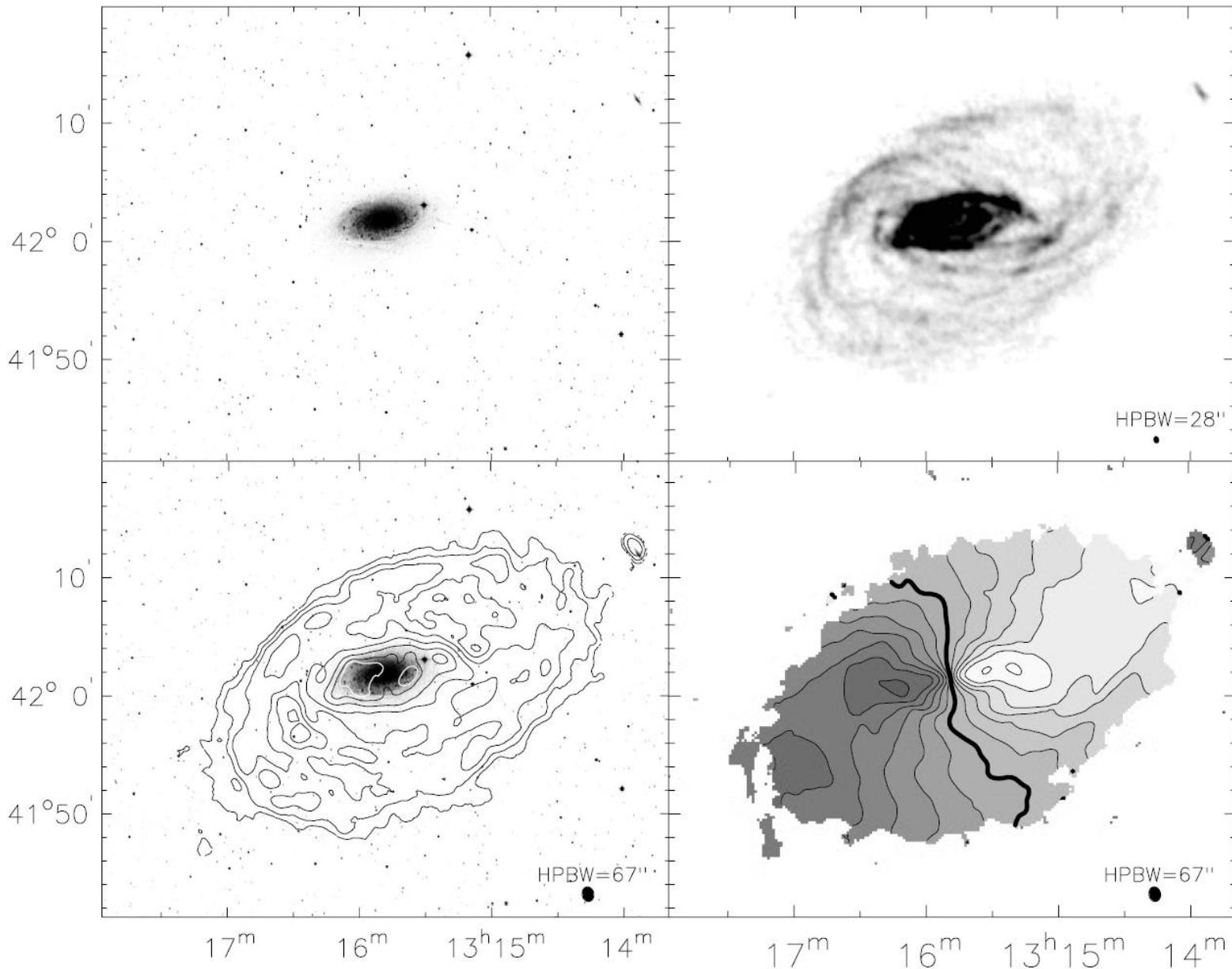
$$\cos \theta = \frac{-(\xi - \xi_0) \sin \chi + (\eta - \eta_0) \cos \chi}{R}$$
$$\sin \theta = \frac{-(\xi - \xi_0) \cos \chi - (\eta - \eta_0) \sin \chi}{R \cos i}$$

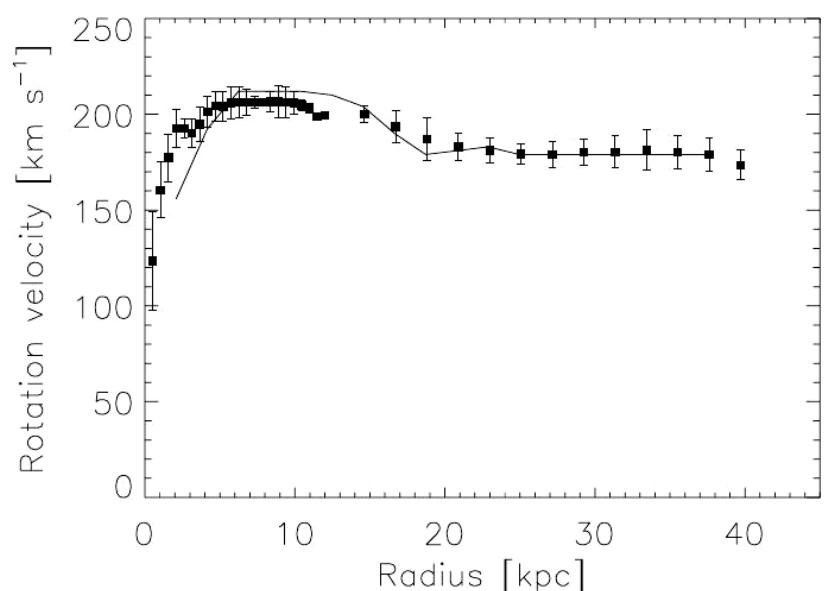
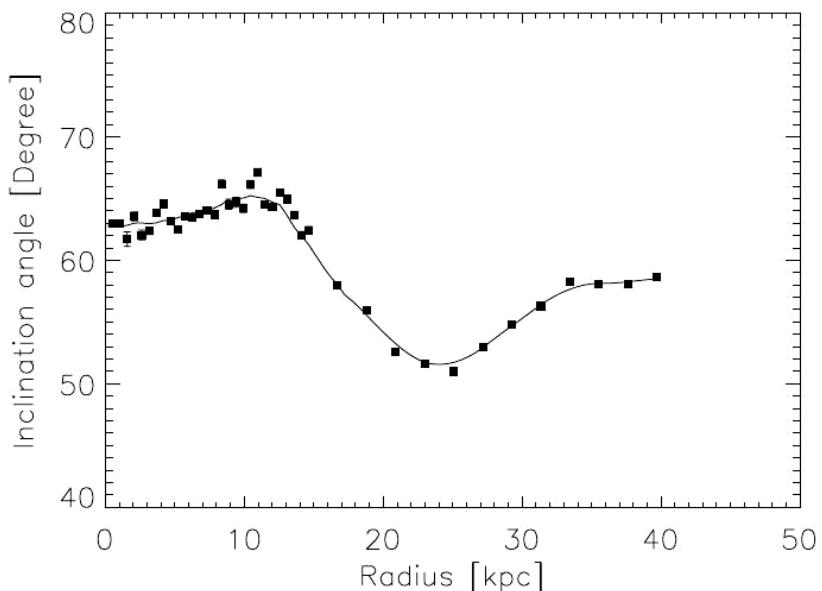
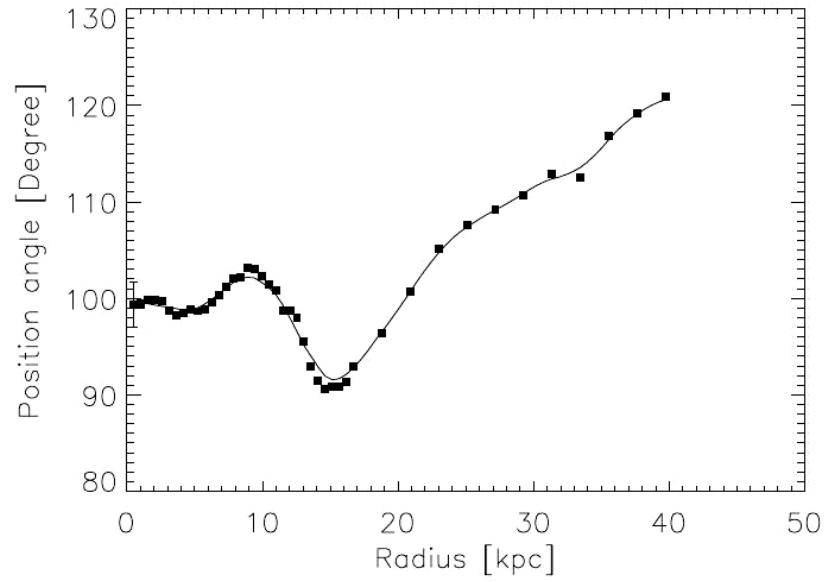
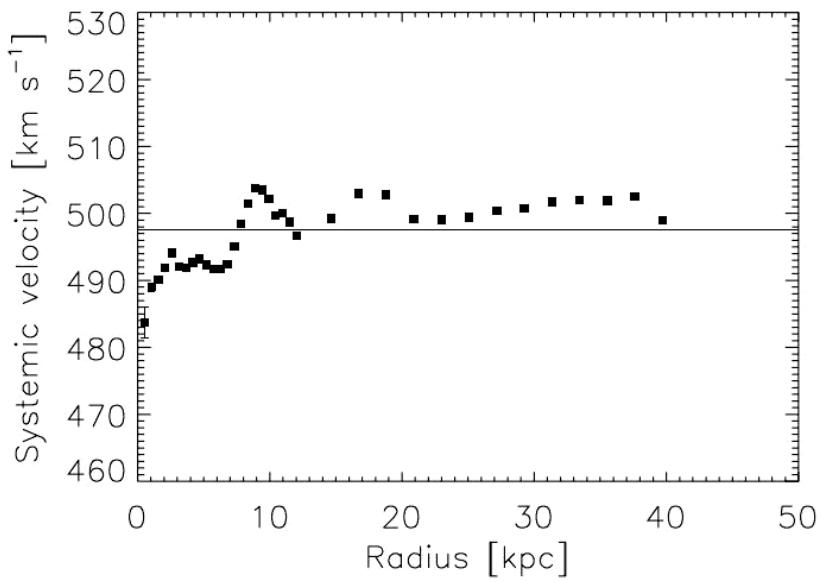


