

Cosmic Ray acceleration in clusters of galaxies

Gianfranco Brunetti

Istituto di Radioastronomia – INAF, Bologna, ITALY

Outline

NT components (CRe, CRp, B) in galaxy clusters : observations

Physics and dynamics of CR in galaxy clusters

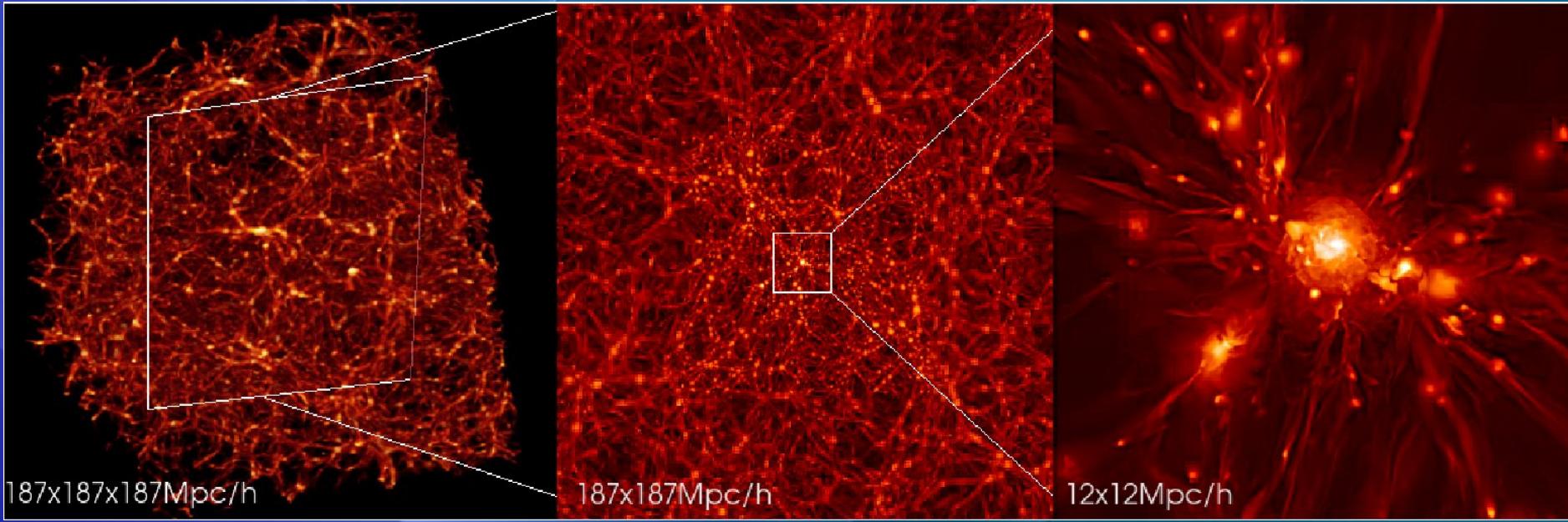
Present constraints on CR protons **new**

Physics of NT Mpc scale diffuse radio emission from
galaxy clusters: Relics & Halos

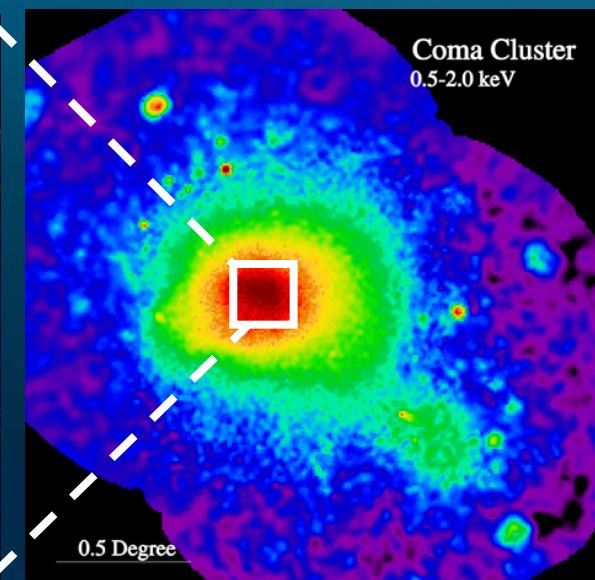
Shocks and turbulent acceleration in clusters

Future at low radio frequencies & gamma rays

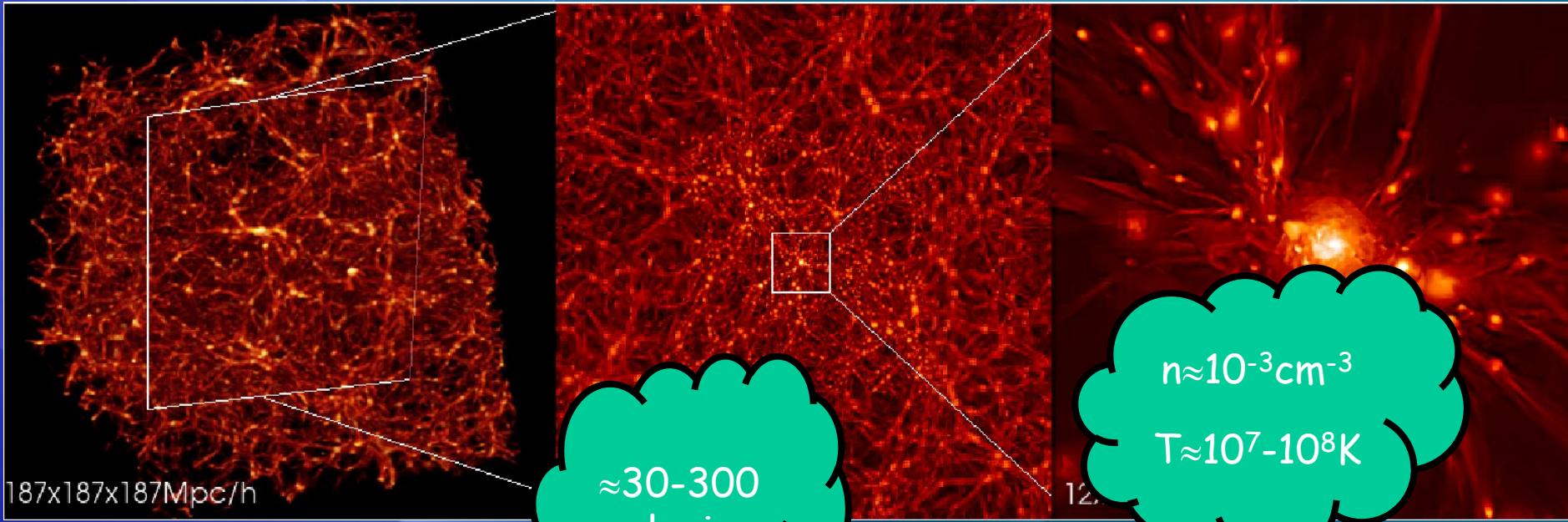
Clusters of galaxies: the largest gravitational structures in the Universe ($M \approx 10^{14}-10^{15} M_{\text{sun}}$, $R_V \approx 2-3 \text{ Mpc}$)



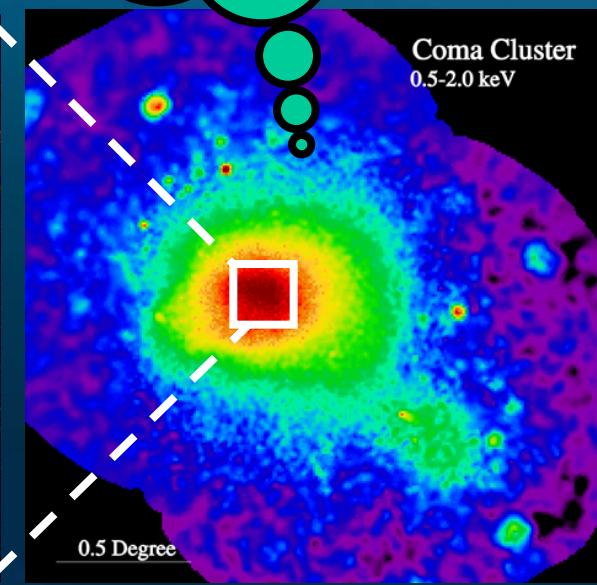
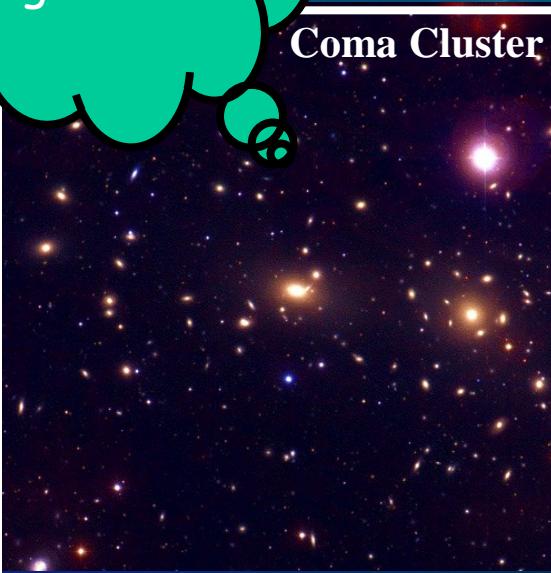
Galaxy cluster mass:
Barions 10% of stars in galaxies
15-20% of hot diffuse gas
Dark Matter 70%



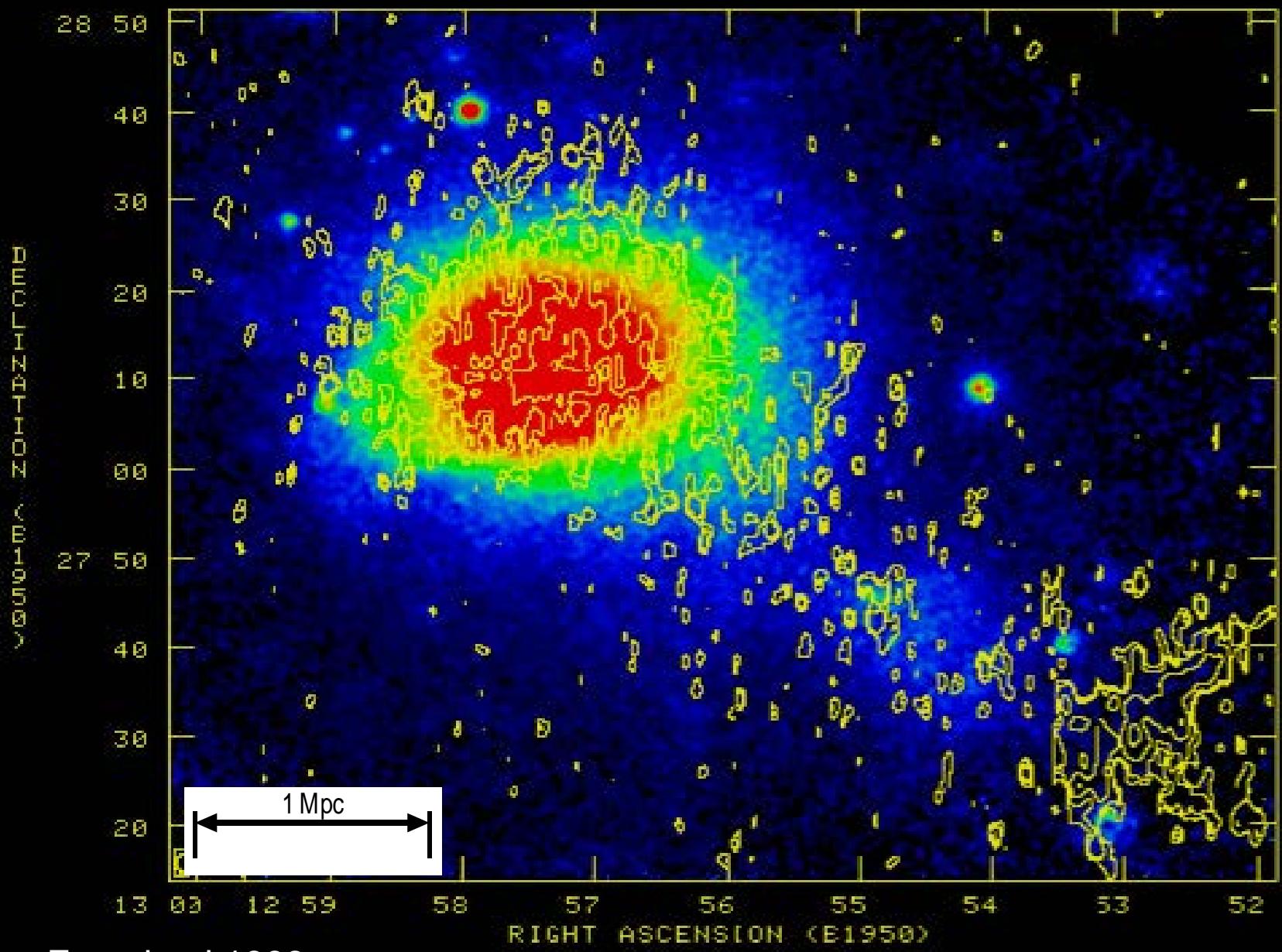
Clusters of galaxies: the largest gravitational structures in the Universe ($M \approx 10^{14}-10^{15} M_{\text{sun}}$, $R_V \approx 2-3 \text{ Mpc}$)



Galaxy cluster mass:
Barions 10% of stars in galaxies
15-20% of hot diffuse gas
Dark Matter 70%