procedure (Begeman 1989):

1. divide galaxy into concentric rings (width ~ 1 beam width)
2. estimate initial values of V_0 , ξ_0 , η_0 , V_c , i and χ
3. calculate initial radial velocities $V(\xi, \eta) \Rightarrow 1^{\text{st}}$ moment
4. make least-squares fit for parameters V_0 , ξ_0 , η_0 , V_c , i and χ , using observed velocity field and initial guess determined above
5. improved values of basic parameters define new set of sky coordinates ξ, η ; go to 3 until convergence is reached; iteration process is monitored by calculating χ^2

Battaglia et al. (2006)





fit parameters in RC fitting:

$$V_{rot}^2(r) = V_{DM}^2(r) + V_b^2(r) + V_d^2(r) + V_{HI}^2(r) + V_{H_2}^2(r)$$

stars

mass-to-light ratio of optical band X: \odot_X (disk, bulge)

gas

- HI: straight forward, just account for helium, $X_{He} \approx 1.3 \dots 1.4$
- H₂: conversion from CO brightness to H₂ column density, X_{CO}

dark halo

- core or characteristic radius : r_0, r_s
- central or characteristic density : ρ_0, ρ_s

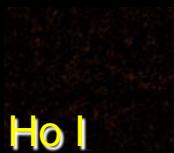
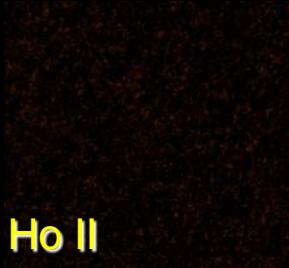
MOND

- acceleration : a_0 (although this ought to be a universal constant)
- distance : D

now perform mass decomposition

needs excellent data quality!

from *THINGS*:



NGC 2903

Probing the galaxy potential

Poisson equation:

$$\vec{\nabla}^2 \Phi = 4\pi \cdot G \cdot \rho$$

in principle for axi-symmetric potentials: measure circular rotation speed V and infer density ρ

for spherical (DM, stellar bulge) potential: measure circular rotation speed $V_{DM}(r)$ and infer $\rho_{DM}(r)$ using

$$\begin{aligned}\vec{\nabla}^2 \Phi_{DM}(r) &= 4\pi \cdot G \cdot \rho_{DM}(r) \\ &= \left(\frac{V_{DM}}{r} \right)^2 + 2 \cdot \left(\frac{V_{DM}}{r} \right) \cdot \frac{\partial V_{DM}}{\partial r}\end{aligned}$$

⇒ most simple inversion method in case of (e.g.) dominating (spherical) DM halo

or, vice versa:

$$M(< r) = \int_0^r 4\pi r'^2 \rho(r') dr'$$

$$V^2(r) = \frac{GM(< r)}{r}$$

e.g. quasi-isothermal halo:

$$\rho(r) = \rho_0 \left(1 + \frac{r^2}{r_0^2} \right)^{-1}$$

i.e.

$$\begin{aligned} M(< r) &= 4\pi \rho_0 \int_0^r \frac{r'^2 r_0^2}{r_0^2 + r'^2} dr' \\ &= 4\pi \rho_0 r_0^2 r \left(1 - \frac{r_0}{r} \arctan \frac{r}{r_0} \right) \end{aligned}$$

so: measure $V_{rot}(\mathbf{r})$, calculate $V_{stellar}(\mathbf{r})$, $V_{gas}(\mathbf{r})$, and deduce $V_{DM}(\mathbf{r})$

$$V_{rot}^2 = V_{DM}^2 + V_{stellar}^2 + V_{gas}^2$$

stellar component : bulge (b) and disk (d)

gaseous component : HI and H₂

$$V_{rot}^2 = V_{DM}^2 + V_b^2 + V_d^2 + V_{HI}^2 + V_{H_2}^2$$

high-precision rotation curve delivers $V_{rot}(\mathbf{r})$

mass surface densities yield $V_{stellar}(\mathbf{r})$, $V_{gas}(\mathbf{r})$

$$V_{DM} = \sqrt{V_{rot}^2 - V_b^2 - V_d^2 - V_{HI}^2 - V_{H_2}^2}$$

stellar disk

solution for infinitely thin exponential disk, which has intensity an distribution

$$I(r) = I_0 \cdot e^{-r/r_D}$$

is (Freeman 1970)

$$V_d^2(r) = 4\pi G \Sigma_0 r_d y^2 [I_0(y)K_0(y) - I_1(y)K_1(y)]$$

$I(R)$ and I_0 have units of $L_\odot \text{ pc}^{-2}$, and $y = R / 2R_d$.

with stellar mass-to-light ratio \odot_* :

$$\Sigma_0 = K_* I_0$$

solution for truncated thick disk reads (Casertano 1983)

$$V_d^2(r) = 4\pi G r \int_0^\infty du \int_0^\infty d\zeta \frac{2\sqrt{u}}{\pi\sqrt{r p}} [\mathcal{K}(p) - \mathcal{E}(p)] \frac{\partial}{\partial u} [\rho(u, \zeta)]$$

where \mathcal{K} and \mathcal{E} are complete elliptical integrals,

$$p = x - \sqrt{x^2 - 1}$$

and

$$x = \frac{r^2 + u^2 + \zeta^2}{2Ru}$$

now plug in numerically any density distribution $\rho(R, z)$ and obtain (circular) velocity of the disk component.

gaseous disk

in general not an exponential disk, but rather has arbitrary $\Sigma(R)$, so use Casertano (1983) formalism:

$$V_{gas}^2(r) = 4\pi G r \int_0^\infty du \int_0^\infty d\zeta \frac{2\sqrt{u}}{\pi\sqrt{rp}} [\mathcal{K}(p) - \mathcal{E}(p)] \frac{\partial}{\partial u} [\rho(u, \zeta)]$$

observed: $N_H(R)$, readily converted into mass surface density $\Sigma_H(R)$

divide by effective thickness of gaseous disk to obtain density ρ

$$\rho_{gas}(r) = 1.4 \cdot \Sigma_{gas}(r) \cdot \left(\int_{-\infty}^{\infty} e^{-z/z_0} dz \right)^{-1}$$

factor of 1.4 accounts for presence of helium.

note: N_{HI} results directly from 21-cm line

N_{H2} results indirectly via CO line (s.b.)

Dark halos

Burkert (1995) established empirical law that fits (DM-dominated) dwarf Galaxies best; characterized by central density ρ_0 and core radius r_0

$$\rho(r) = \frac{\rho_0 r_0^3}{(r + r_0)(r^2 + r_0^2)}$$

test particle has circular velocity

$$V^2(r) = 2\pi G \rho_0 \frac{r_0^3}{r} \left[\ln\left(\frac{r + r_0}{r_0}\right) + \frac{1}{2} \ln\left(\frac{r^2 + r_0^2}{r_0^2}\right) - \arctan\frac{r}{r_0} \right]$$

numerical simulations in the (Λ) CDM framework yield halos that are best fitted by analytic function (Navarro, Frenk & White 1997) referred to as “NFW profile”

$$\rho(r) = \frac{\rho_s}{r/r_s (1 + r/r_s)^2}$$

test particle in such a potential has circular velocity

$$V^2(r) = V_{200}^2 \frac{1}{x} \frac{\ln(1 + cx) - (cx/1 + cx)}{\ln(1 + c) - (c/1 + c)}$$

where $x = r/r_{200}$. V_{200} is the circular velocity at r_{200} , the “virial radius”, for which $\langle \rho \rangle = 200 \rho_{crit}$. c is the concentration parameter defined as

$$c = \frac{r_{200}}{r_s}$$

concentration parameter c , characteristic radius r_s and density ρ_s are connected by

$$c \approx 20 \left(\frac{M_{vir}}{10^{11} M_\odot} \right)^{-0.13}$$

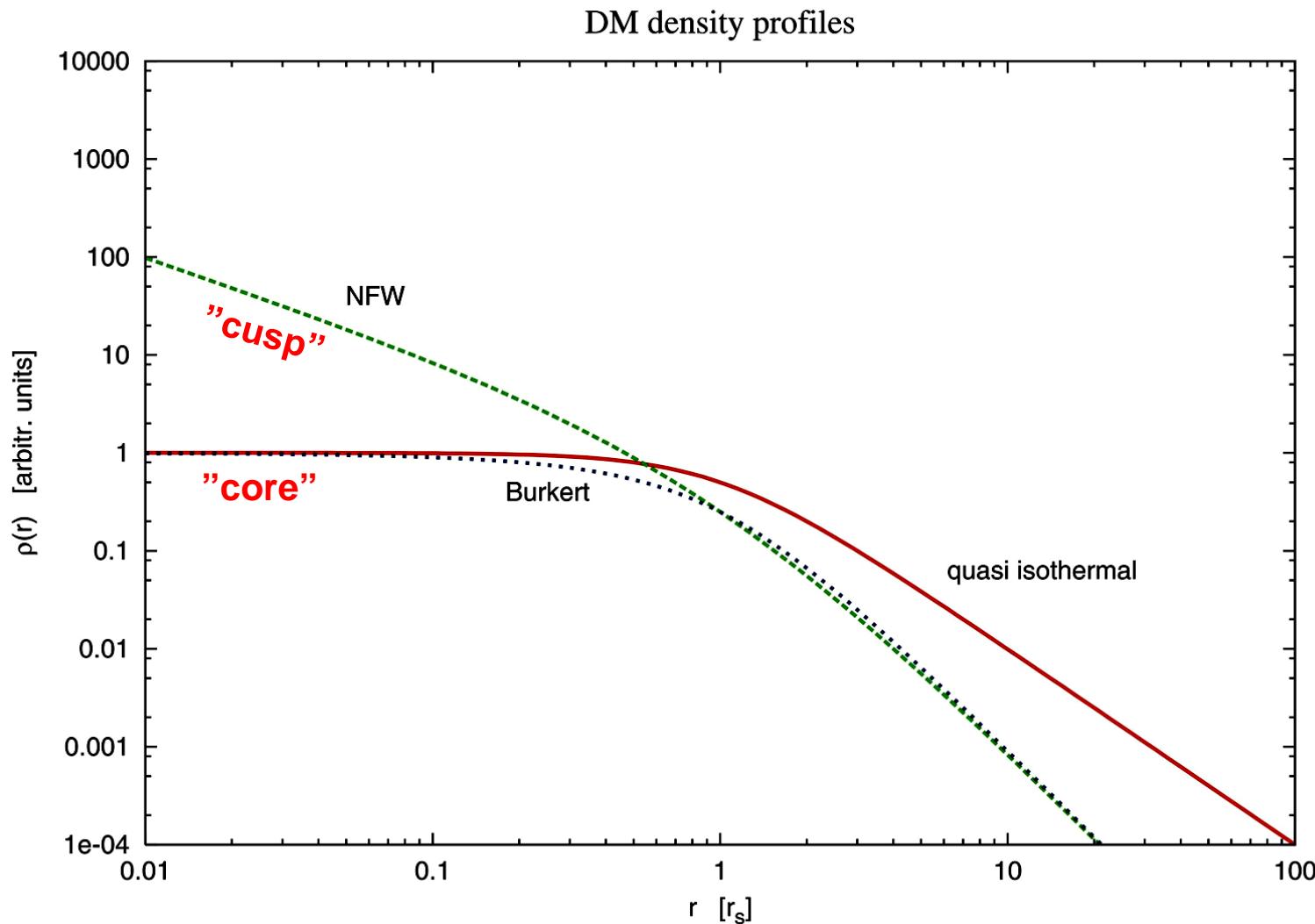
$$r_s \approx 5.7 \left(\frac{M_{vir}}{10^{11} M_\odot} \right)^{0.46} \text{ kpc}$$

$$\rho_s \approx \frac{\Delta}{3} \frac{c^3}{\ln(1+c) - c/(1+c)} \rho_{crit}$$

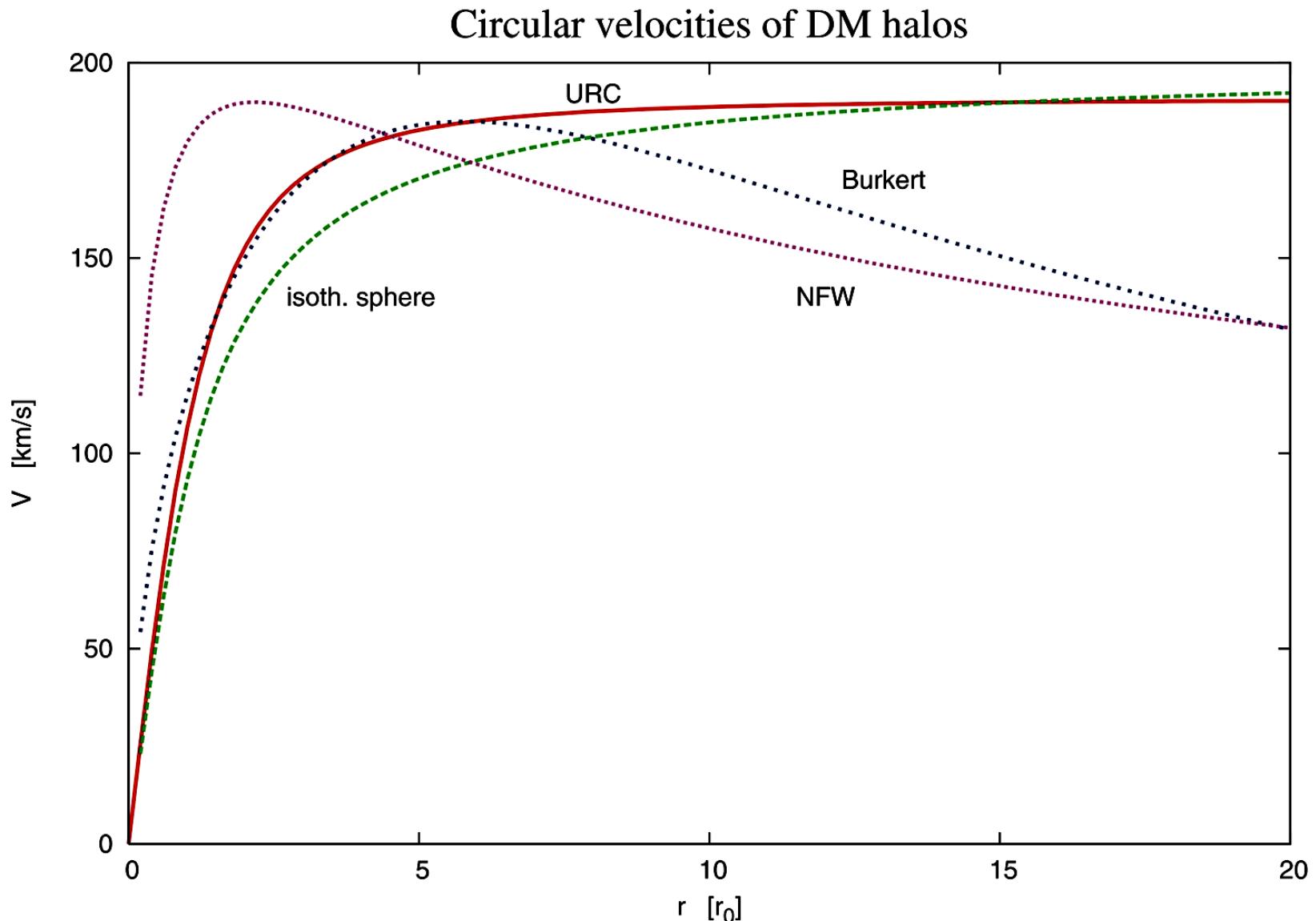
$$M_{vir} \equiv \frac{4}{3} \pi r_{200}^3 \Delta \cdot \rho_{crit}$$

$\Delta \approx 337$ is the overdensity at $z = 0$ (see Bryan & Norman 1998).