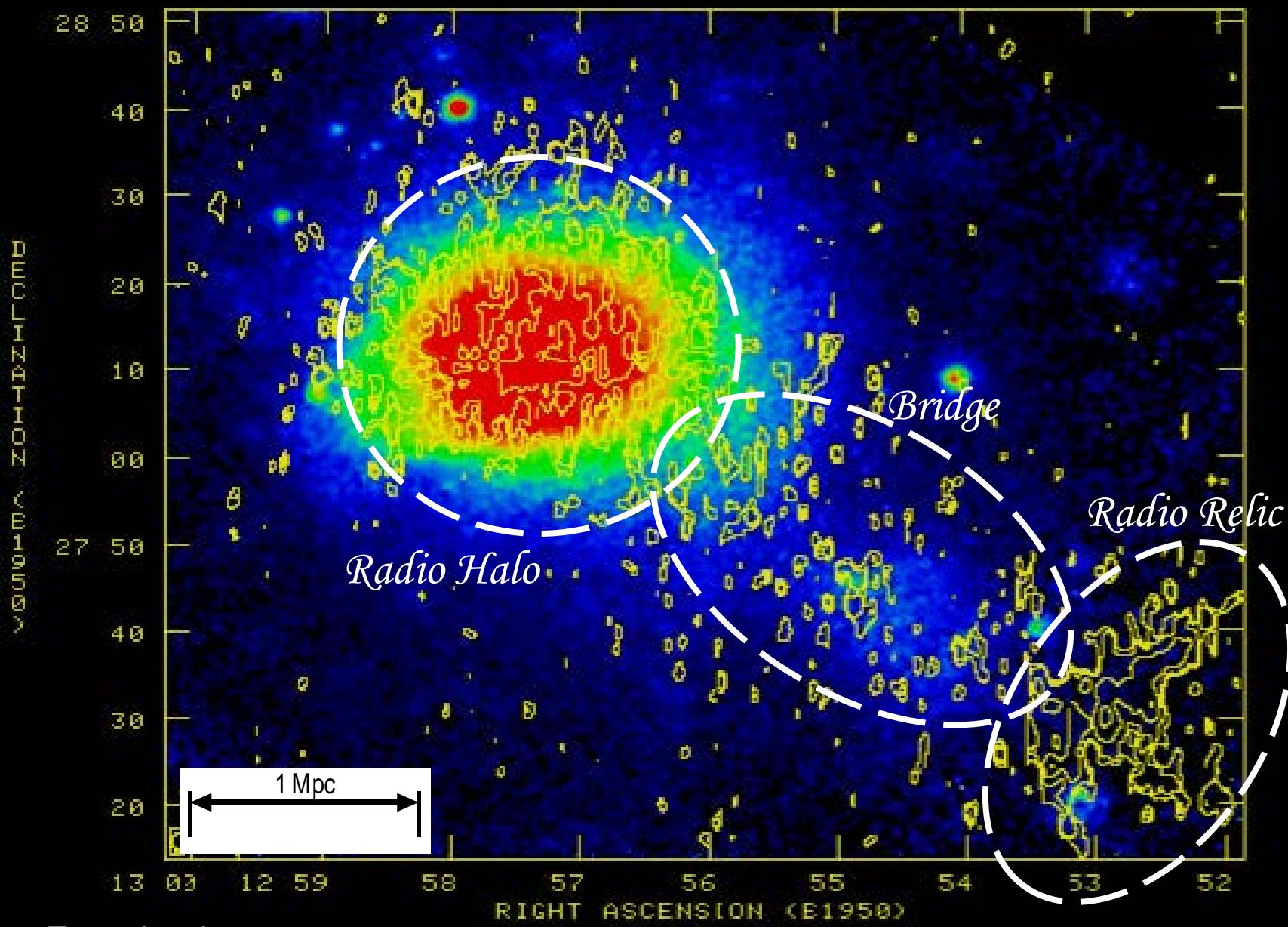


Coma Cluster



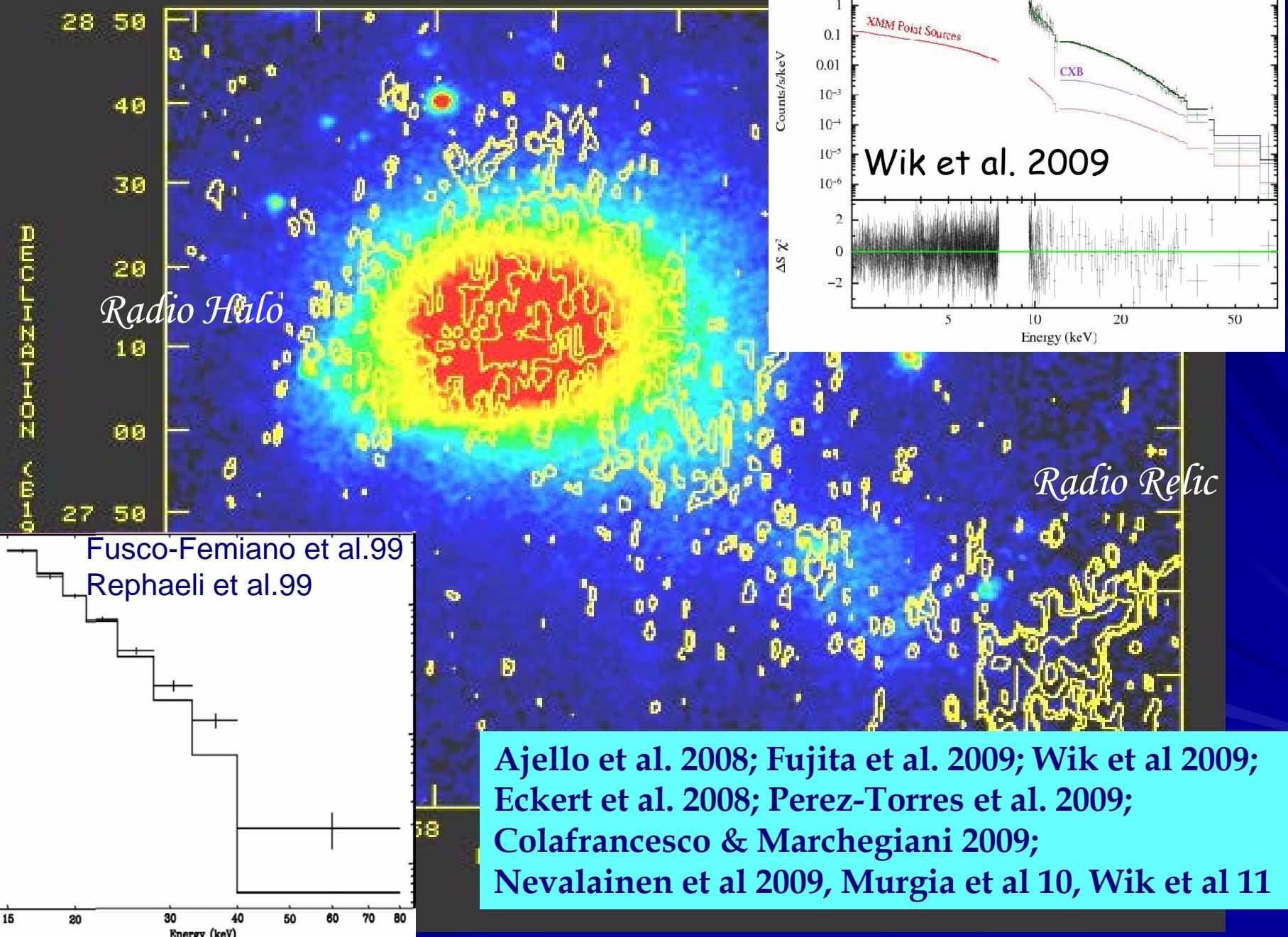
Feretti +al.1998

Coma Cluster

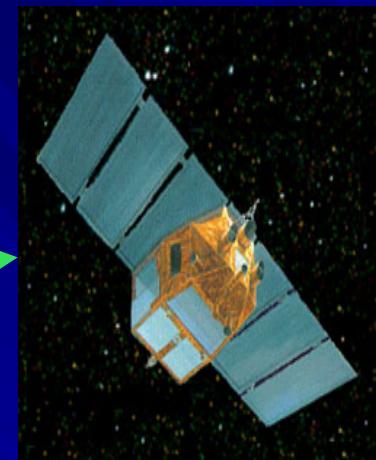
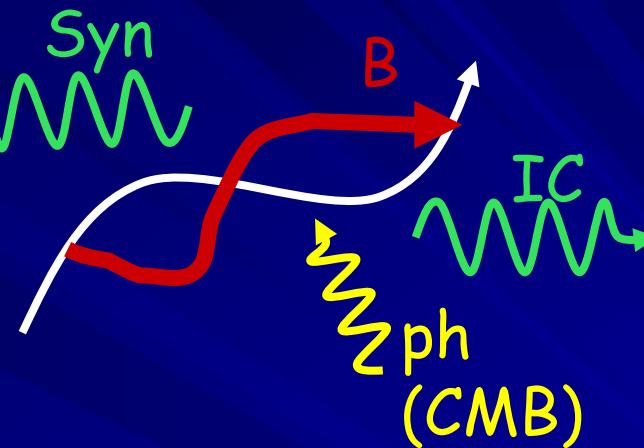
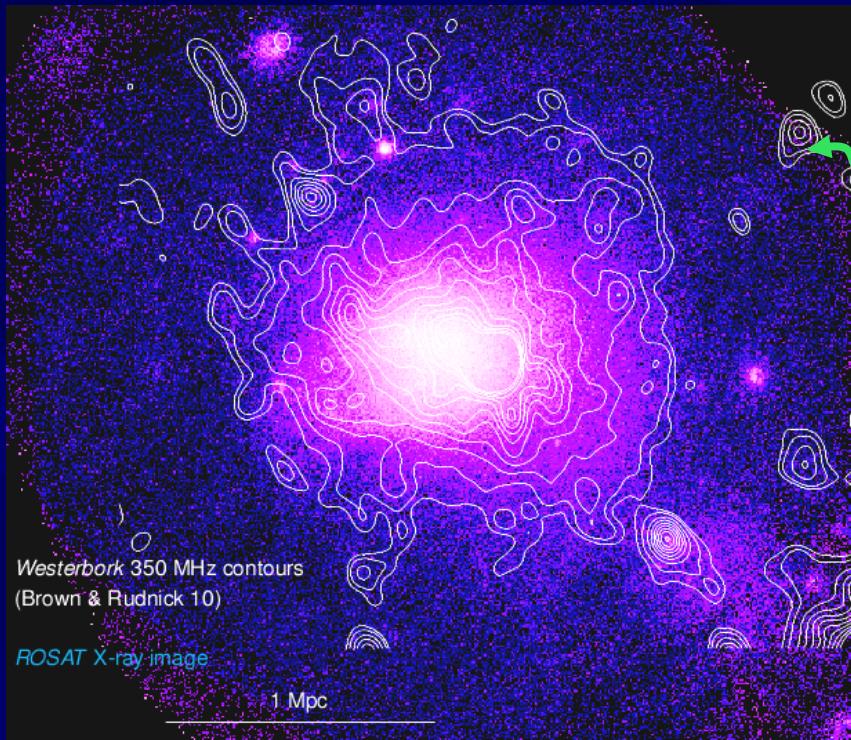


Feretti +al.1998

Coma Cluster: high energy NT



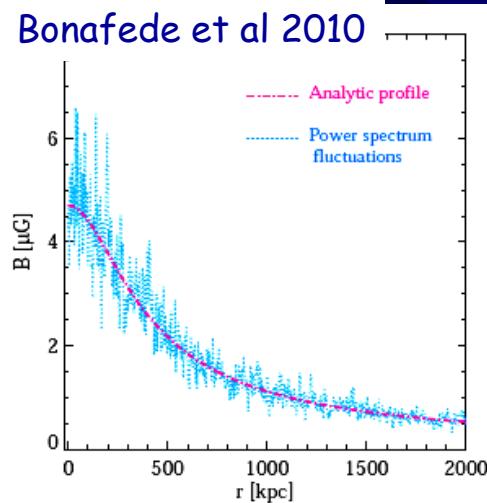
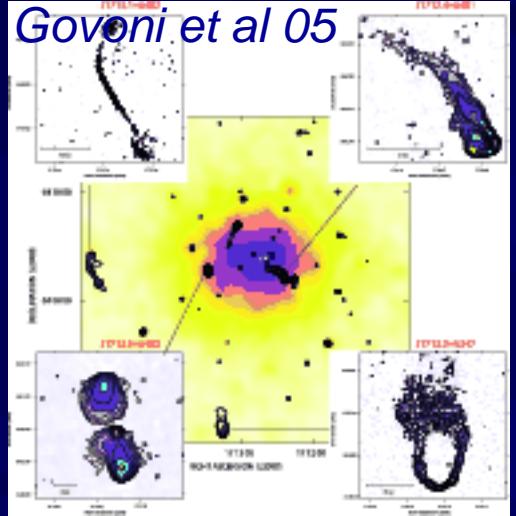
Inverse Compton Emission from GC ??



$$L_{\text{rad}} \rightarrow (U_e, U_B) \rightarrow K_e B^2$$

$$L_{\text{HE}} \rightarrow (U_e, U_{\text{ph}}) \rightarrow K_e U_{\text{ph}}$$

$$L_{\text{rad}} / L_{\text{HE}} \approx U_B / U_{\text{ph}} \rightarrow B \quad \Rightarrow \quad B > 0.1-0.2 \mu G$$



B in Galaxy Clusters

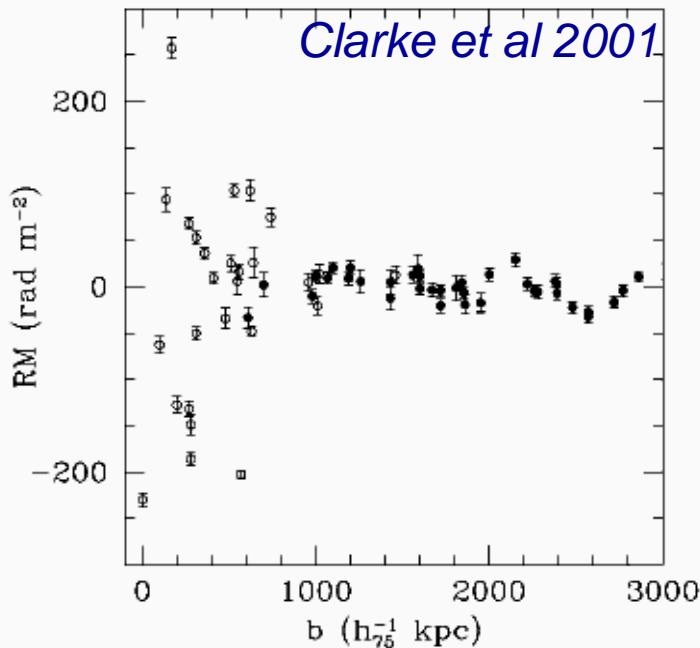
(also Bruggen,Dolag,Neronov lectures)

$B \approx \text{few } \mu\text{G}$

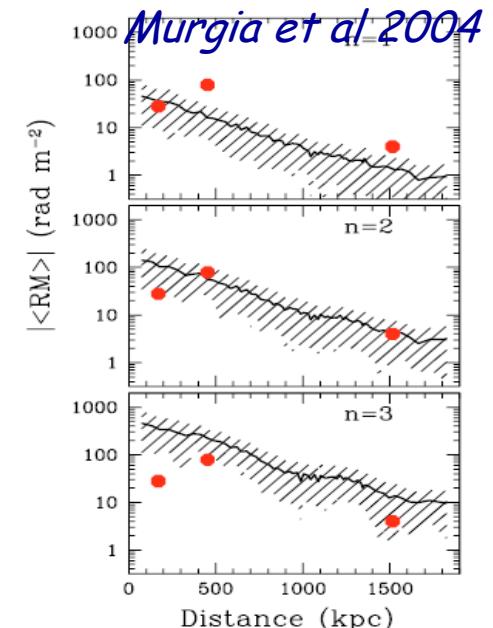
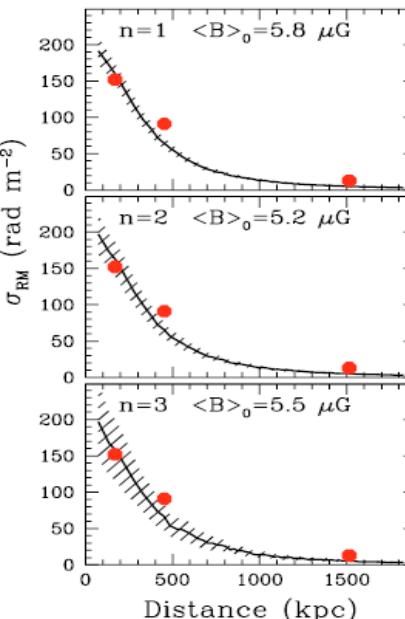
$\Lambda c \approx \text{few-50 kpc}$

RM probe turbulent motions
in the IGM

$$\text{RM} = \frac{\Delta\chi}{\Delta\lambda^2} = 811.9 \int_0^L n_e B_{\parallel} d\ell \text{ rad m}^{-2},$$



$$\sigma_{RM}^2 = \langle \text{RM}^2 \rangle = 812^2 \Lambda_c \int (n_e B_{\parallel})^2 dl .$$



Injection & Dynamics of CR in GC

Cosmological Shocks

(e.g. Sarazin 1999, Miniati et al. 2001, Blasi 2001,
Gabici & Blasi 2003, Ryu et al. 2003, Pfrommer et al. 2006, 2008,
Hoeft & Bruggen 2007, Skillman et al. 2008,
Vazza, Brunetti, Gheller 2009, 2010, etc..)

AGN, Galactic Winds

(e.g. Ensslin et al. 1998; Voelk & Atoyan 1999)

Reconnection (turbulent .. Lazarian & Vishniac 99)

(e.g. Brunetti & Lazarian 2011, DeGouveia dal Pino et al 2011,..)

Physics of CR Leptons

$(dE/dt) / m_e c^2 = b = \text{rate of energy losses in units of } m_e c^2$

$$b_{\text{IC}}(\gamma) = \frac{4}{3} \frac{\sigma_T}{m_e c} \gamma^2 U_{\text{CMB}} = 1.37 \times 10^{-20} \gamma^2 (1+z)^4 \text{ s}^{-1},$$

$$b_{\text{syn}}(\gamma) = \frac{4}{3} \frac{\sigma_T}{m_e c} \gamma^2 U_B = 1.30 \times 10^{-21} \gamma^2 \left(\frac{B}{1 \mu\text{G}} \right)^2 \text{ s}^{-1},$$

Photon
Collisions

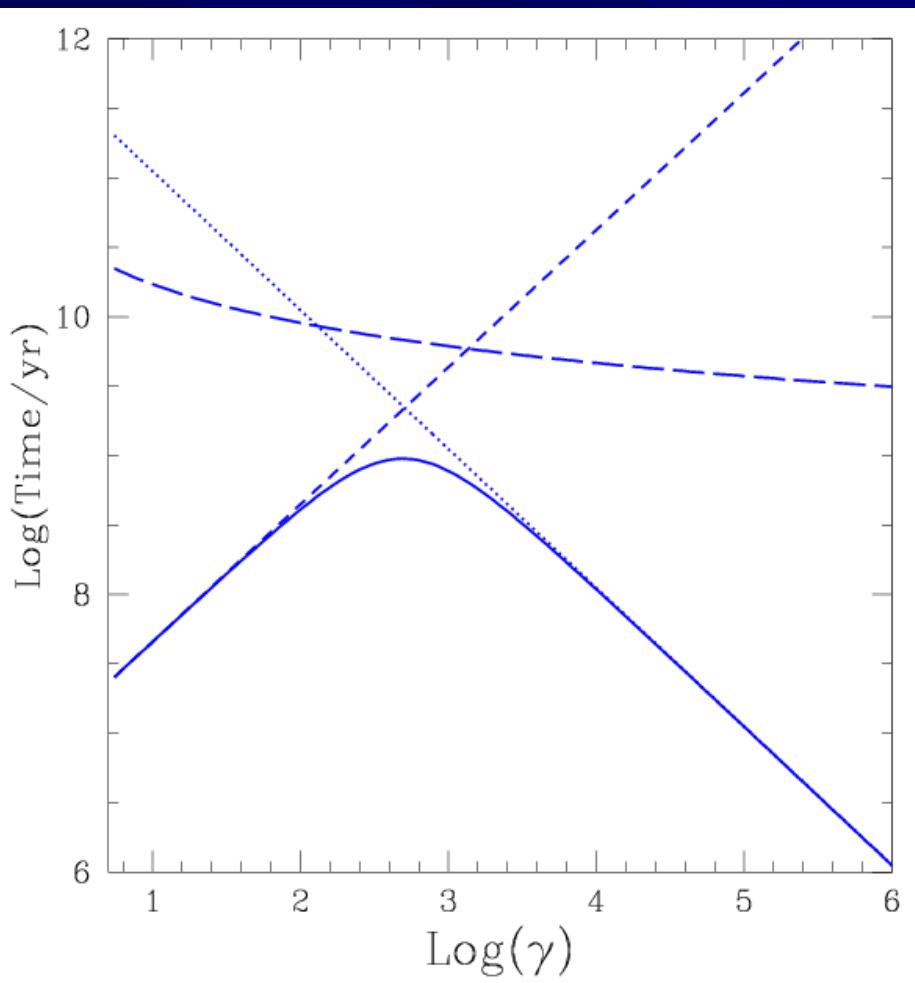
Particle
Collisions

$$b_{\text{Coul}}(\gamma) \approx 1.2 \times 10^{-12} n_e \left[1.0 + \frac{\ln (\gamma/n_e)}{75} \right] \text{ s}^{-1},$$

$$b_{\text{brem}}(\gamma) \approx 1.51 \times 10^{-16} n_e \gamma [\ln (\gamma) + 0.36] \text{ s}^{-1},$$

Physics of CR Leptons

$$(dE/dt) \sim E / \text{Time} \sim m_e c^2 b$$



$$\begin{aligned}\tau_e(\text{Gyr}) \sim 4 \times & \left\{ \frac{1}{3} \left(\frac{\gamma}{300} \right) \left[\left(\frac{B_{\mu G}}{3.2} \right)^2 \frac{\sin^2 \theta}{2/3} + (1+z)^4 \right] \right. \\ & \left. + \left(\frac{n_{\text{th}}}{10^{-3}} \right) \left(\frac{\gamma}{300} \right)^{-1} \left[1.2 + \frac{1}{75} \ln \left(\frac{\gamma/300}{n_{\text{th}}/10^{-3}} \right) \right] \right\}^{-1}.\end{aligned}$$

The life-time of electrons depends on quantities that can be measured

Physics of CR Hadrons

CR protons more energetics than thermal electrons: Coulomb scattering

$$\beta_c \equiv (3/2m_e/m_p)^{1/2} \beta_e$$

$$\frac{dp}{dt} \simeq -1.7 \times 10^{-29} \left(\frac{n_{\text{th}}}{10^{-3}} \right) \frac{\beta_p}{x_m^3 + \beta_p^3} \text{ cgs}$$

$$\frac{dp}{dt} \propto \left(\frac{n_{\text{th}}}{10^{-3}} \right) \times \begin{cases} p & \text{for } mc\beta_c < p < mcx_m \\ p^{-2} & \text{for } mcx_m < p \ll mc \\ \text{Const.} & \text{for } p \gg mc \end{cases}$$

$$X_m = \left(\frac{3\sqrt{\pi}}{4} \right)^{1/3} \beta_e$$

like leptons

$$\tau_{pp} = \frac{1}{n_{\text{th}} \sigma_{pp} c} \sim 10^{18} \left(\frac{n_{\text{th}}}{10^{-3}} \right)^{-1} \text{ s.}$$

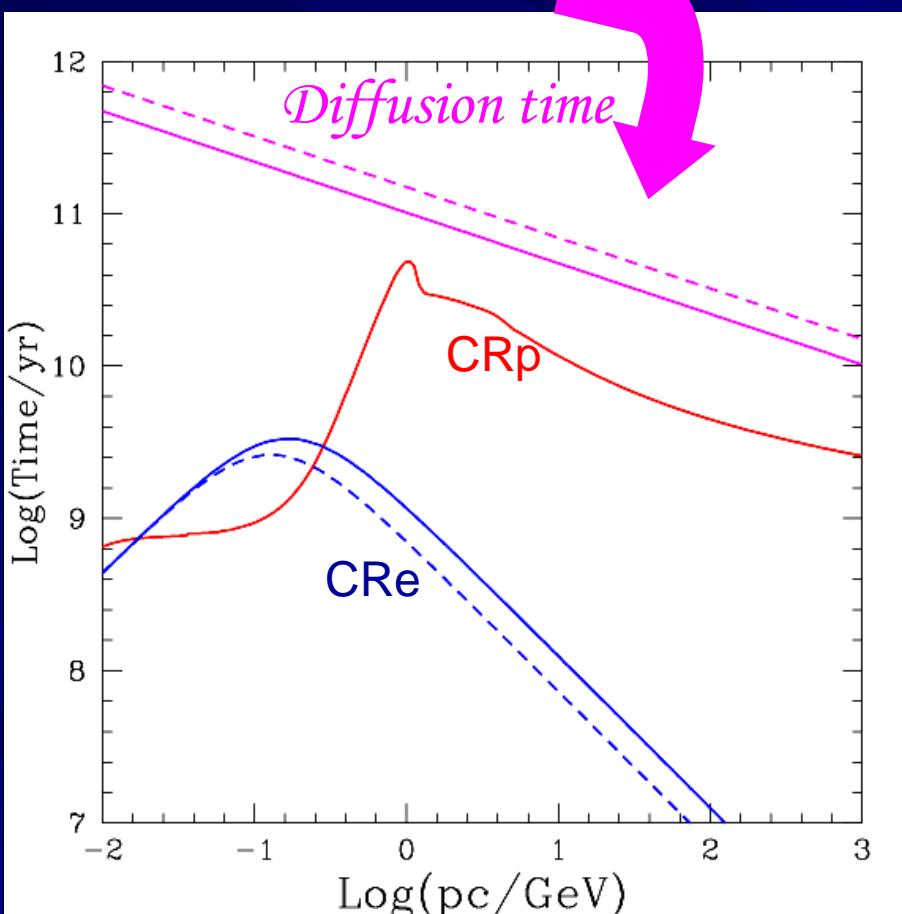
Collisions between CR & thermal protons

~30 Gyrs !