“cuspy” and “cored” density profiles of DM halos



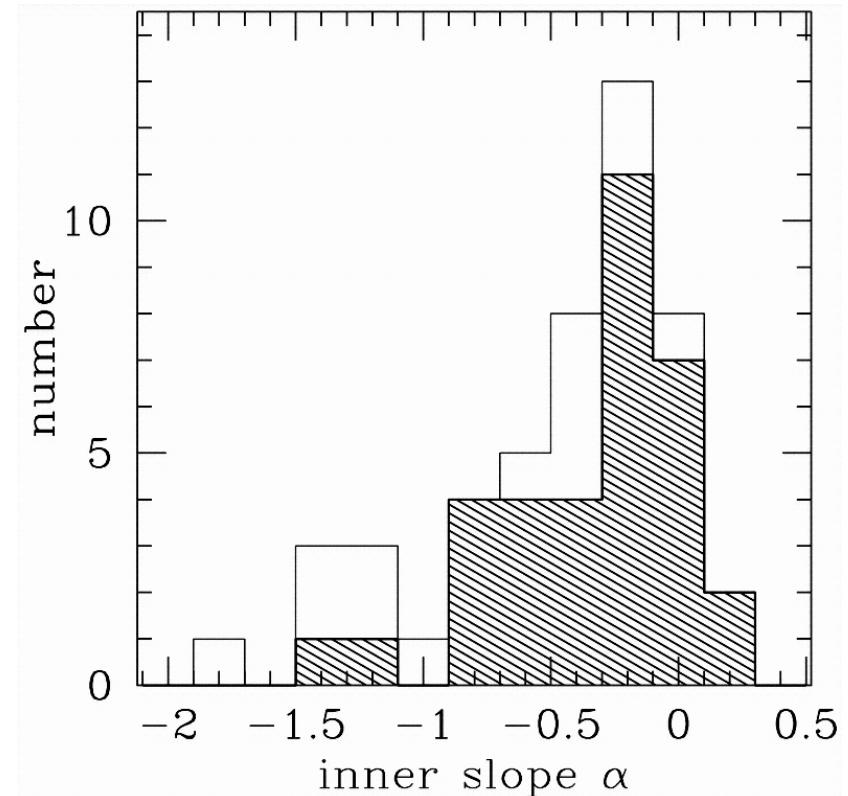
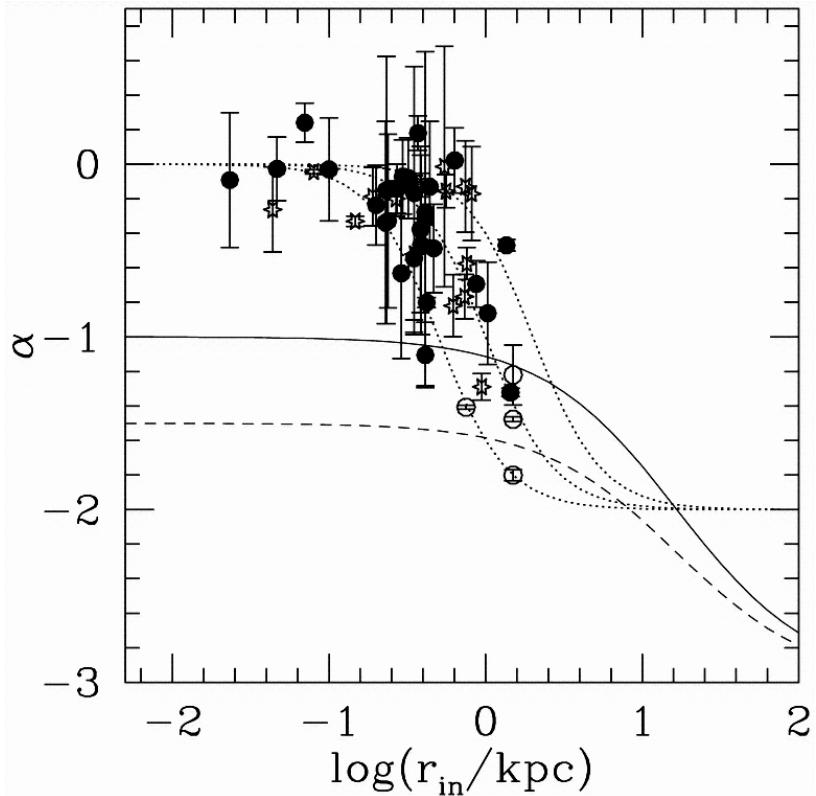
... and the circular velocities of DM halos



e.g. de Blok et al. (2001a): 48 LSB galaxies

high-resolution RCs ($\text{H}\alpha + \text{HI}$)

inner slopes strongly peaked around $\alpha = -0.2$ for $\rho_{DM} \propto r^\alpha$



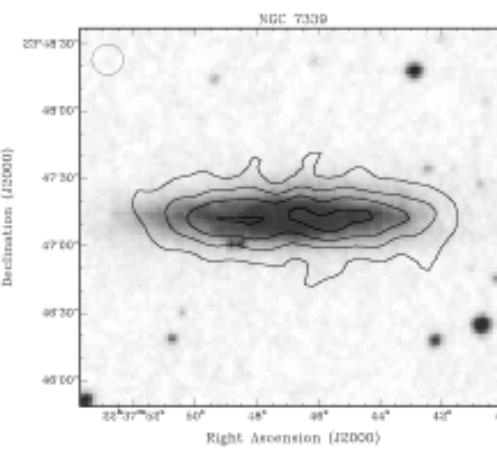
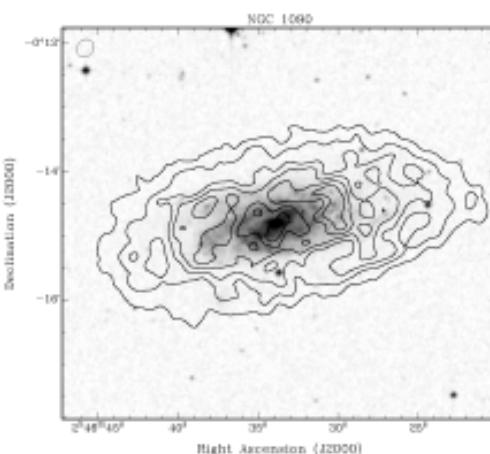
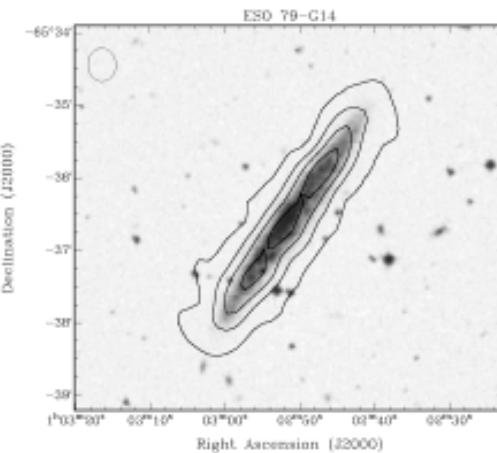
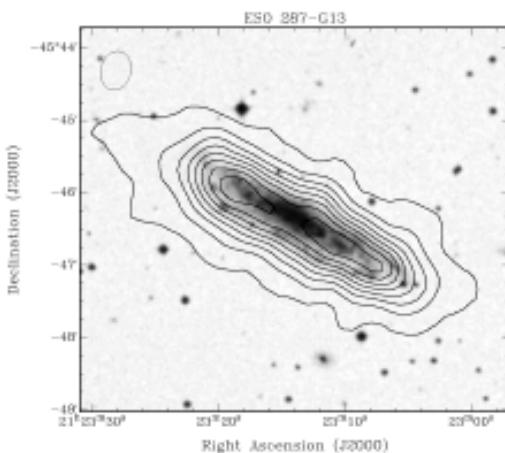
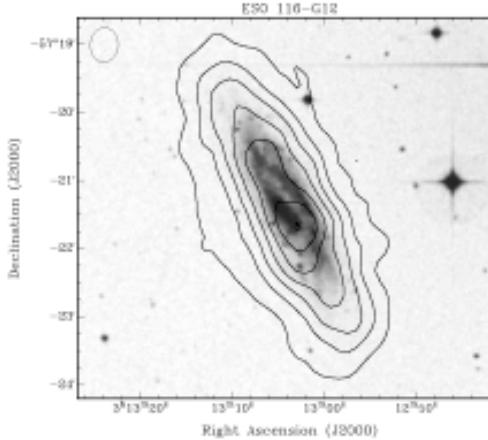
dotted : isothermal halo, with core radii of 0.5, 1 and 2 kpc