Physics of Cosmic Rays

$$D(E_p) = \frac{1}{3} r_L c \frac{B^2}{\int_{1/r_L}^{\infty} dk P(k)}$$

$D(\text{GeV}) \approx 10^{28}-10^{29} \text{ cm}^2/\text{s} \ll 10^{31} \text{ cm}^2/\text{s}$
(Schlickeiser +al 1987, Blasi+Colafrancesco 1999, GB +al 2011...)



Blasi, Gabici, Brunetti 07

CR are confined in GC

Voelk et al 1996;
Berezinsky, Blasi, Ptuskin 1997; ...

CR protons are long living and accumulated

Voelk et al 1996;
Berezinsky, Blasi, Ptuskin 1997;
Ensslin et al 1998; ...

CR electrons are short living particles and accumulated at $\gamma \approx 100-300$

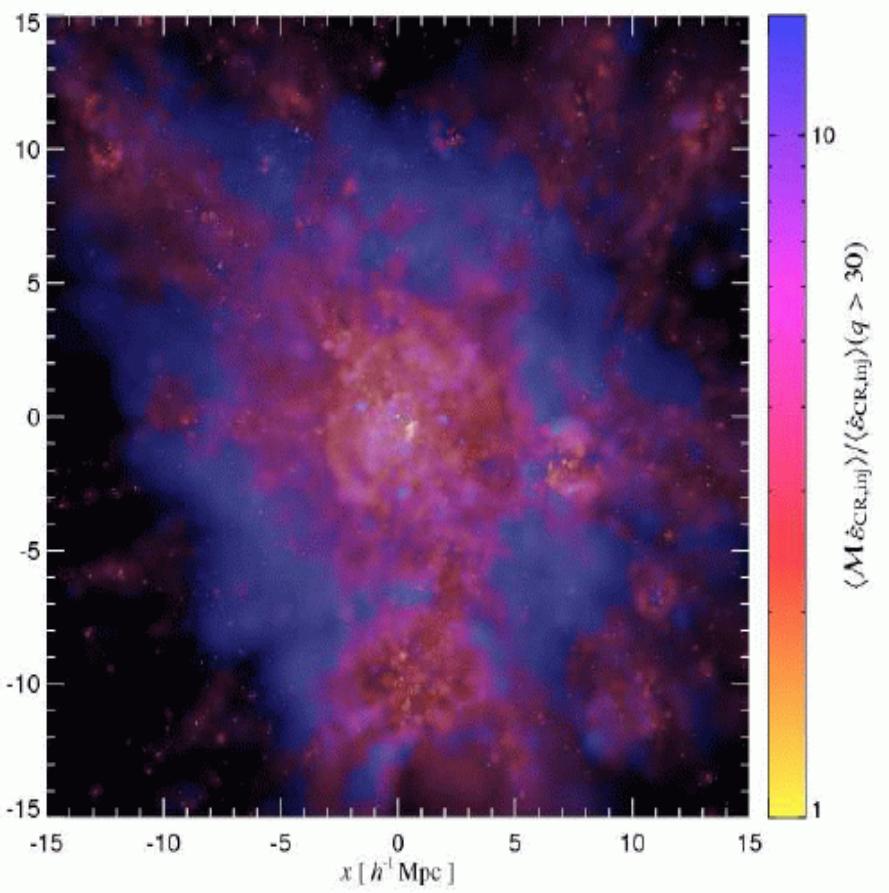
Sarazin 1999; Petrosian 2001; ...

Acceleration & transport of CR : simulations

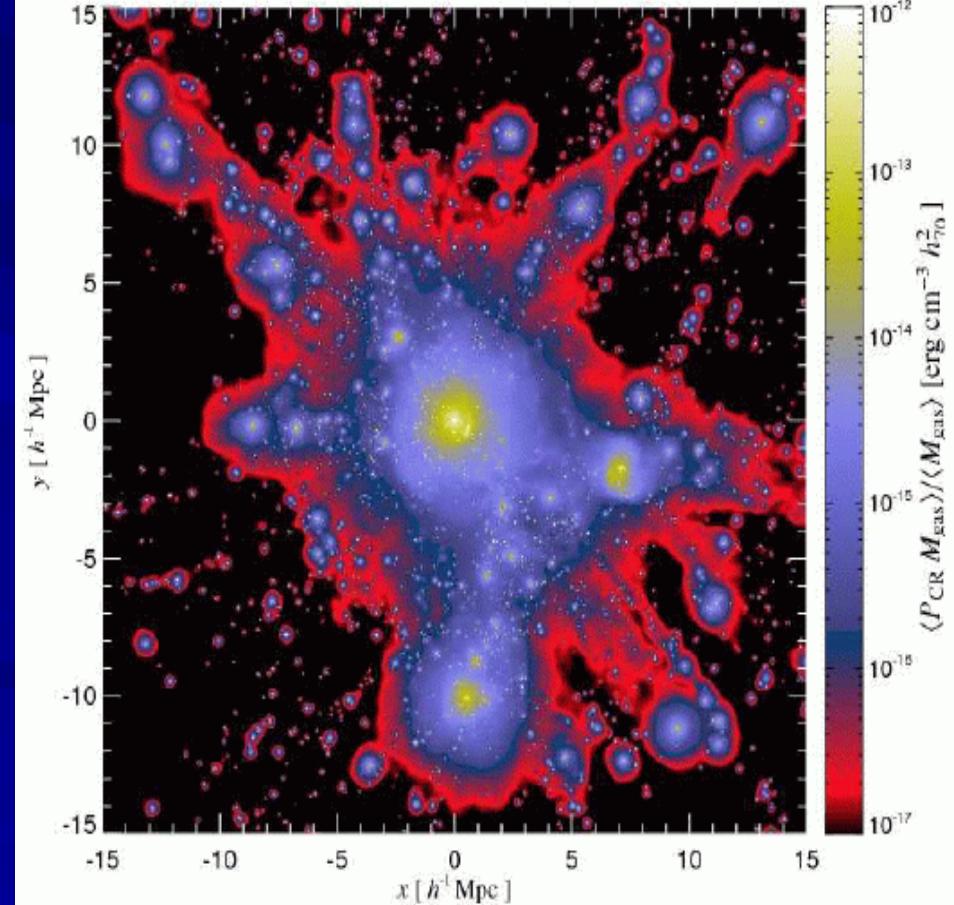
Pfrommer et al. 2007, 08 : simulations of CR+IGM +CR transport/advection

- Acceleration efficiency is the "free" parameter
- Diffusion time \gg advection time

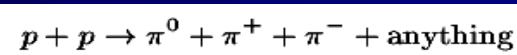
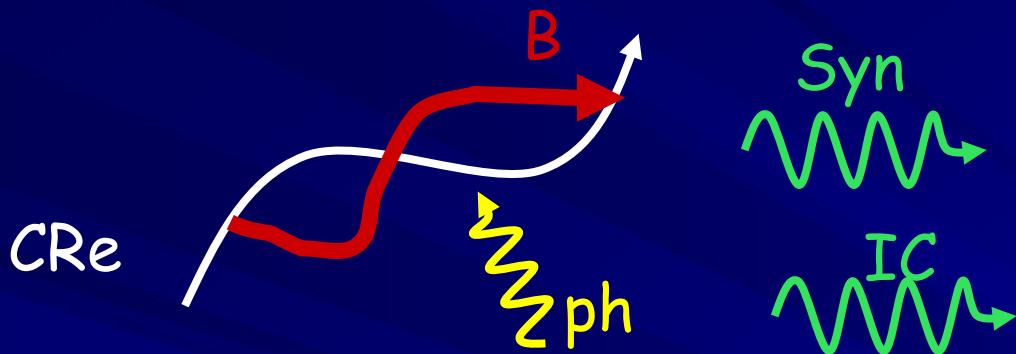
Shock Mach numbers weighted by $\dot{\epsilon}_{\text{CR,inj}}$:



CR proton pressure:

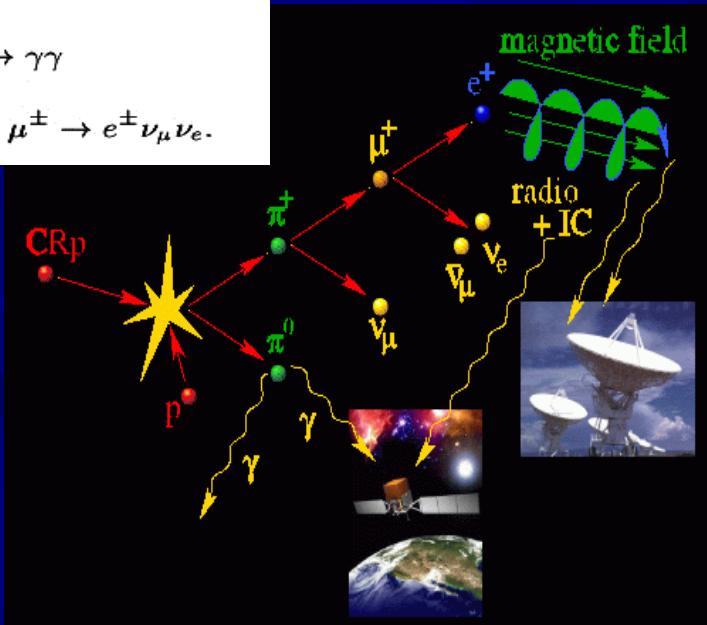


Radiation from Cosmic Rays in GC

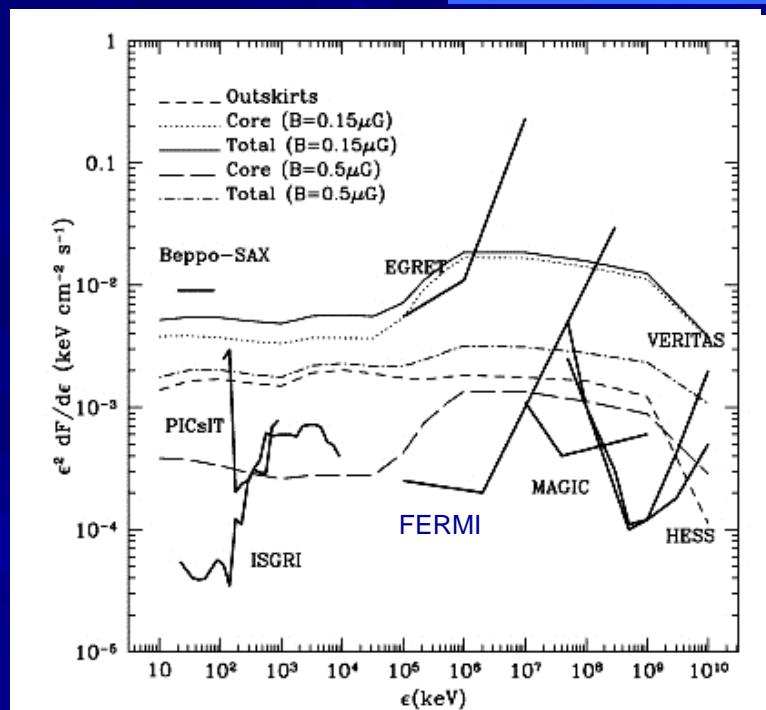


$$\pi^0 \rightarrow \gamma\gamma$$

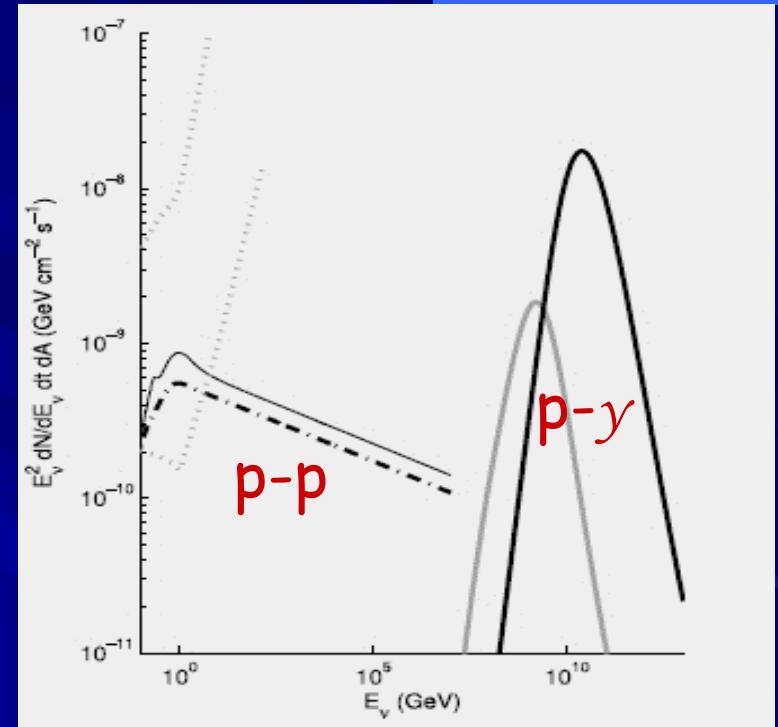
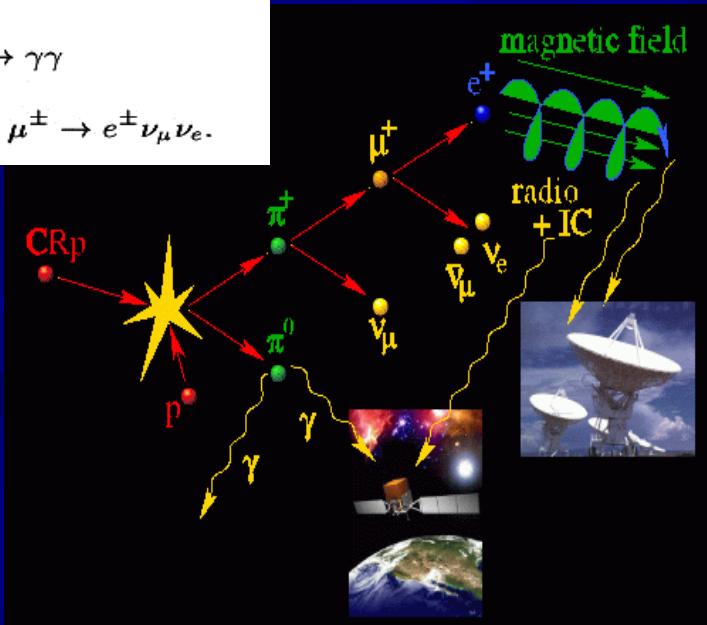
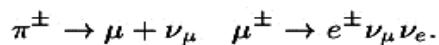
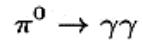
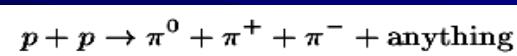
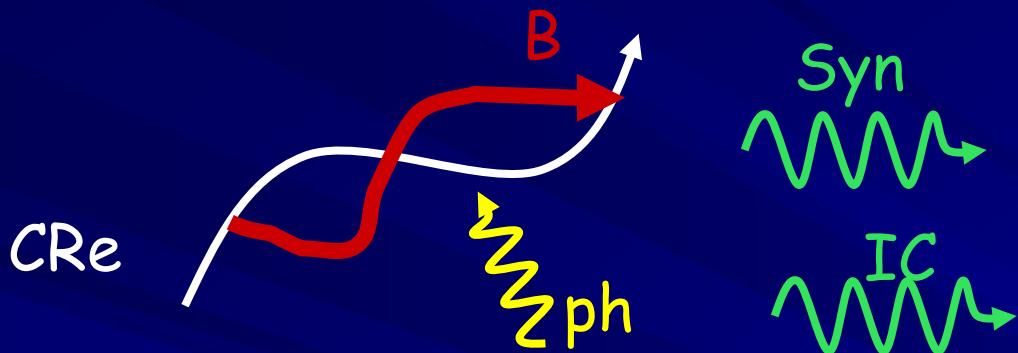
$$\pi^\pm \rightarrow \mu + \nu_\mu \quad \mu^\pm \rightarrow e^\pm \nu_\mu \nu_e.$$



Miniati 2003



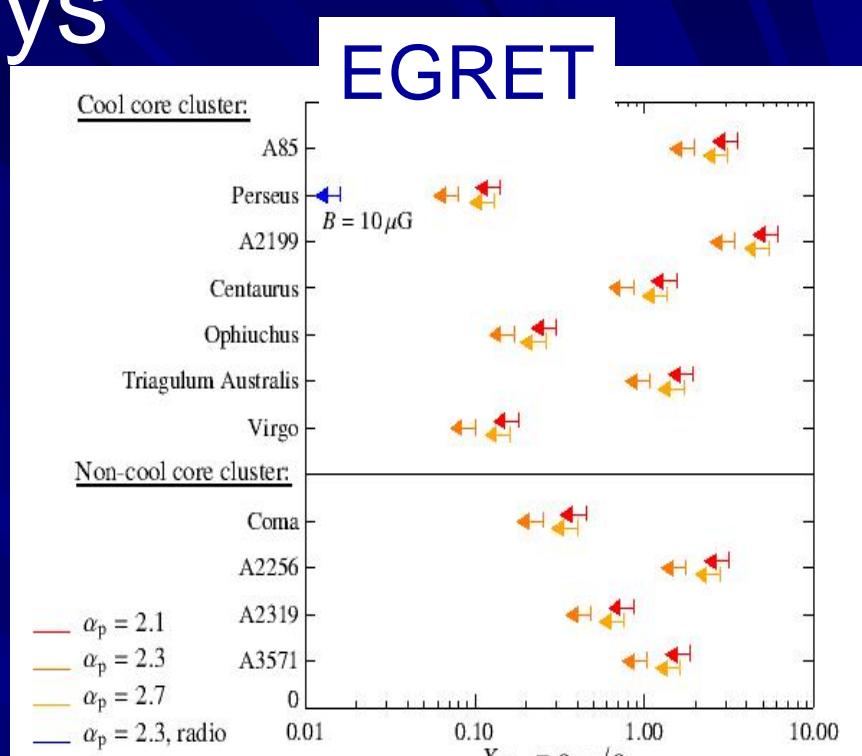
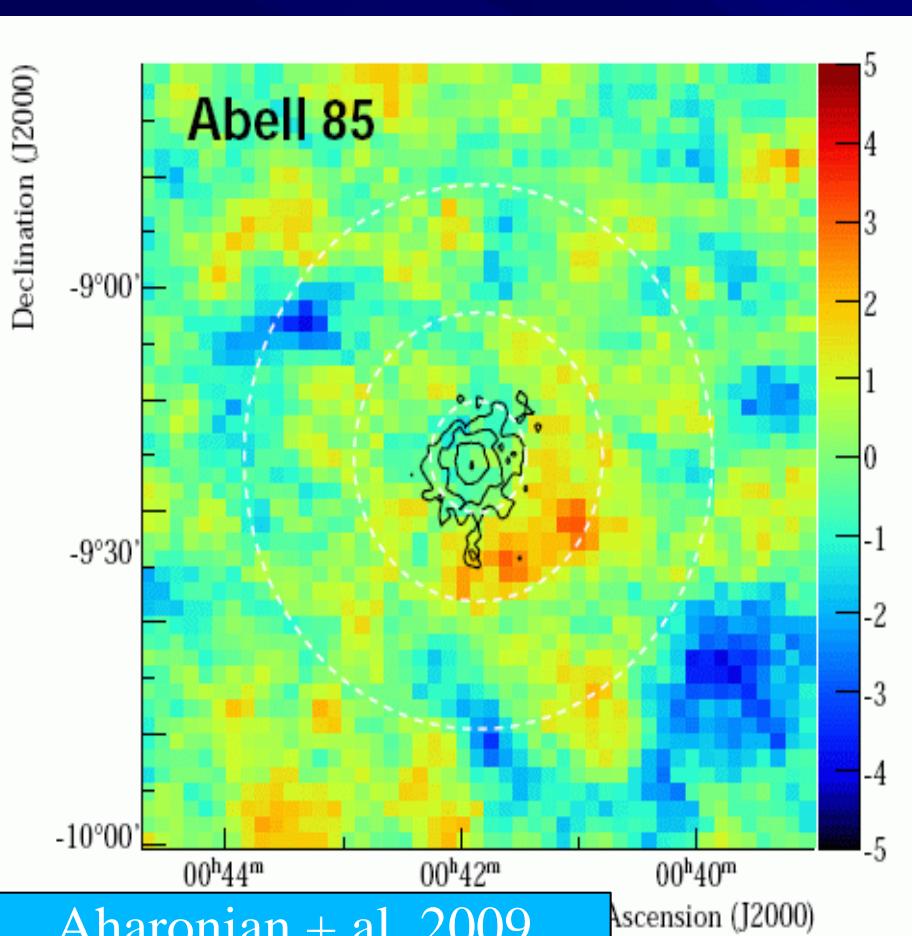
Radiation from Cosmic Rays in GC



Wolfe +al 2008

Limits from gamma rays

$$L_{\gamma,\pi} \sim f(\delta) \langle E_{CR} \rangle \langle E_{th}/T \rangle V_\gamma$$



Reimer +al. 2003; Pfrommer & Ensslin 2004

H.E.S.S.

A 85 : $E_{CR}/E_{th} < 6\text{-}15\%$ (hard spectra)

Coma : $E_{CR}/E_{th} < 12\%$

VERITAS (Perkins +al. 2008)

Coma : $E_{CR}/E_{th} < 5\text{-}10\%$ (hard spectra)

MAGIC (Aleksic +al. 2010)

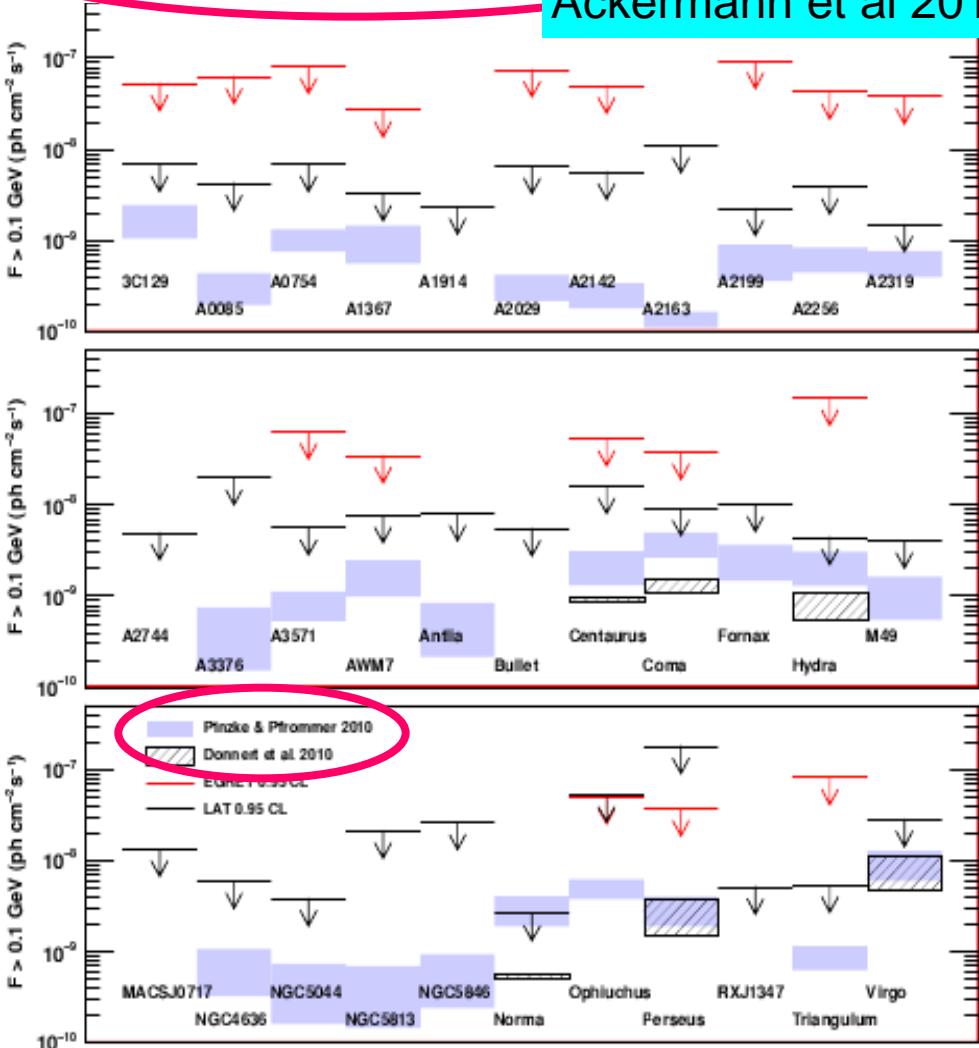
Perseus : $E_{CR}/E_{th} < 4\%$ (hard spectra)

Gamma rays : energy content of CRp

$\langle \epsilon_{CR}/\epsilon_{Th} \rangle$	$\langle \epsilon_{CR}/\epsilon_{Th} \rangle$	Cluster	Spatial Model (R_{50})	f_{IR}	N	$\langle \epsilon_y F(\epsilon_y) \rangle$	$\langle \epsilon_y F(\epsilon_y) \rangle$
$\alpha_p = 2.1$	$\alpha_p = 2.4$				0.2–100	0.2–100	0.2–1
0.16	0.12	3C129	King	0.56	3.93	1.26	1.84
0.06	0.04	A0085	King	0.46	2.23	0.71	1.17
0.35	0.27	A0754	King	0.54	3.31	1.06	1.65
0.26	0.16	A1367	King	0.48	1.83	0.59	1.03†
0.38	0.24	A1914	King	0.54	1.18	0.38†	0.72
0.11	0.09	A2029	King	0.49	3.18	1.02	1.72
0.07	0.05	A2142	King	0.52	2.75	0.88	1.59
0.81	0.61	A2163	King	0.54	5.50	1.76†	2.32
0.14	0.11	A2199	King	0.51	1.18	0.76	...
0.16	0.12	A2256	King	0.47	1.83	0.59	0.81
0.03	0.02	A2319	King	0.54	0.73	0.23†	0.54
1.21	0.95	A3376	King	0.57	9.69	3.11	5.18
0.05	0.04	A3571	King	0.50	3.26	1.04	1.85
1.52	1.19	Antlia	King	0.52	4.84	1.55	2.86
0.10	0.08	AWM7	King	0.55	3.95	1.27	1.92
0.09	0.07	Centaurus	King	0.51	8.15	2.61	3.90
...	...	Coma	Gauss (0.2)	0.53	4.84	1.55	2.28
...	...	Coma	Gauss (0.4)	0.52	4.86	1.56	2.36
...	...	Coma	Gauss (0.6)	0.58	5.12	1.64	2.38
...	...	Coma	Gauss (0.8)	0.56	4.93	1.58	2.73
0.05	0.04	Coma	King	0.55	5.14	1.65	2.18
...	...	Fornax	Gauss (0.2)	0.51	4.77	1.53	2.61
...	...	Fornax	Gauss (0.4)	0.62	5.40	1.73	2.73
...	...	Fornax	Gauss (0.6)	0.59	5.73	1.84	3.02
...	...	Fornax	Gauss (0.8)	0.62	5.39	1.73	2.61
...	...	Fornax	Gauss (1.0)	0.60	5.03	1.61	2.87
0.75	0.59	Fornax	King	0.60	5.64	1.81	2.80
0.28	0.21	Hydra	King	0.60	2.24	0.72†	0.94
5.09	3.98	M49	King	0.52	2.08	0.67	1.14
3.89	3.04	NGC4636	King	0.46	2.67	0.86	1.28
1.58	1.24	NGC5044	King	0.50	1.87	0.60	0.81
25.59	20.03	NGC5813	King	0.52	10.57	3.39	4.25
13.82	10.82	NGC5846	King	0.55	13.01	4.17	5.38
0.03	0.02	Norma	King	0.54	1.21	0.39†	0.94
0.05	0.04	Ophiuchus	King	0.54	26.22	8.41	14.18
0.27	0.22	Perseus	King	0.70	87.36	28.01	28.11
0.07	0.05	Triangulum	King	0.54	2.39	0.77†	0.91
...	...	Virgo	Gauss (0.2)	0.62	14.49	4.65	4.93
...	...	Virgo	Gauss (0.4)	0.61	15.27	4.90	5.26
...	...	Virgo	Gauss (0.6)	0.64	14.97	4.80	5.62
...	...	Virgo	Gauss (0.8)	0.64	15.76	5.05	5.62
...	...	Virgo	Gauss (1.0)	0.66	16.01	5.13	5.71
...	...	Virgo	Gauss (1.2)	0.64	17.03	5.46	5.62
0.17	0.13	Virgo	King	0.61	14.89	4.77	5.24

The constraints on hadronic CR populations derived from LAT data are in agreement with limits placed by indirect methods (Brunetti et al. 2007; Churazov et al. 2008) and with the predictions of theoretical models and numerical simulations pointing out morphological and spectral difficulties (namely, observed radio “pseudo cut-offs”) in explaining large-scale radio halos with purely secondary emission (e.g., Blasi et al. 2005 and references therein; Donnert et al. 2010). For the clusters examined thus far, multiwavelength evidence suggests that secondary electrons play a minor role in NT emission.

Ackermann et al 2010



CRp: limits from Radio

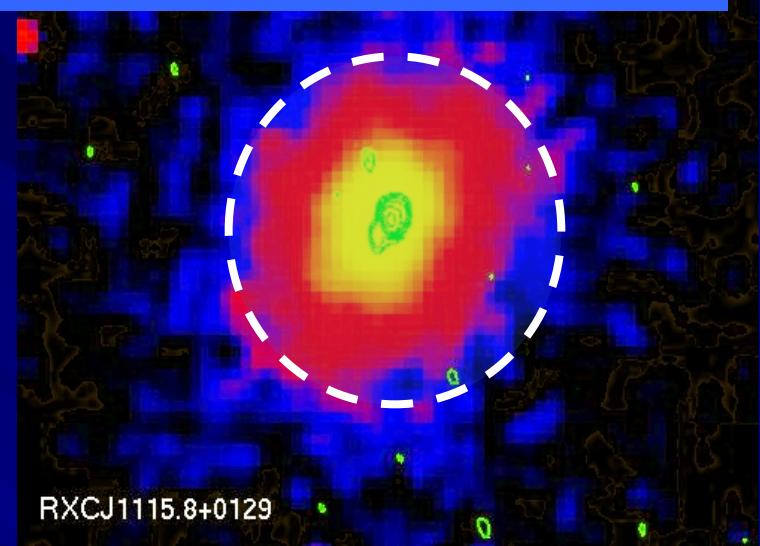
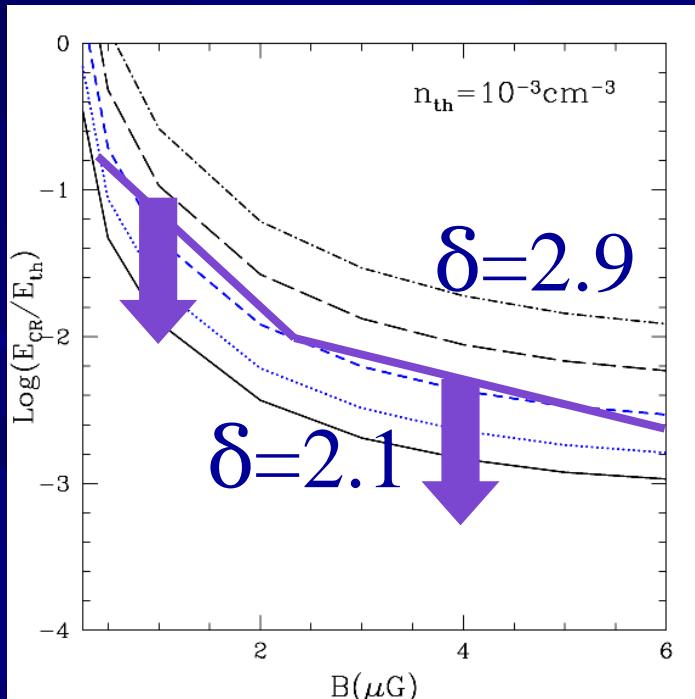
$$p + p \rightarrow \pi^0 + \pi^+ + \pi^- + \text{anything}$$

$$\pi^0 \rightarrow \gamma\gamma$$

$$\pi^\pm \rightarrow \mu + \nu_\mu \quad \mu^\pm \rightarrow e^\pm \nu_\mu \nu_e.$$

$$L_{\gamma,\pi} \sim f_\gamma(\delta) \langle E_{CR} \rangle \langle E_{th}/T \rangle V_\gamma$$

$$L_R \sim f_R(\delta) \langle E_{CR} \rangle \langle E_{th}/T \rangle \langle B^{\delta/2+1}/(B^2+B_{cmb}^2) \rangle V_R$$



Assuming that secondary particles are injected in the IGM, their synchrotron emission should be smaller than upper limits to the diffuse radio emission.

limits on: (B, E_{CRp}) , δ



CRp: limits from Radio

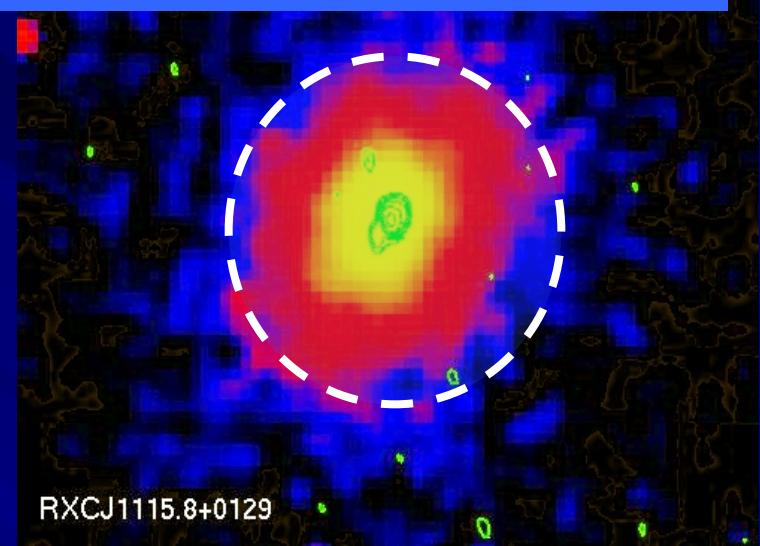
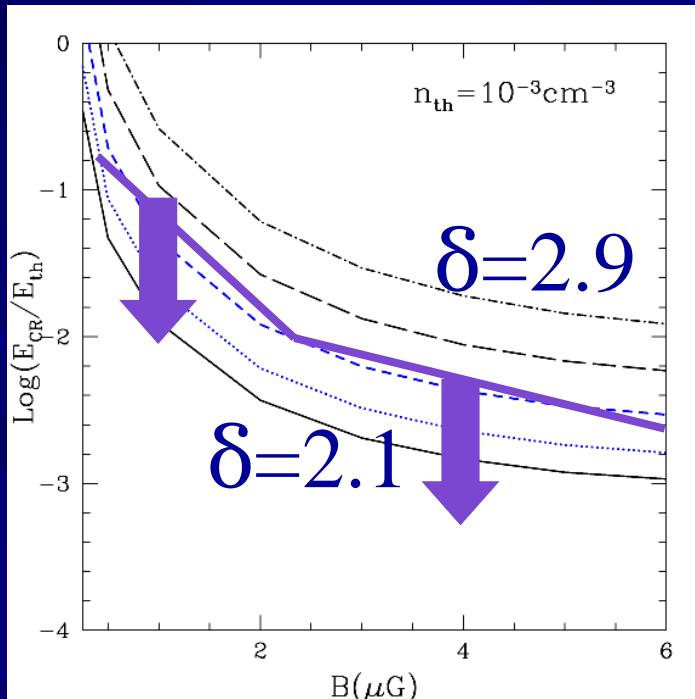
$$p + p \rightarrow \pi^0 + \pi^+ + \pi^- + \text{anything}$$

$$\pi^0 \rightarrow \gamma\gamma$$

$$\pi^\pm \rightarrow \mu + \nu_\mu \quad \mu^\pm \rightarrow e^\pm \nu_\mu \nu_e.$$

$$L_{\gamma,\pi} \sim f_\gamma(\delta) \langle E_{CR} \rangle \langle E_{th}/T \rangle V_\gamma$$

$$L_R \sim f_R(\delta) \langle E_{CR} \rangle \langle E_{th}/T \rangle \langle B^{\delta/2+1}/(B^2+B_{cmb}^2) \rangle V_R$$

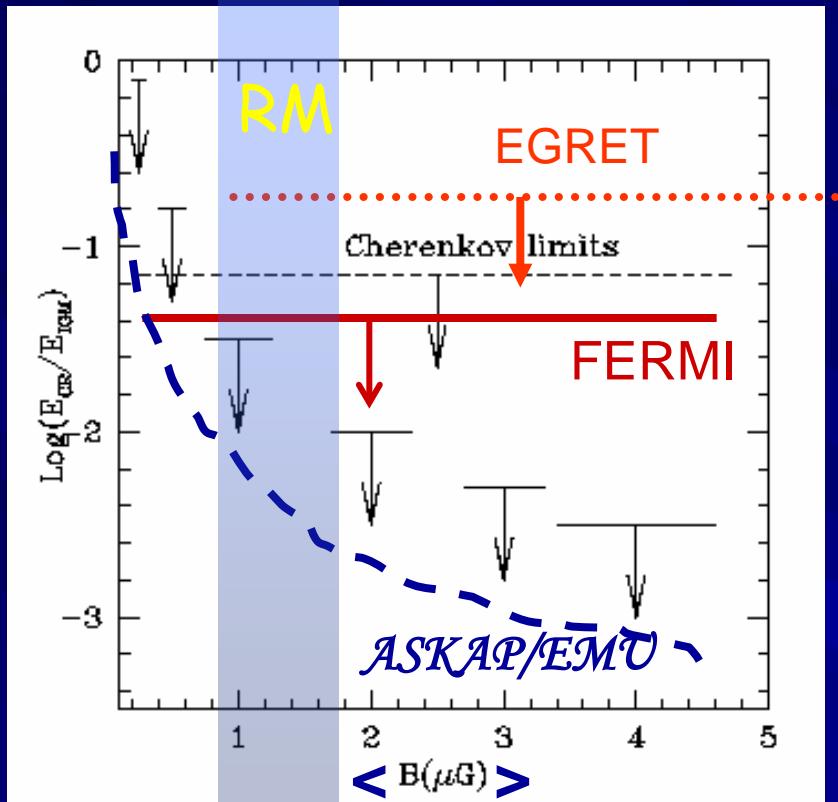


Assuming that secondary particles are injected in the IGM, their synchrotron emission should be smaller than upper limits to the diffuse radio emission.

limits on: (B, E_{CRp}) , δ



Energy content of CRp



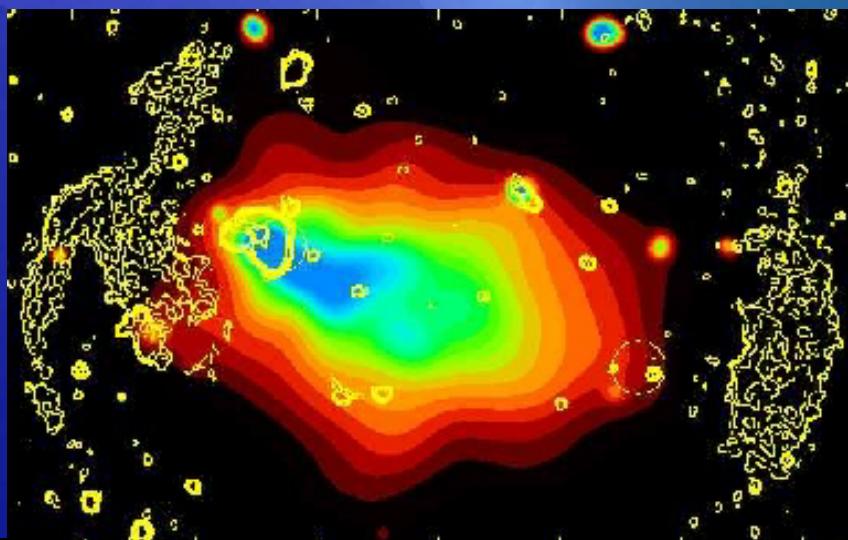
- Reimer et al. (2003)
- Reimer et al. (2004)
- Pfrommer & Ensslin (2004)
- Perkins et al. (2006)
- Brunetti et al. (2007)
- Brunetti et al. (2008)
- Perkins et al. (2008)
- Aharonian et al. (2008 a,b)
- Aleksic et al. (2009)
- Ackermann et al (2010)

Gamma + Radio observations independently suggest that non-thermal components are dynamically NOT important (% level)

Additional limits from cluster dynamics (e.g. Churazov et al. 2008; Lagana et al 2009) constrain $E_{\text{CR}} + E_B + E_{\text{turb}}$ below 10% (< 30%) E_{thermal} .