solid : NFW model
dashed : Moore } $c = 8$ and $V_{200} = 100 \text{ km s}^{-1}$

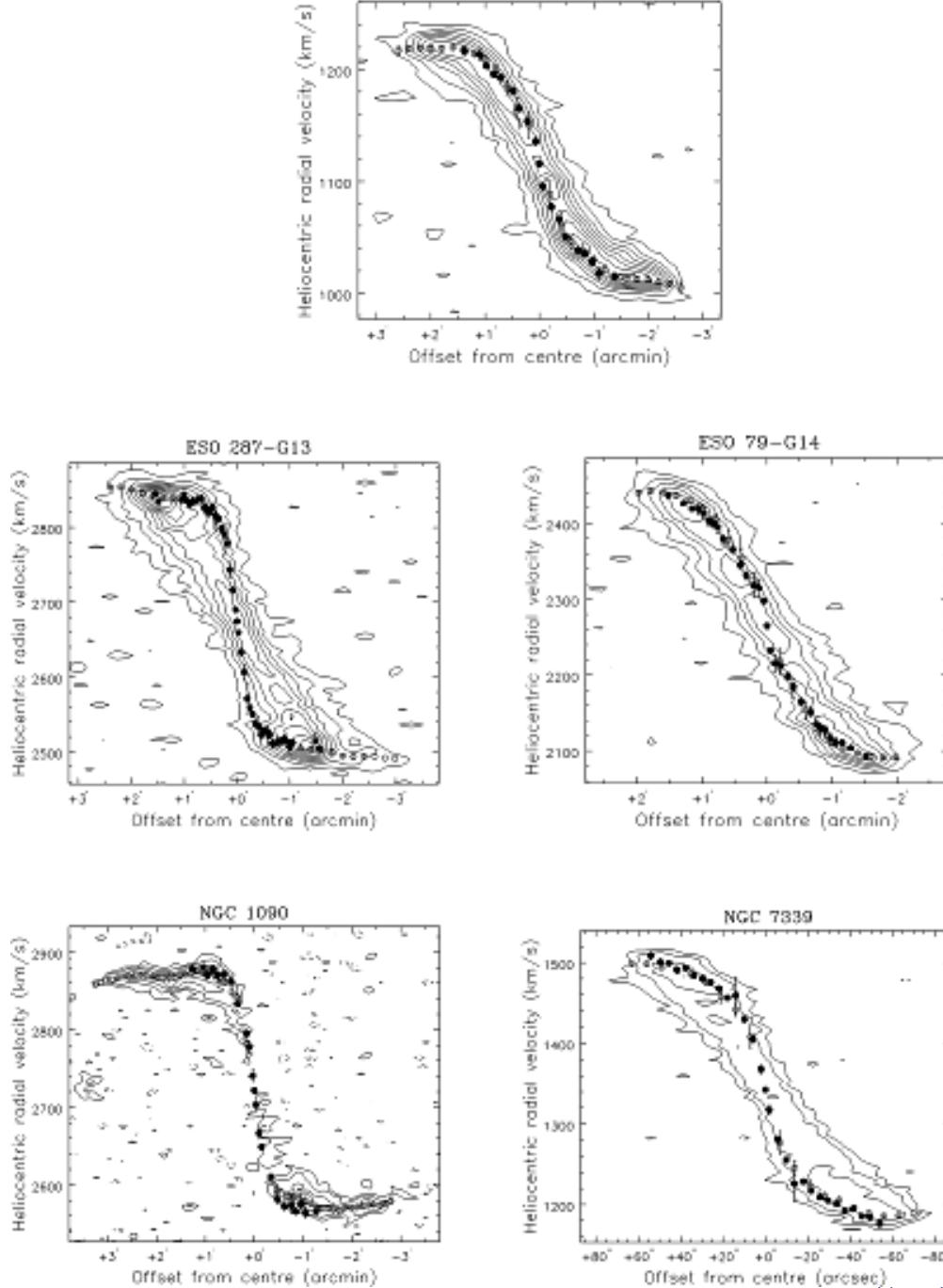
Gentile et al. (2004):

sample of spiral galaxies with

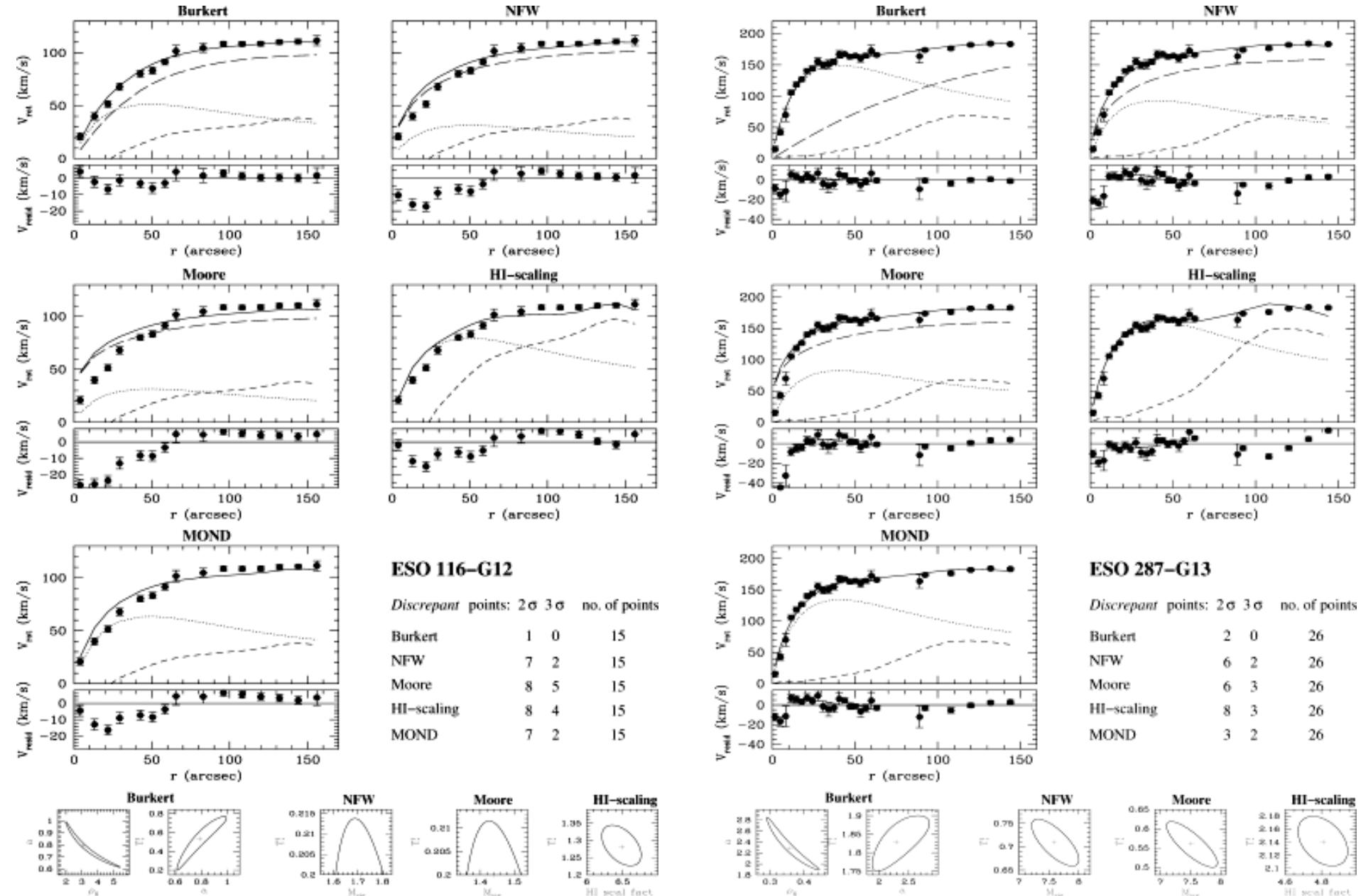
- low luminosities
- precise optical RCs available
- late type (small or no bulges)
- well known distances



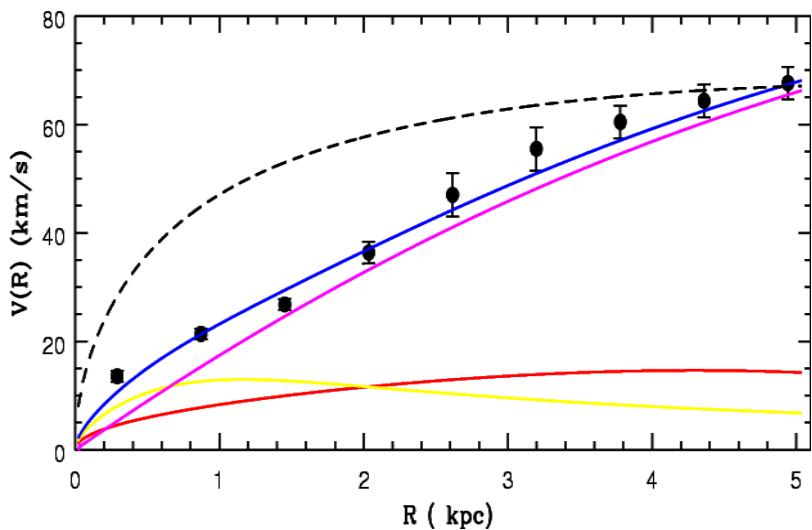
derived rotation curves



comparison with models

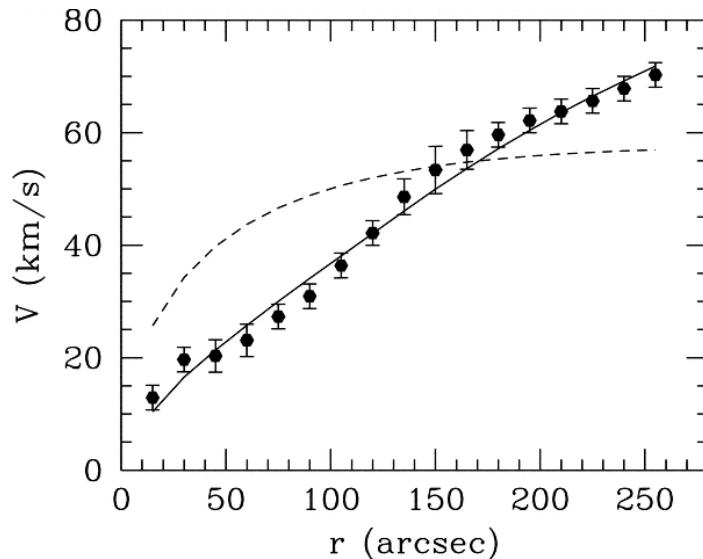


fits with NFW (dashed) and Burkert (magenta & black solid) law



last point matches M_{vir}

NFW “flagrantly” bad ($c = 25$)
Burkert yields: $r_0 = 7$ kpc
 $\rho_0 = 1.4 \cdot 10^{-24} \text{ g cm}^{-3}$



c left as free parameter

Relation to magnetic fields

'flux freezing':

magnetic fields tightly coupled to gas
(via ionized component)

⇒ B-field influenced by kinematics!

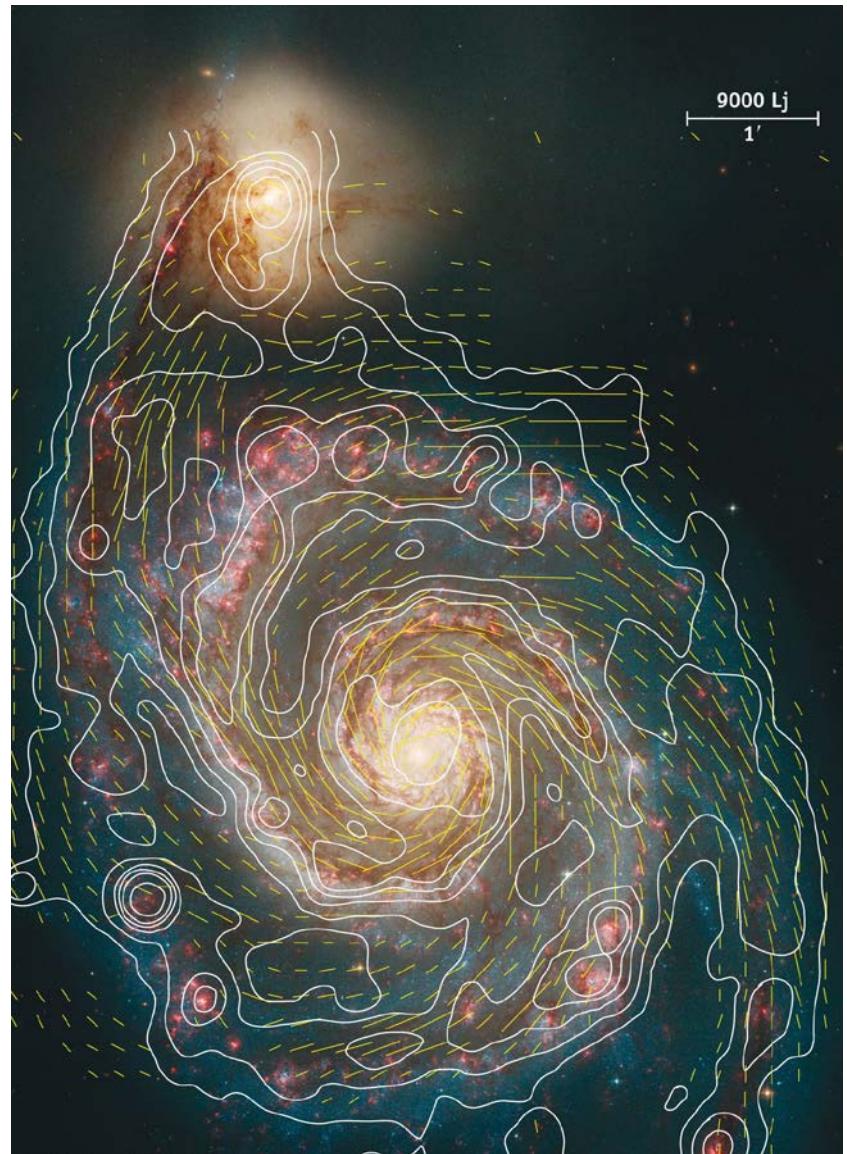
observations:

B-field follows spiral arms

kinematics:

- galactic rotation
- spiral density waves

B-field influenced by density waves?