Non-thermal emission from GC

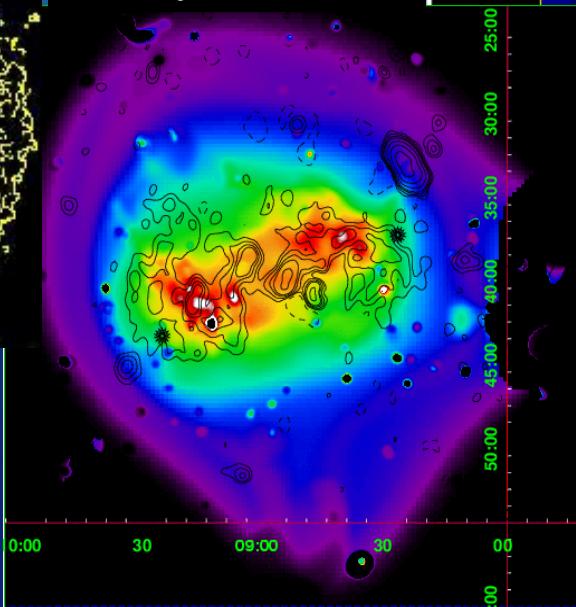
Both **Halos** & **Relics** have **steep spectrum**, $F(v) = F_0 v^{-\alpha}$, with $\alpha \approx 1.3$



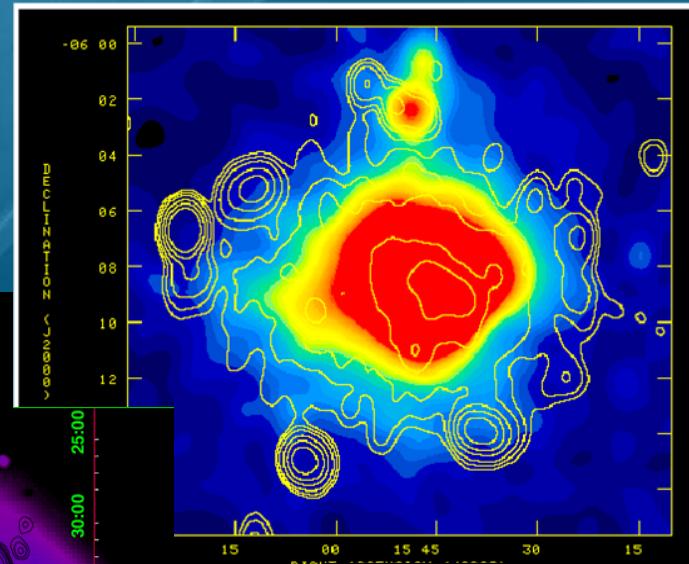
Abell 3376
Bagchi et al. 2005

Radio Relics

Abell 754
Henry et al. 2004



Radio Halos



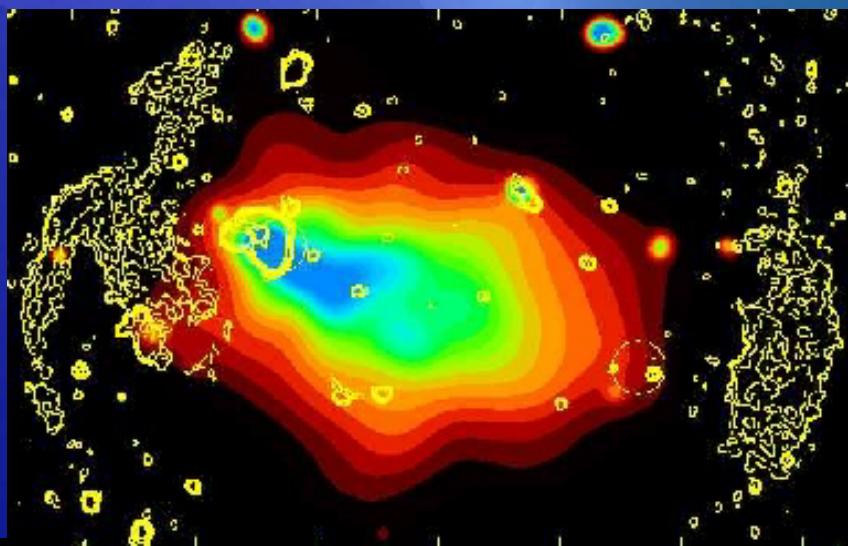
Abell 2163
Feretti et al. 2001

Non-thermal emission from GC

Both **Halos & Relics** have **steep spectrum**, $F(v) = F_0 v^{-\alpha}$, with $\alpha \approx 1.3$

Unpolarised, follow the X-ray brightness
(originate from cluster central regions)

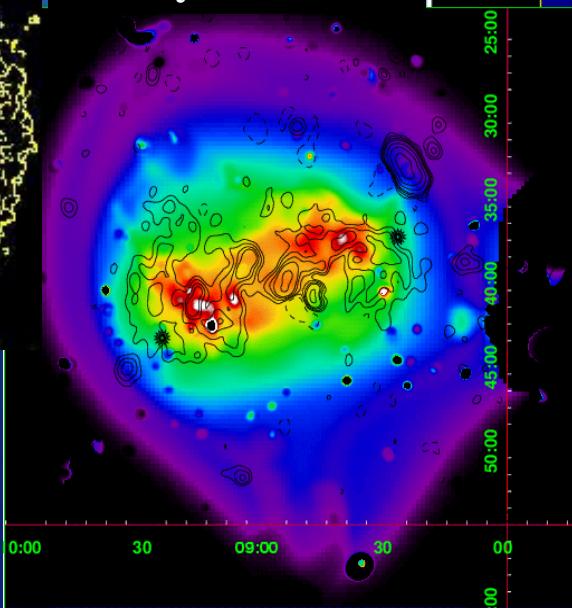
Polarised, no correlation with X-ray brightness
(form in cluster outskirts)



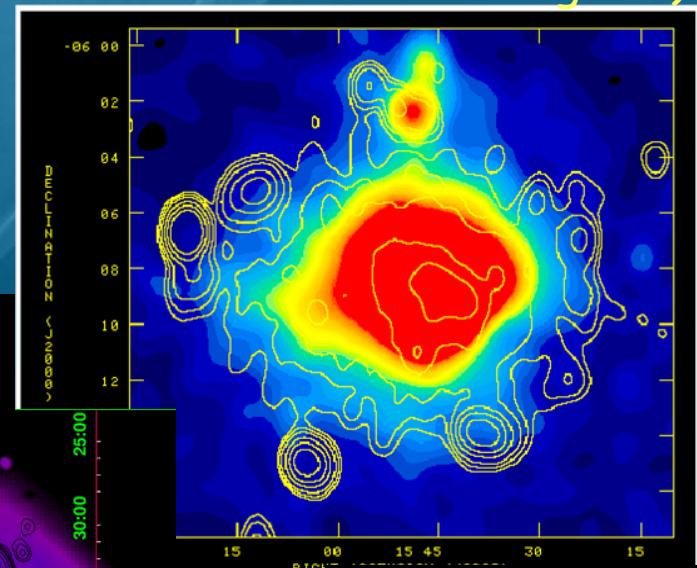
Abell 3376
Bagchi et al. 2005

Radio Relics

Abell 754
Henry et al. 2004



Radio Halos

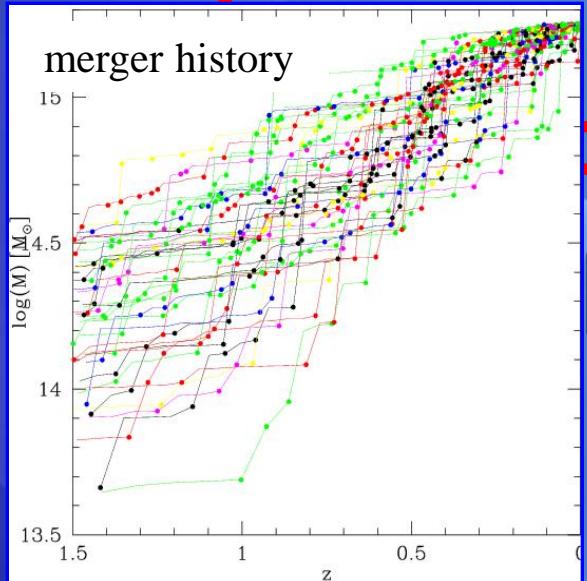


Abell 2163
Feretti et al. 2001

Connecting LSS formation

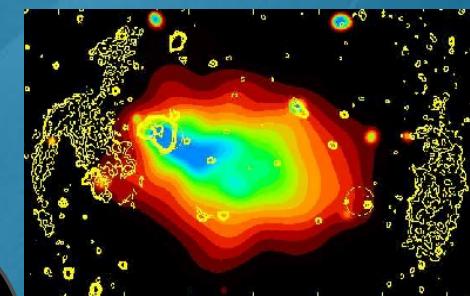
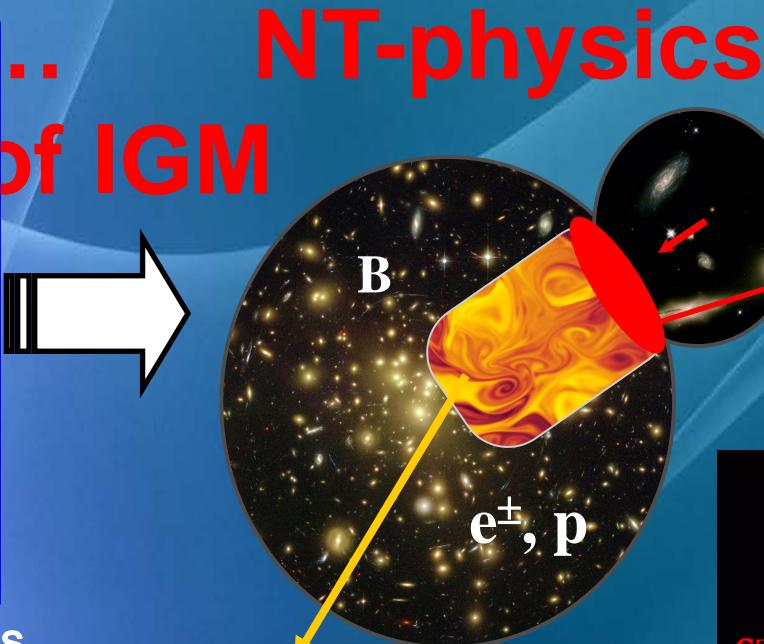
NT-physics

of IGM

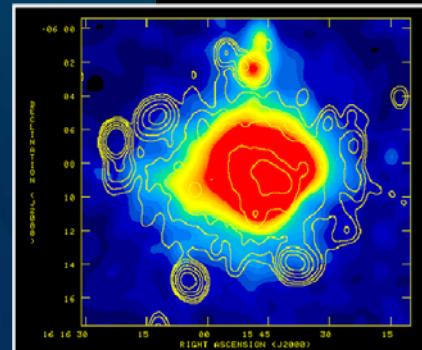
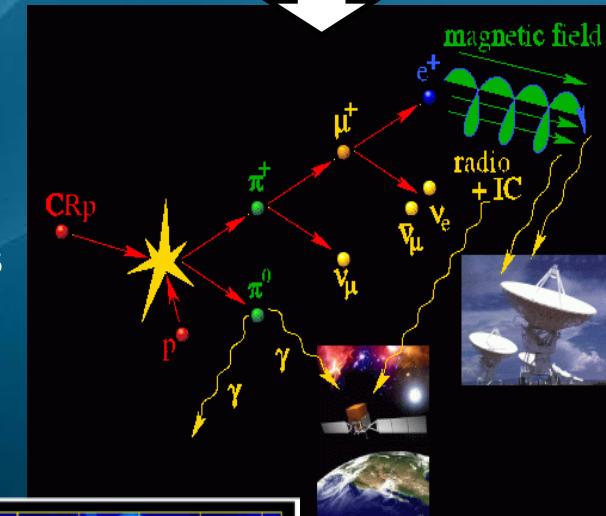


clusters increase their mass
via merger with smaller
subclusters

TURBULENCE reaccelerates
fossil e^\pm and secondaries e^\pm on
Mpc scales



SHOCKS
accelerate e^\pm , p_{cr}



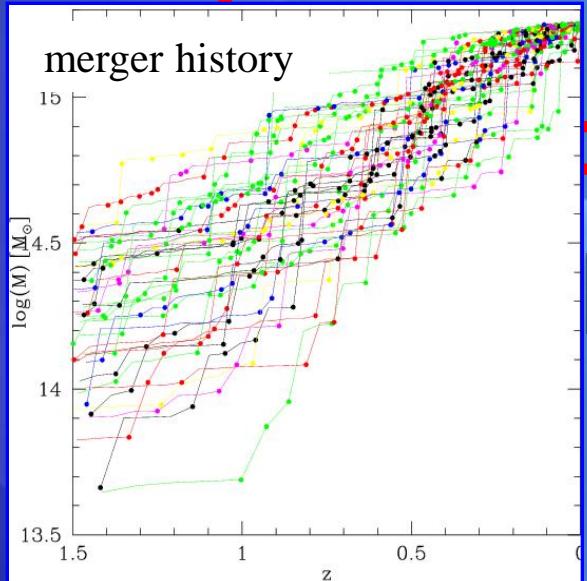
?

(e.g., Brunetti *et al.* 2001, 2004, 2009; Petrosian 2001;
Miniati *et al.* 2001; Fujita *et al.* 2003; Ryu *et al.* 2003;
Gabici & Blasi 2003; Berrington & Dermer 2003;
Pfrommer & Ensslin 2004; Brunetti & Blasi 2005;
Cassano & Brunetti 2005; Cassano *et al.* 2006;
Brunetti & Lazarian 2007; Hoeft & Bruggen 2007;
Pfrommer *et al.* 2008; Petrosian & Bykov 2008, ...)

Connecting LSS formation

NT-physics

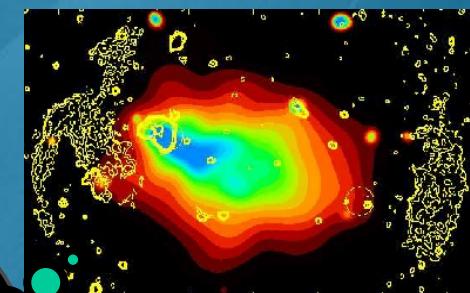
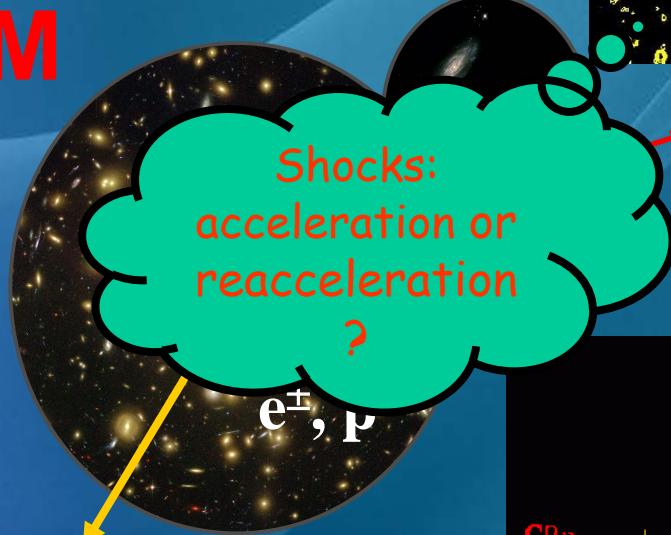
of IGM



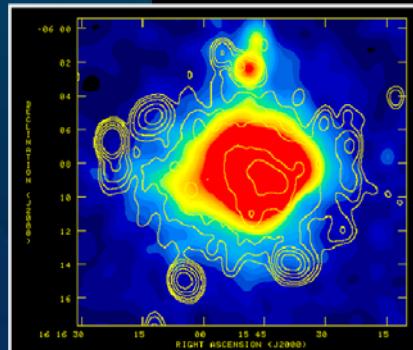
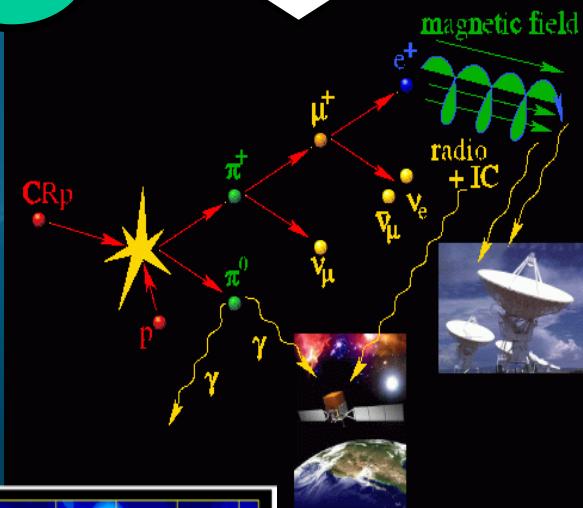
clusters increase their mass
via merger with smaller
subclusters

TURBULENCE reaccelerates
fossil e^\pm and secondaries e^\pm on
Mpc scales

... NT-physics



SHOCKS
accelerate e^\pm , p_{cr}



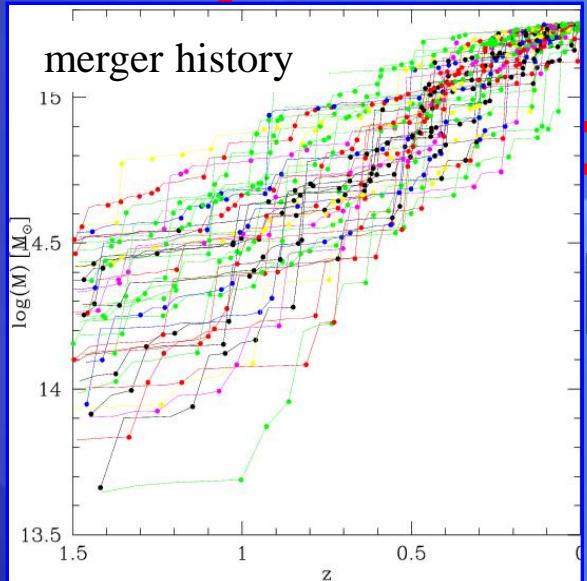
?

(e.g., Brunetti *et al.* 2001, 2004, 2009; Petrosian 2001;
Miniati *et al.* 2001; Fujita *et al.* 2003; Ryu *et al.* 2003;
Gabici & Blasi 2003; Berrington & Dermer 2003;
Pfrommer & Ensslin 2004; Brunetti & Blasi 2005;
Cassano & Brunetti 2005; Cassano *et al.* 2006;
Brunetti & Lazarian 2007; Hoeft & Bruggen 2007;
Pfrommer *et al.* 2008; Petrosian & Bykov 2008,...)

Connecting LSS formation

NT-physics

of IGM

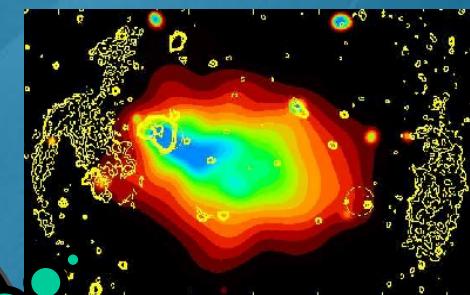
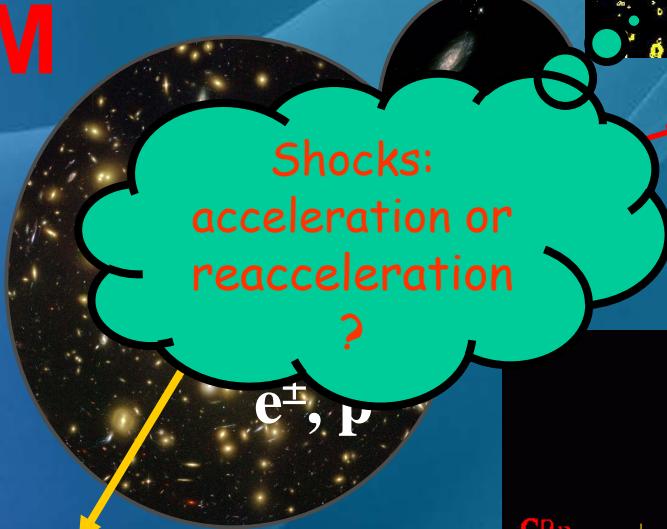


clusters increase their mass
via merger with smaller
subclusters

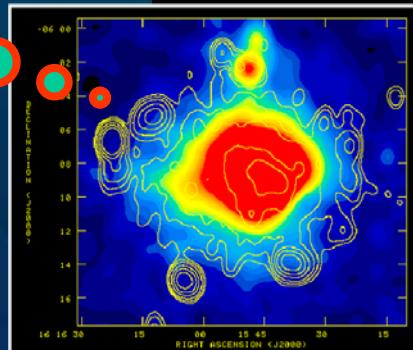
TURBULENCE reaccelerates
fossil e^\pm and secondaries e^\pm on
Mpc

Turbulence?

(e.g., Brunetti *et al.* 2001, 2004,
Miniati *et al.* 2001; Fujita *et al.* 2002;
Gabici & Blasi 2003; Berrington & Dermer 2003;
Pfrommer & Ensslin 2004; Brunetti & Blasi 2005;
Cassano & Brunetti 2005; Cassano *et al.* 2006;
Brunetti & Lazarian 2007; Hoeft & Bruggen 2007;
Pfrommer *et al.* 2008; Petrosian & Bykov 2008, ...)



SHOCKS
accelerate e^\pm , p_{cr}

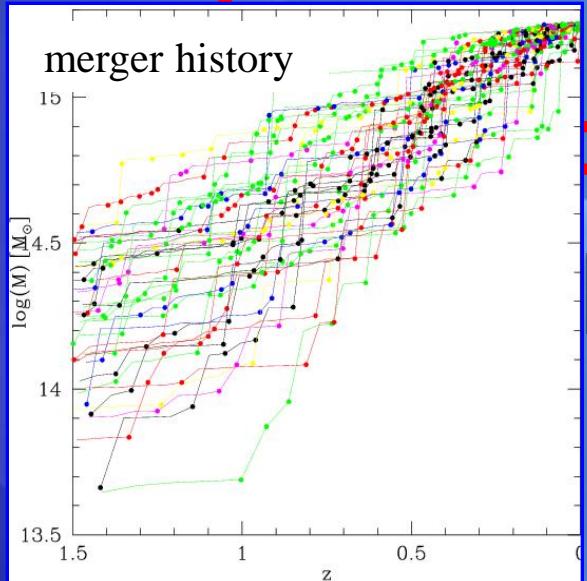


?

Connecting LSS formation

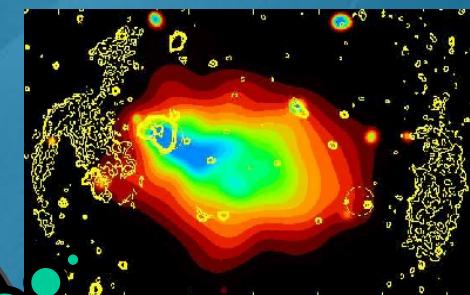
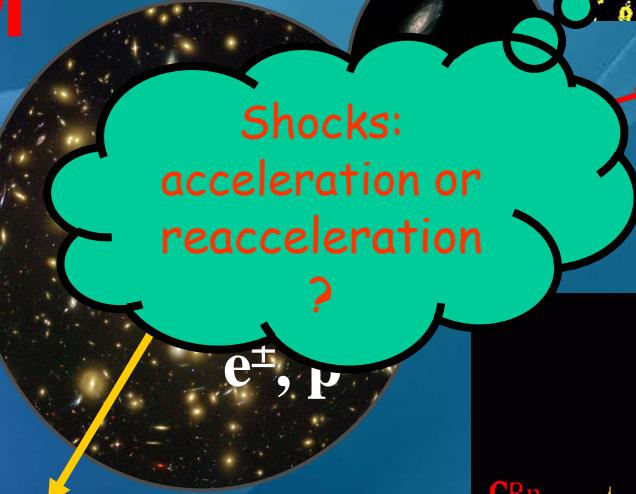
NT-physics

of IGM

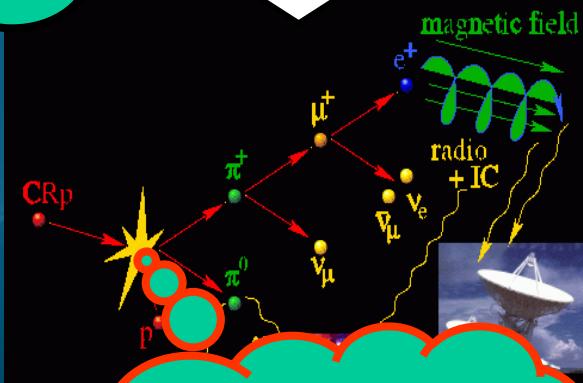


clusters increase their mass
via merger with smaller
subclusters

(e.g., Brunetti *et al.* 2001, 2004,
Miniati *et al.* 2001; Fujita *et al.* 2003;
Gabici & Blasi 2003; Berrington & Dermer 2003;
Pfrommer & Ensslin 2004; Brunetti & Blasi 2005;
Cassano & Brunetti 2005; Cassano *et al.* 2006;
Brunetti & Lazarian 2007; Hoeft & Bruggen 2007;
Pfrommer *et al.* 2008; Petrosian & Bykov 2008, ...)

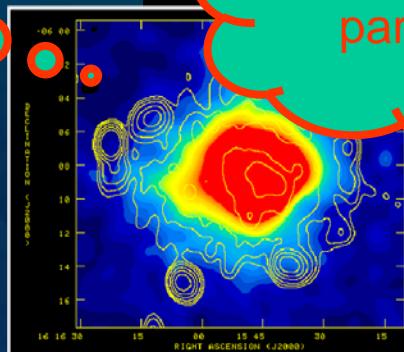


SHOCKS
accelerate e^\pm, p_{cr}



TURBULENCE reaccelerates
fossil e^\pm and secondaries e^\pm on
Mpc

Turbulence?



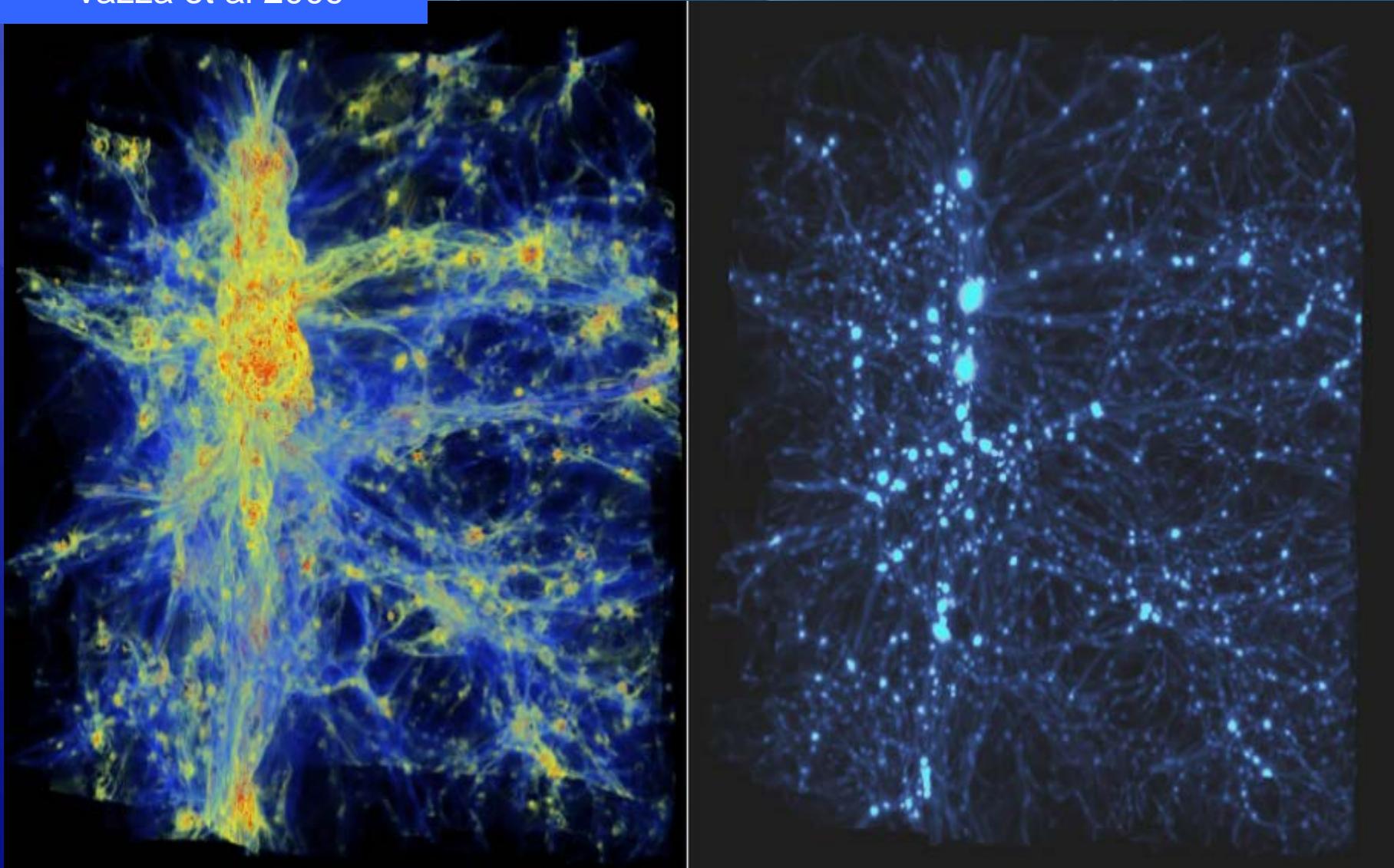
Relevance of
secondary
particles ?

?

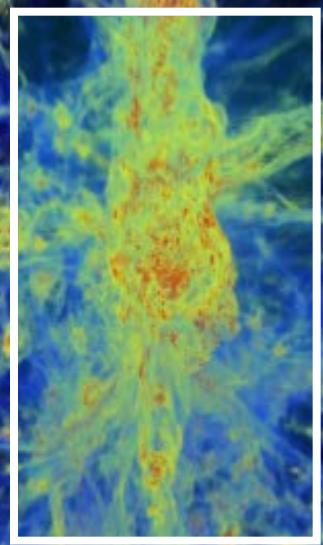
Cosmological Shocks

Natural consequence of the hierarchical process of LSS formation

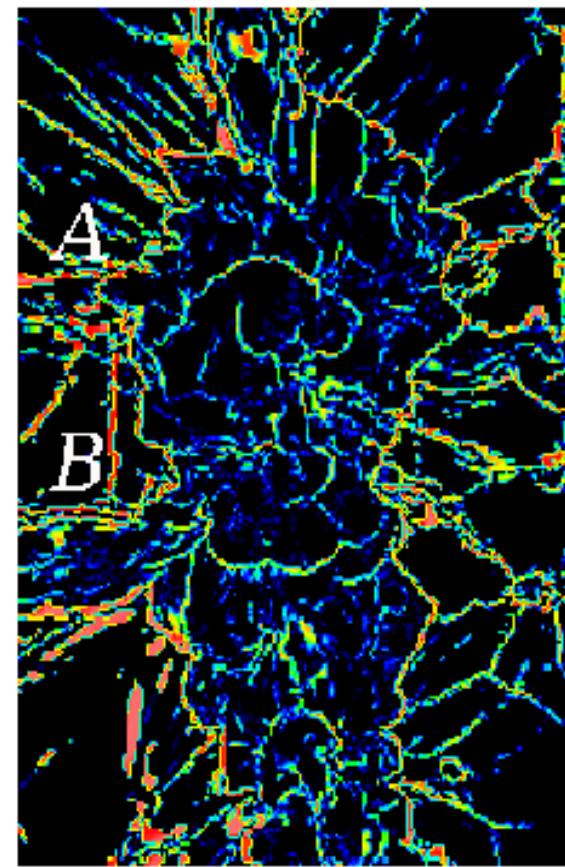
Vazza et al 2009



Shocks in Galaxy Clusters



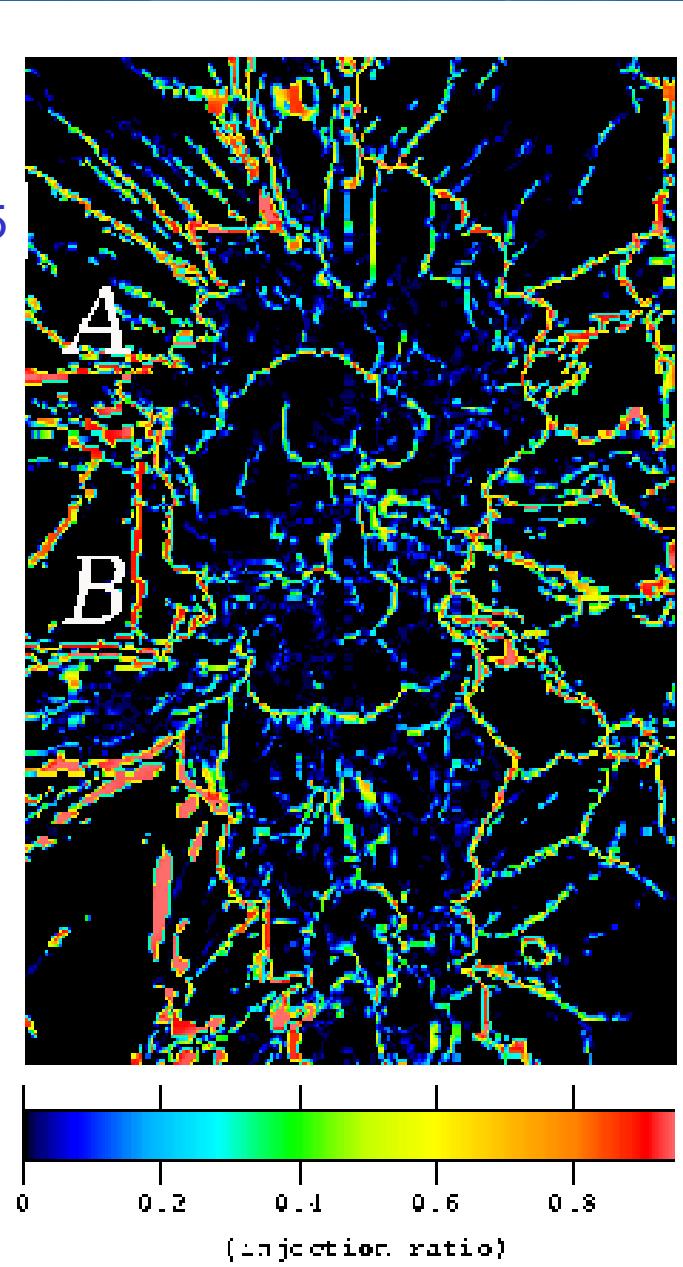
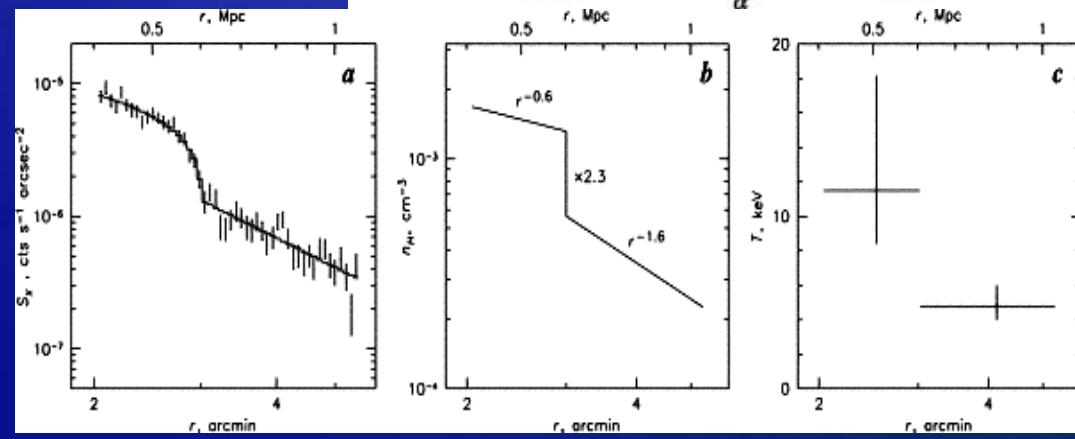
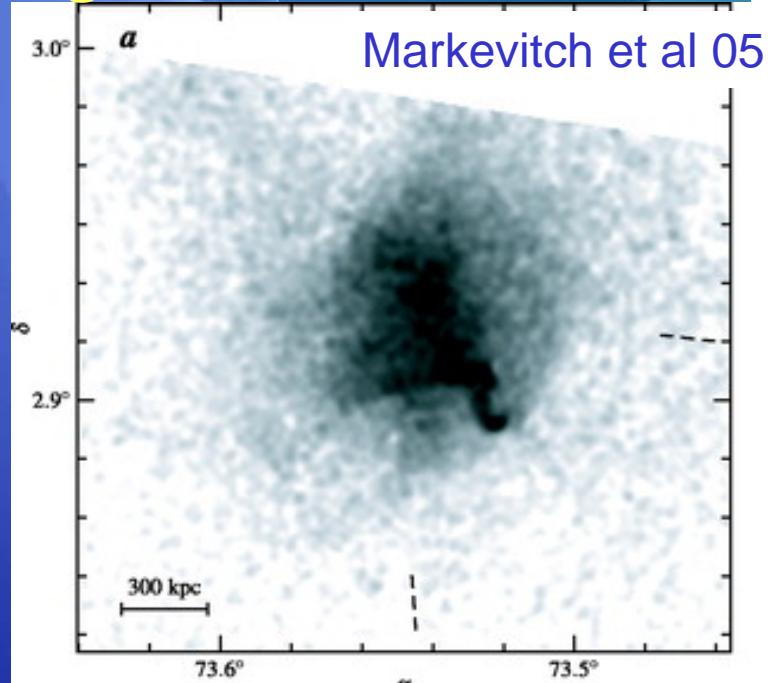
Miniati et al. 2001;
Ryu et al. 2003;
Pfrommer et al. 2006,08;
Hoeft & Bruggen 2007;
Skillman et al. 2008,11
Vazza et al. 2009, 11