Fletcher et al. (2011)

Ringberg, 19 July 2011

influence by magnetic field on gas kinematics requires

$$\frac{B^2}{8\pi} \approx \rho (\Delta V)^2$$

e.g.

turbulence: $u_{mag}/u_{kin} \approx 3$

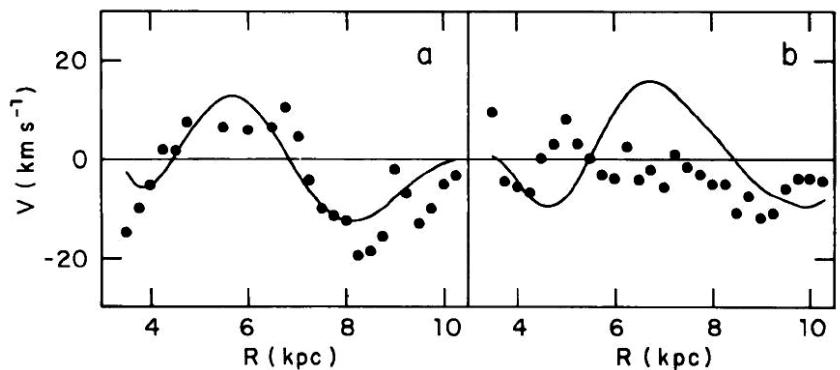
rotation: $u_{mag}/u_{kin} \approx 10^{-4}$

magnetic field passive on large scales

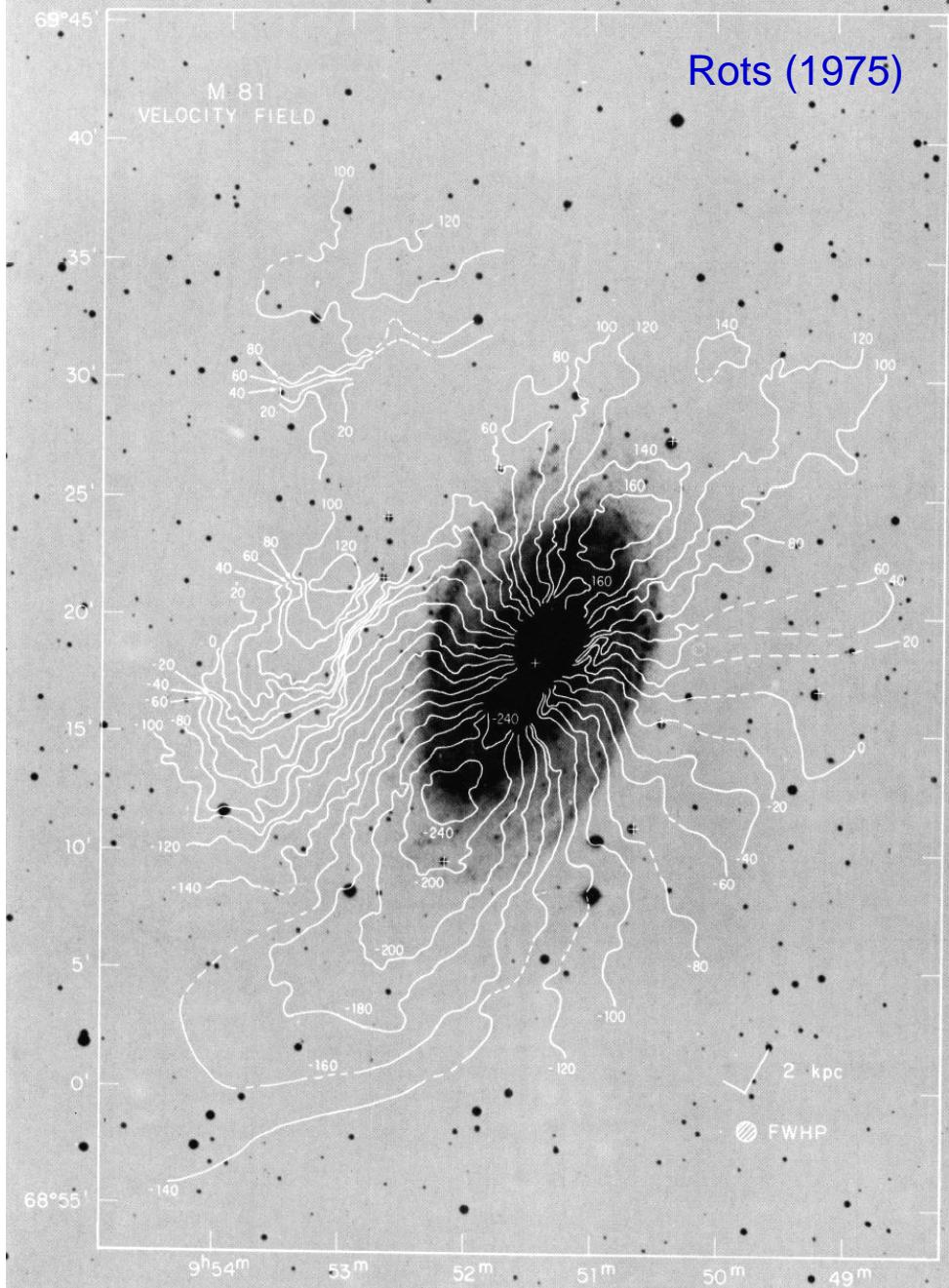
density waves

classical case: M 81 (Rots 1975)

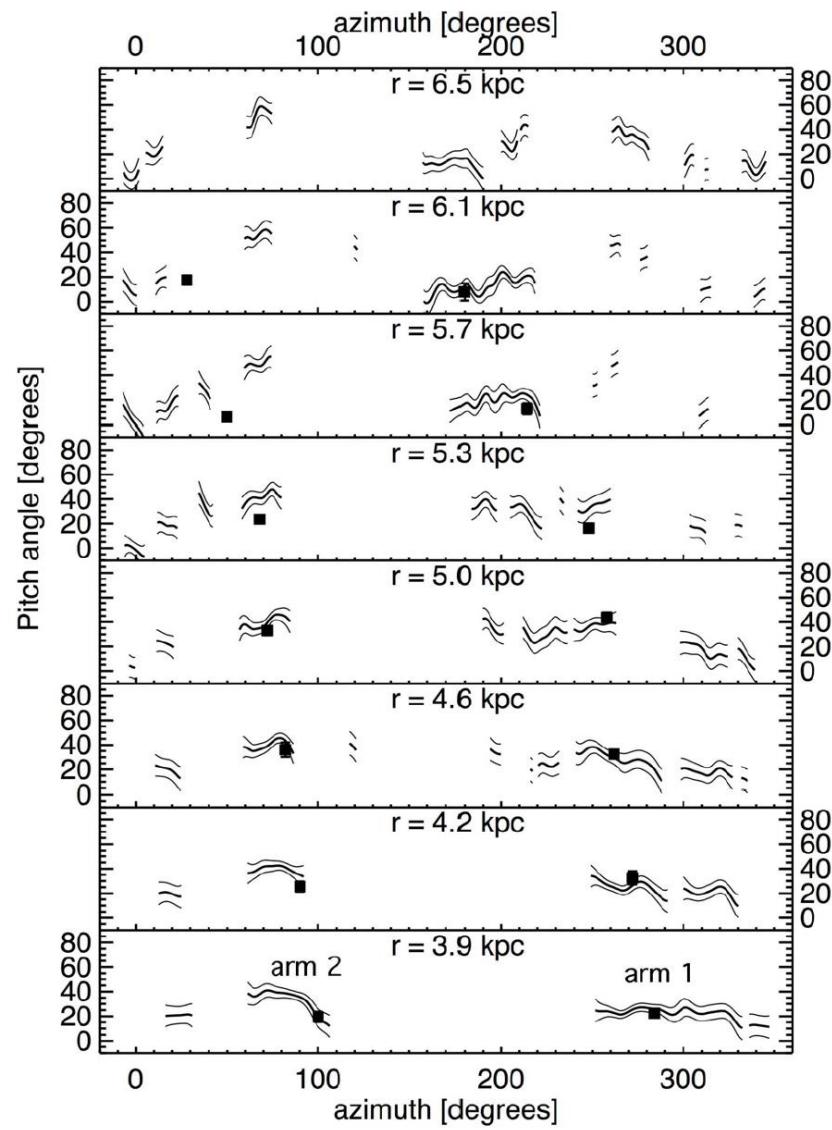
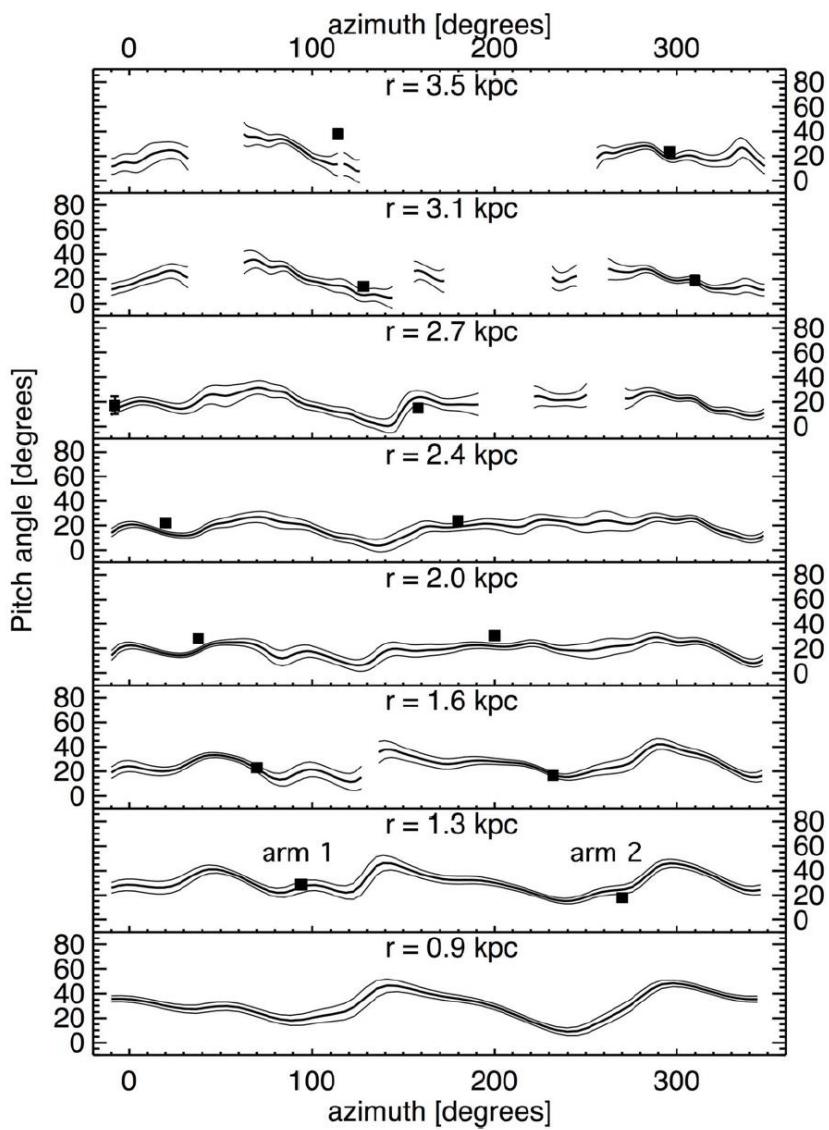
kinematic imprint: $|\Delta V| \text{ } \square \text{ } 20 \text{ km s}^{-1}$



does this affect the B-field?

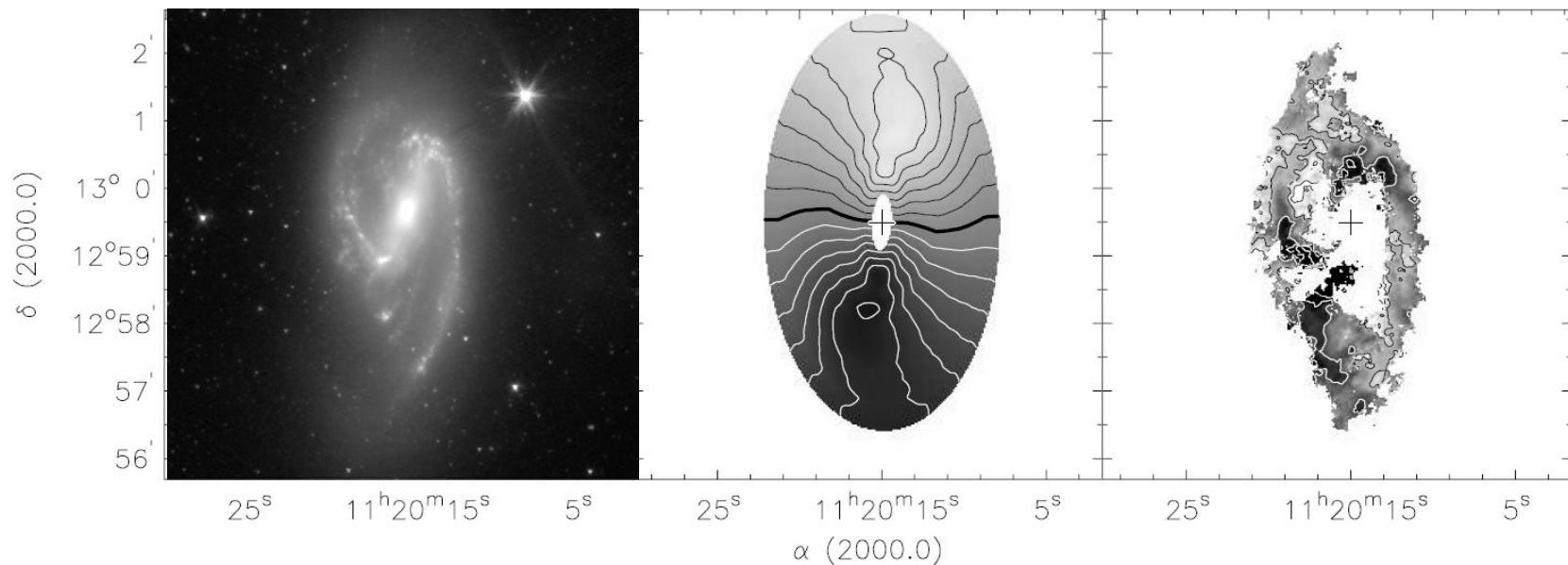
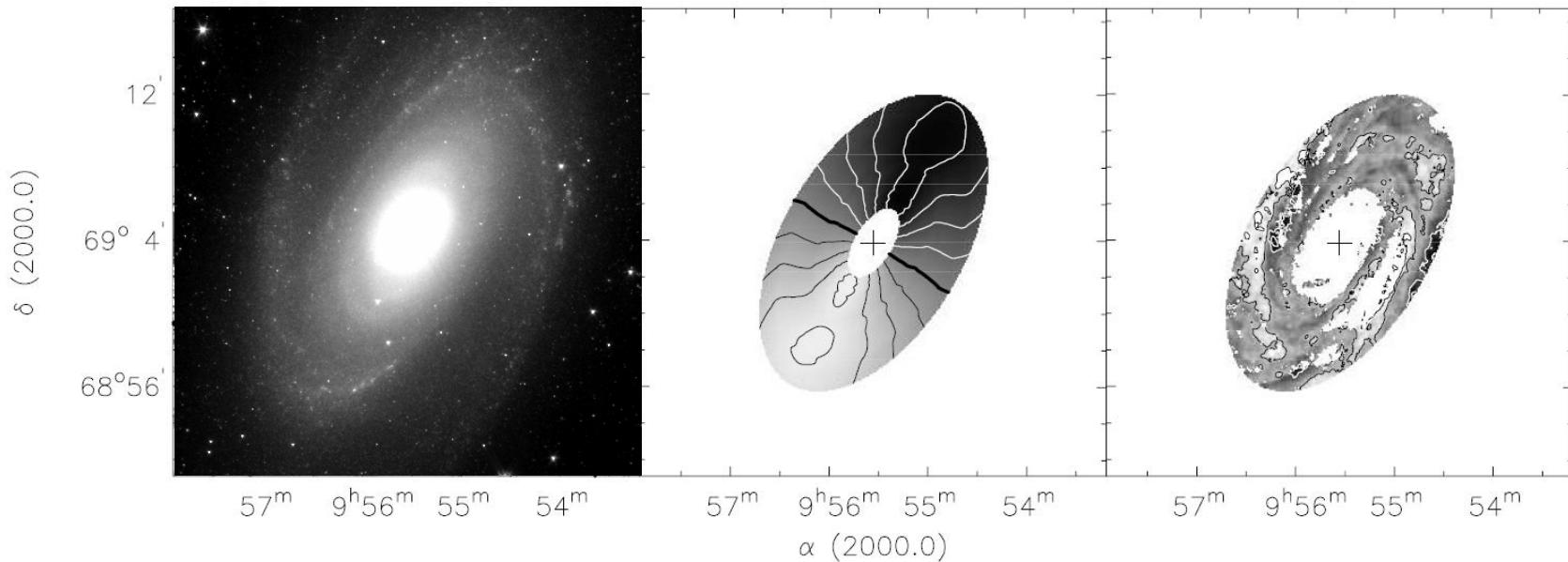


pitch angles of B-field in M 51 (Patrikeev et al. 2006)



⇒ inspect HI data cubes!

de Blok et al. (2008)



construct deprojected velocity vectors from residual velocities and compare with B-field orientation

good candidates:

spirals with pronounced density waves:

M 51, M 81, M 83, NGC 2903

spirals with bars:

NGC 1097, NGC 1365, NGC 3627

THINGS

The HI Nearby
Galaxy Survey

↔
10 kpc



Data: Walter et al 2008

Milky Way HI map: Oort et al (1958)

Milky Way art: NASA/JPL, R. Hurt (SSC)



Ringberg, 19 July 2011



Ringberg, 19 July 2011