Vazza, Brunetti, Gheller 2009

Shocks in Galaxy Clusters

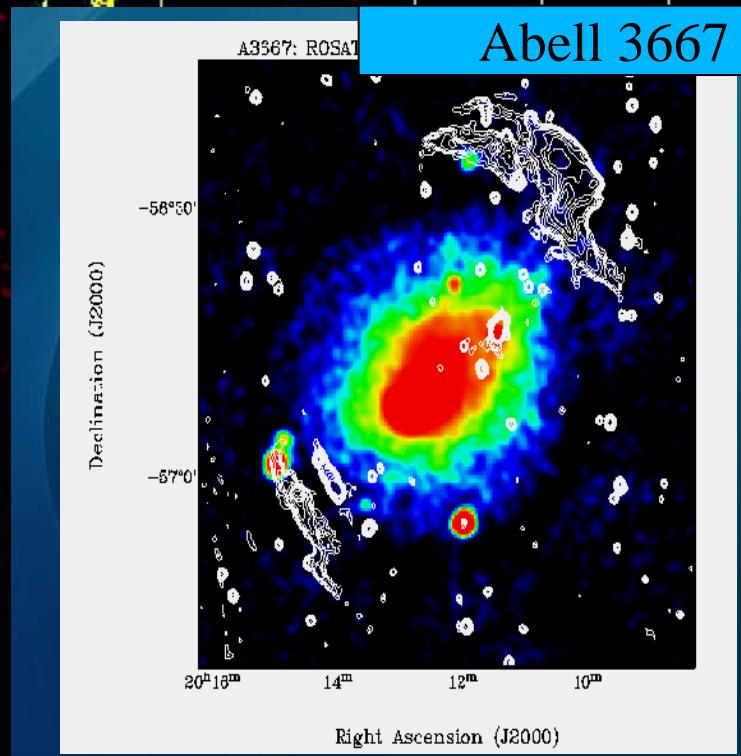
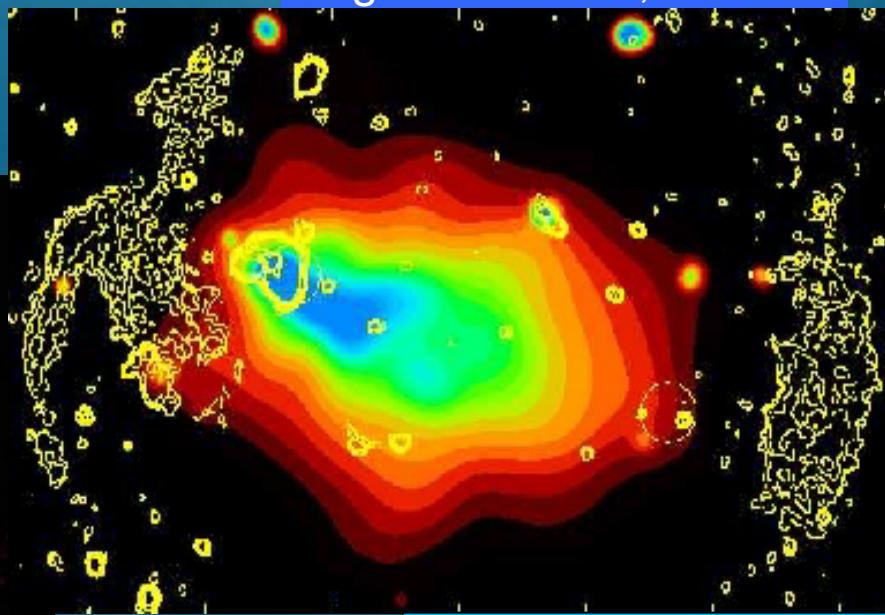
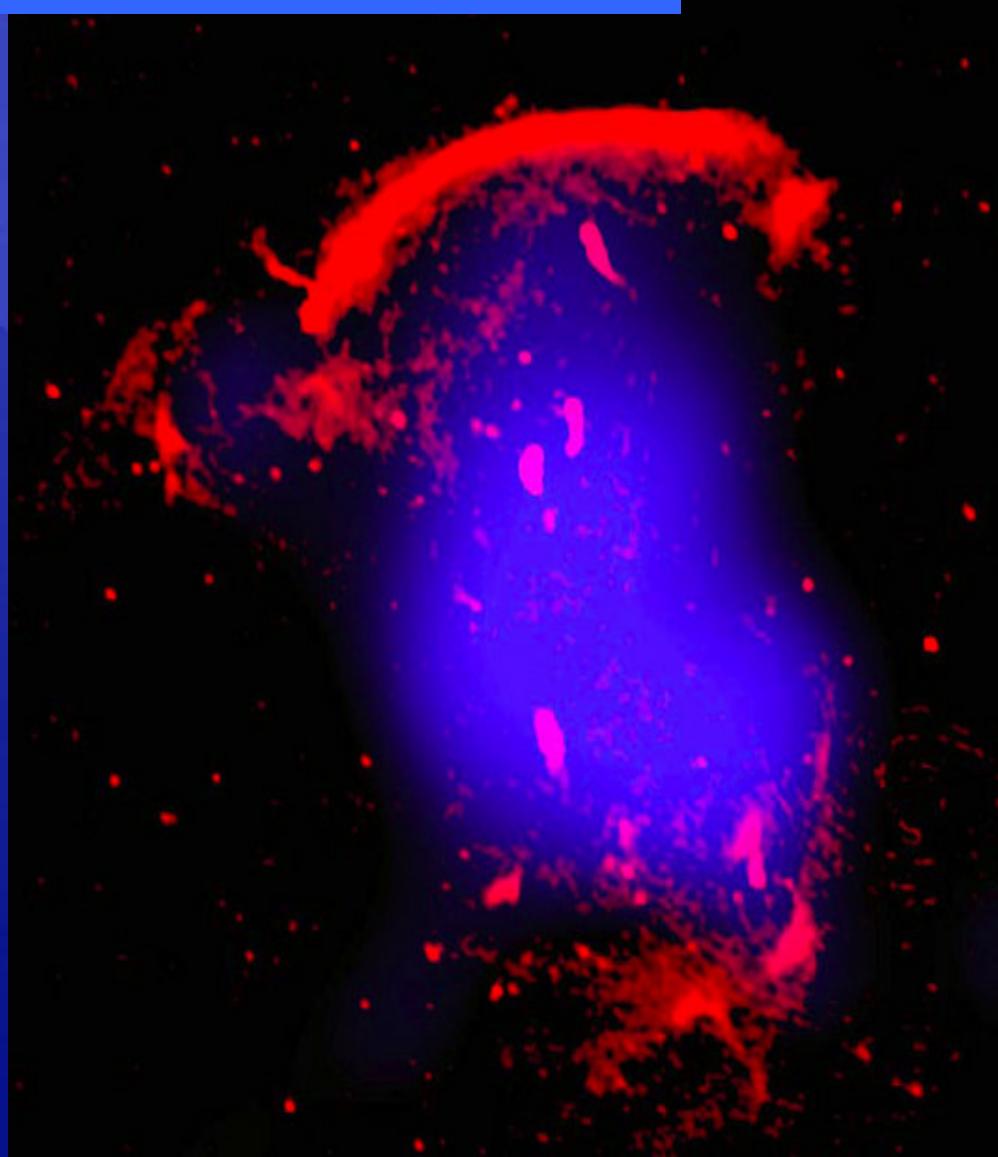
Shocks are responsible for
the heating of the IGM



Shock—Relic connection

Bagchi+al. 2002, *Science*

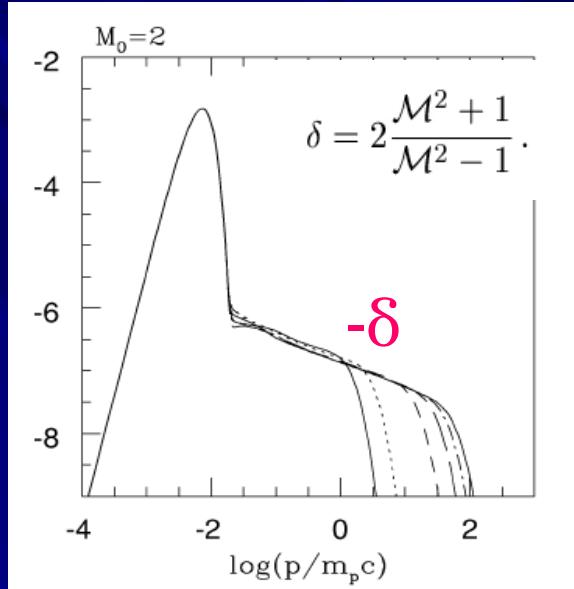
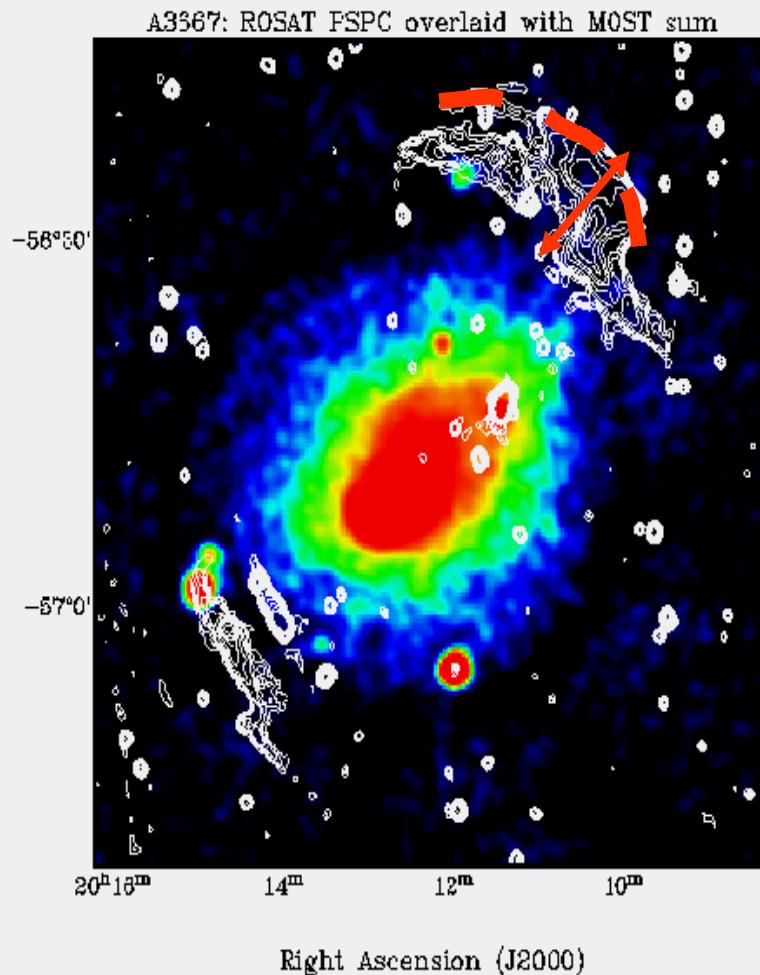
van Weeren+al. 2010, *Science*



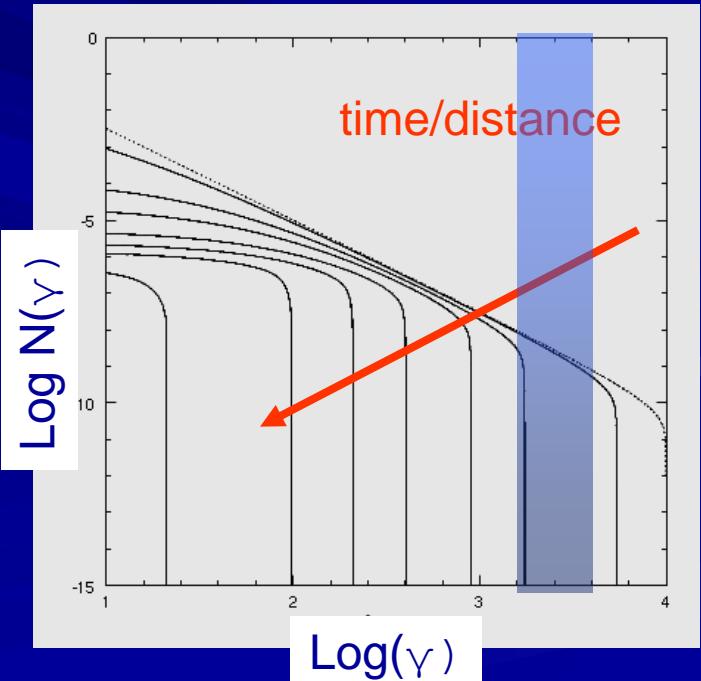
Shock Acceleration: Radio Relics

(Ensslin et al 1998, Roettiger et al. 1999, Sarazin 1999, ...)

Abell 3667



$$I_R \approx V_d \tau e(v) \approx 100 \text{ kpc}$$

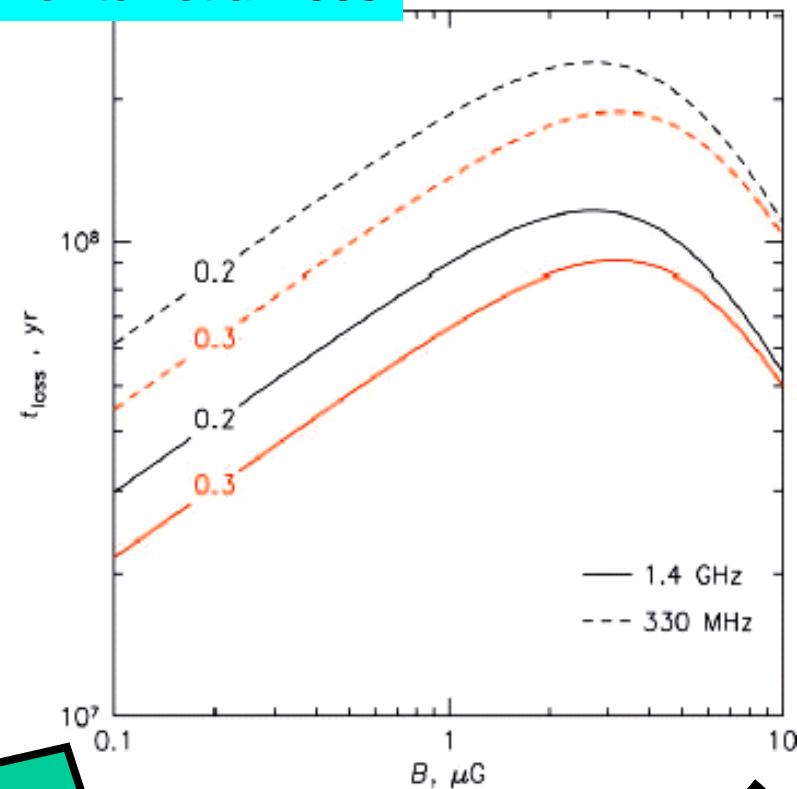


Width of Relics & constraints on B

Markevitch et al 2005

$$\tau_e(\text{Gyr}) \sim 4 \times \left\{ \frac{1}{3} \left(\frac{\gamma}{300} \right) \left[\left(\frac{B_{\mu G}}{3.2} \right)^2 \frac{\sin^2 \theta}{2/3} + (1+z)^4 \right] \right. \\ \left. + \left(\frac{n_{\text{th}}}{10^{-3}} \right) \left(\frac{\gamma}{300} \right)^{-1} \left[1.2 + \frac{1}{75} \ln \left(\frac{\gamma/300}{n_{\text{th}}/10^{-3}} \right) \right] \right\}^{-1}.$$

$$\gamma \approx c_{\text{syn}} (v/B)^{1/2}$$

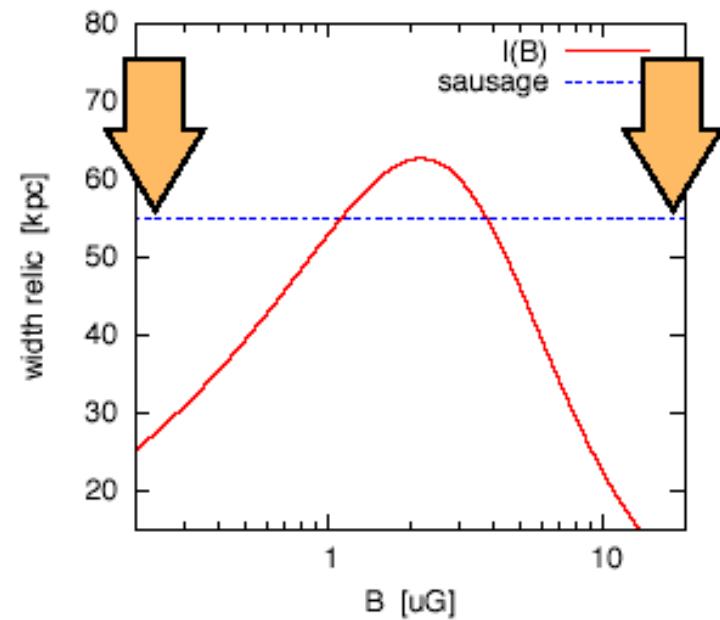
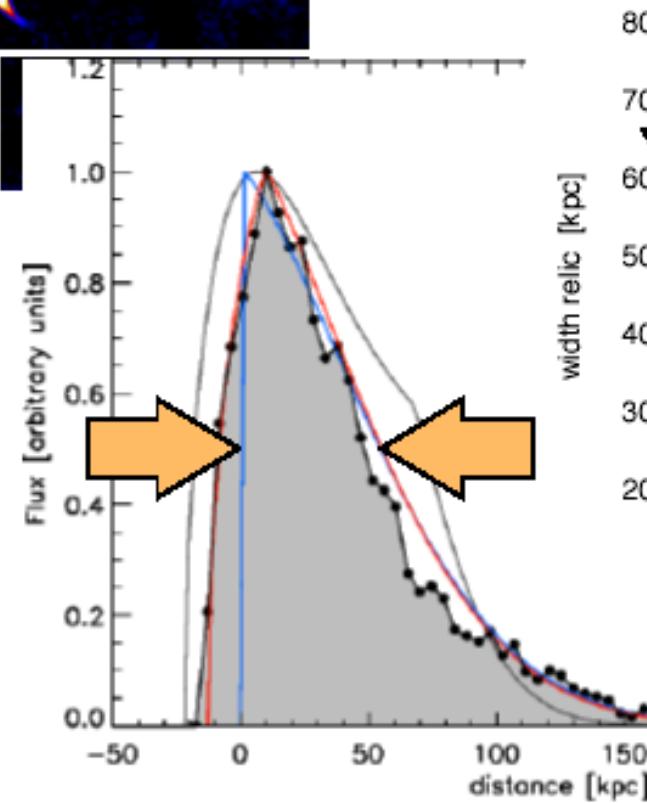
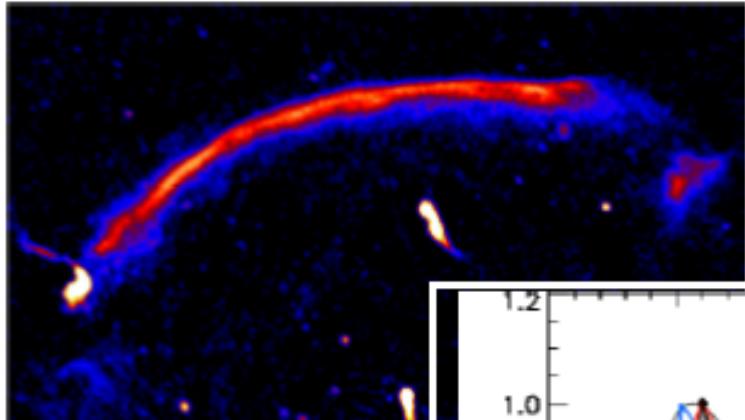


Width of Relic

$$V_d \approx c_s M (M^2 + 3) / 4M^2$$

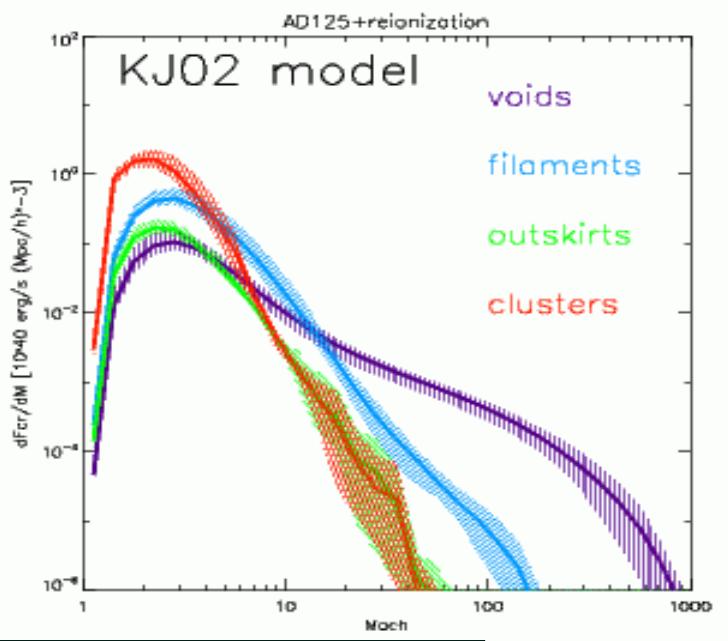
The width of the 'sausage' (CIZA 2242)

Van Weeren et al., 10

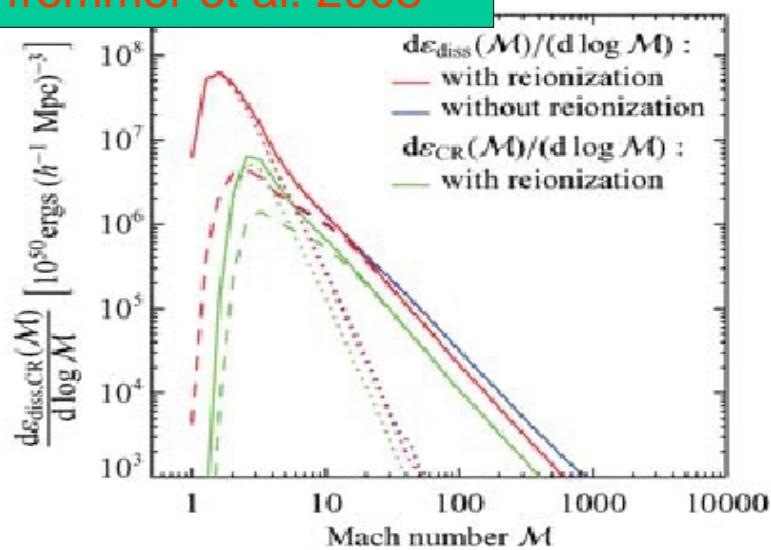


Mach numbers in galaxy clusters

Vazza, Brunetti, Gheller 2009

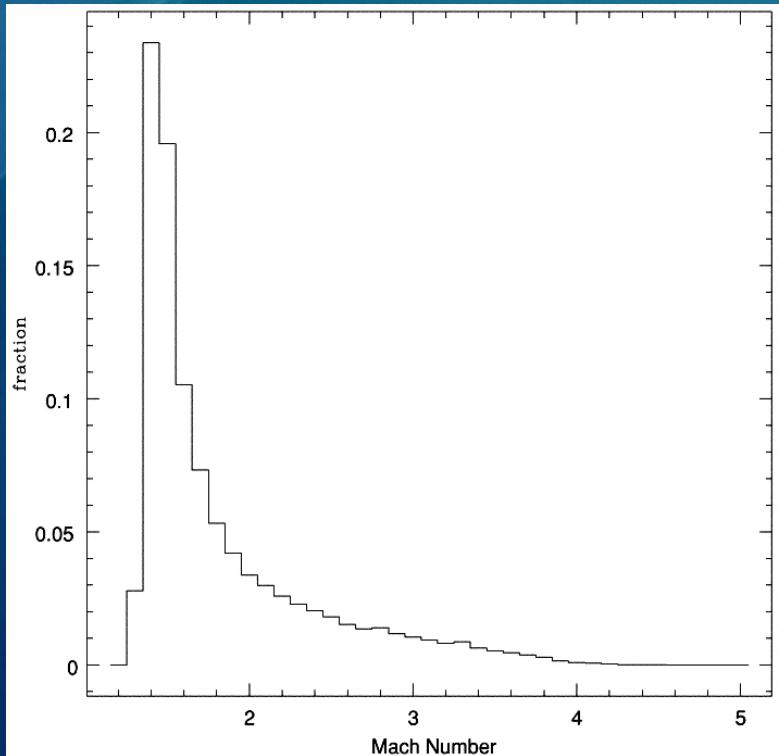


Pfrommer et al. 2008



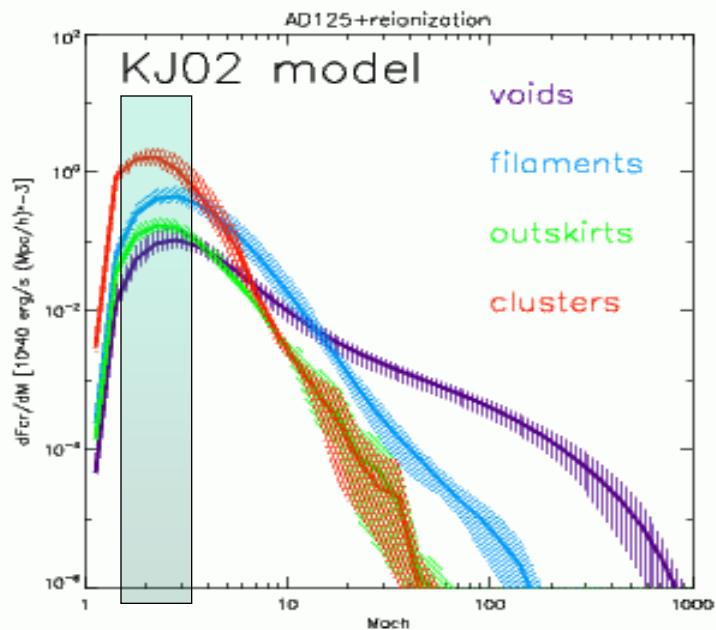
Semi-analytics :
Gabici & Blasi 2003
Berrington & Dermer 2003

some agreement...

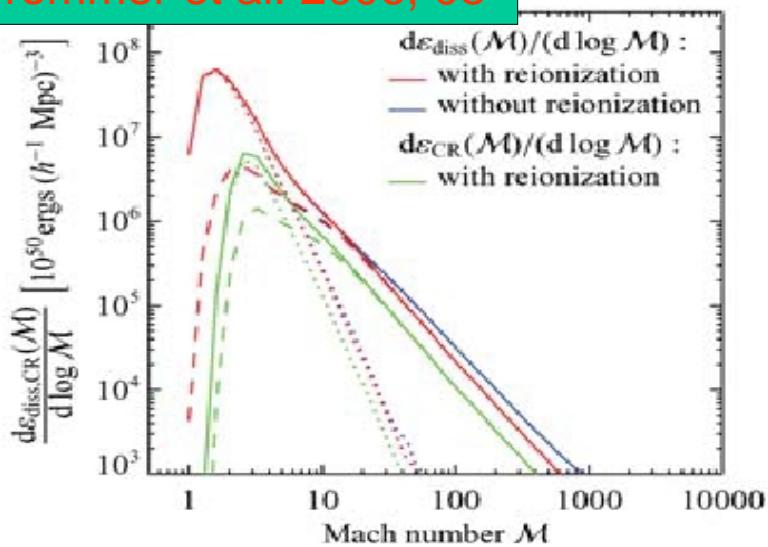


Uncertainties in CR acceleration

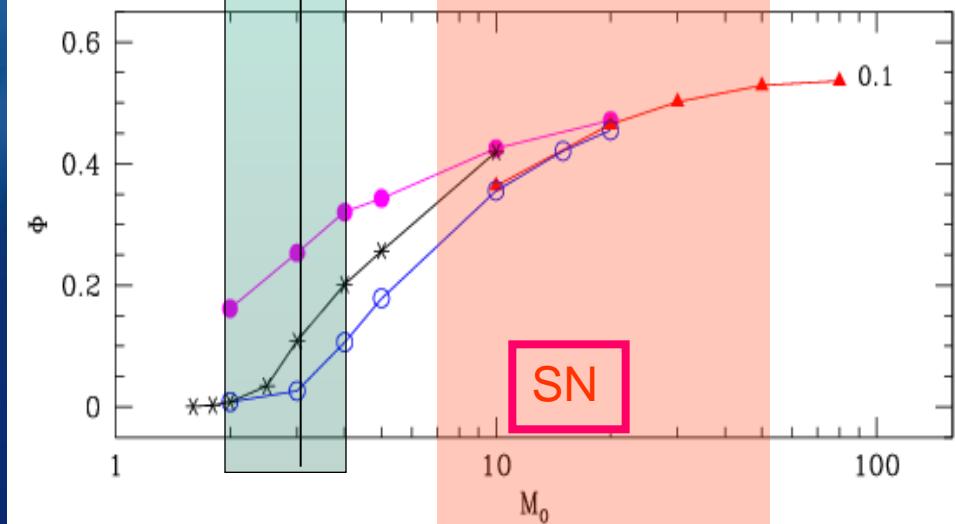
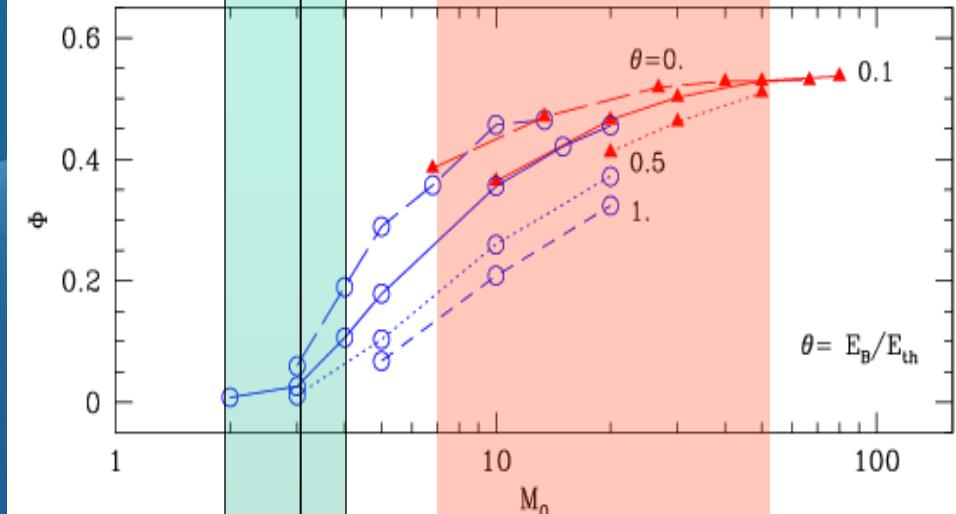
Vazza, Brunetti, Gheller 2009



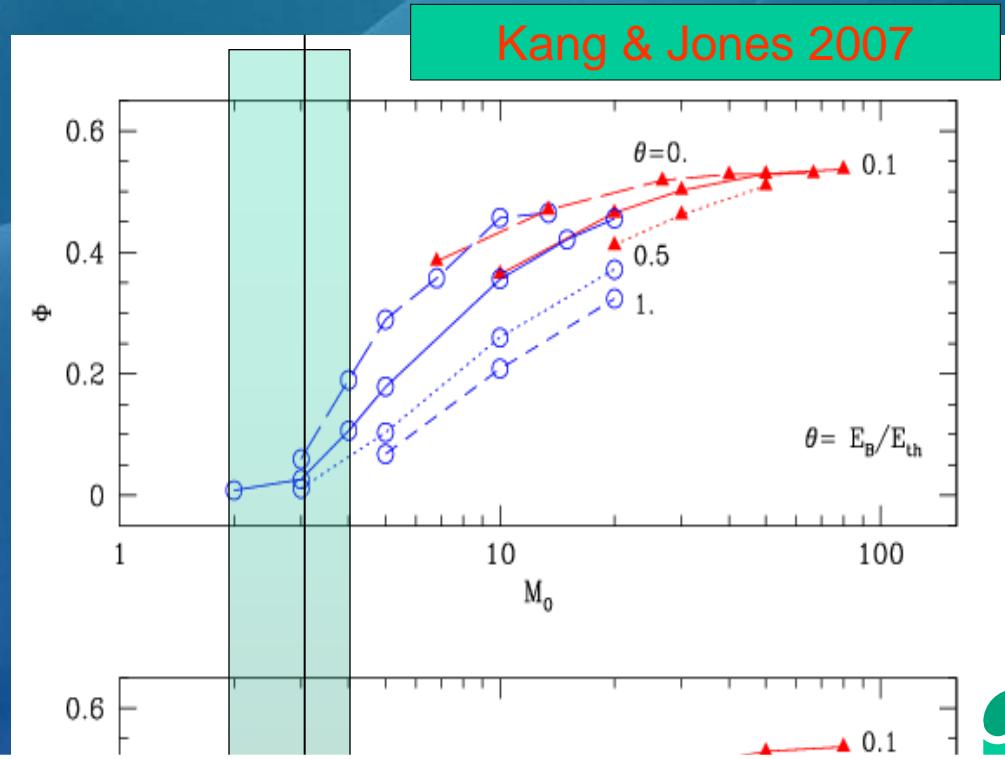
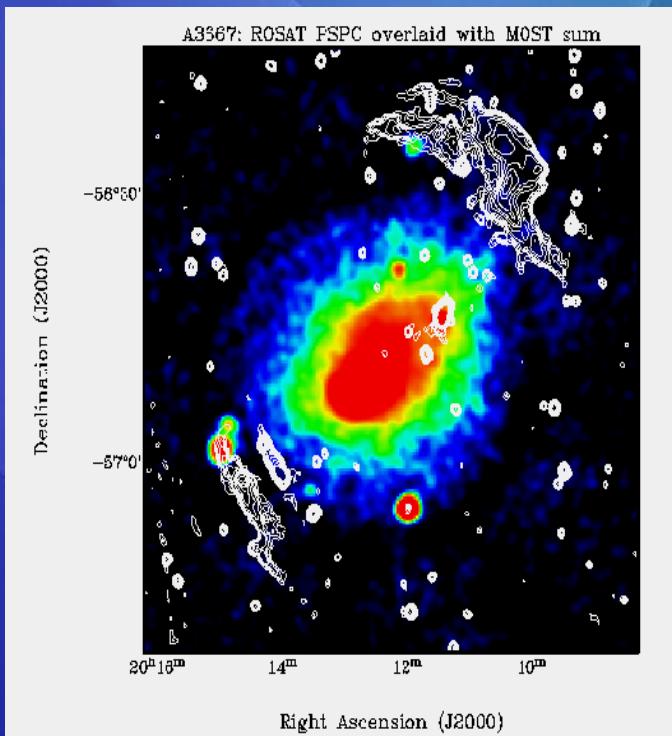
Pfrommer et al. 2006, 08



Kang & Jones 2007



CR acceleration or REacceleration?



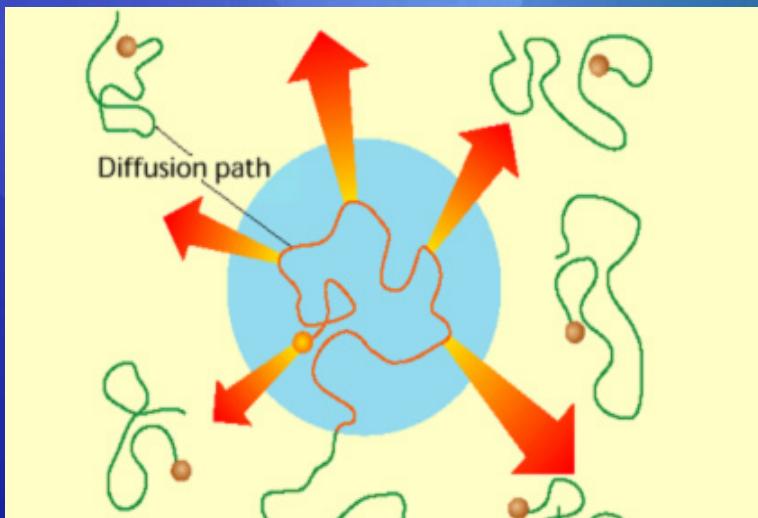
Merger shocks have $M=1.5-3$.
Reacceleration of
pre-existing relativistic
electrons at these shocks is
efficient (eg. Kang & Ryu 11)

Galaxy clusters are unique labs
to study particle acceleration
at weak & LS shocks

Radio Halos as “labs” for CR acceleration in GC

$$L^2 \sim D \times t$$

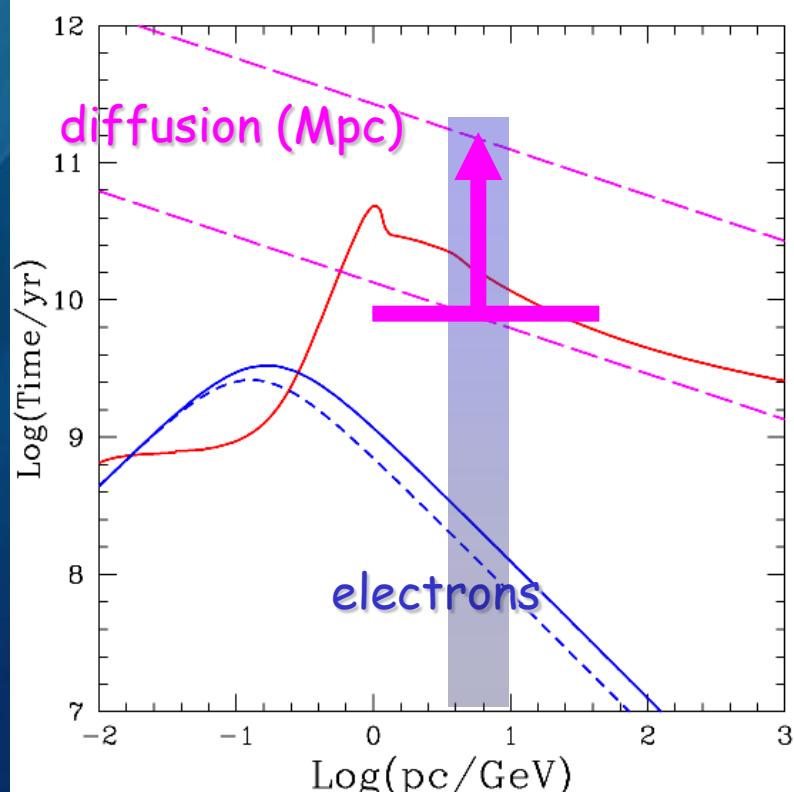
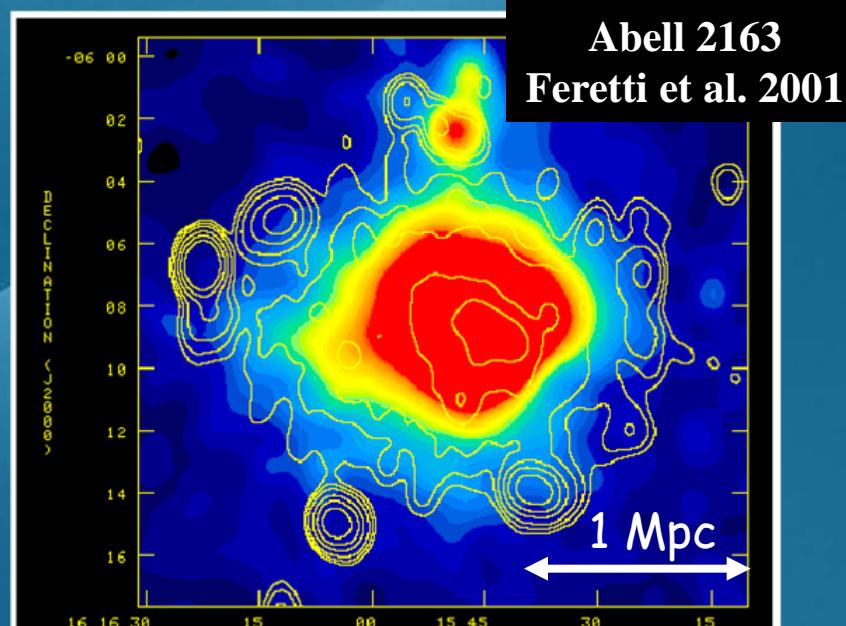
$$D(E_p) = \frac{1}{3} r_L c \frac{B^2}{\int_{1/r_L}^{\infty} dk P(k)}$$



$$T_{\text{diff}} (\sim 10^{10} \text{ yr}) \gg T_{\text{cool}} (\sim 10^8 \text{ yr})$$

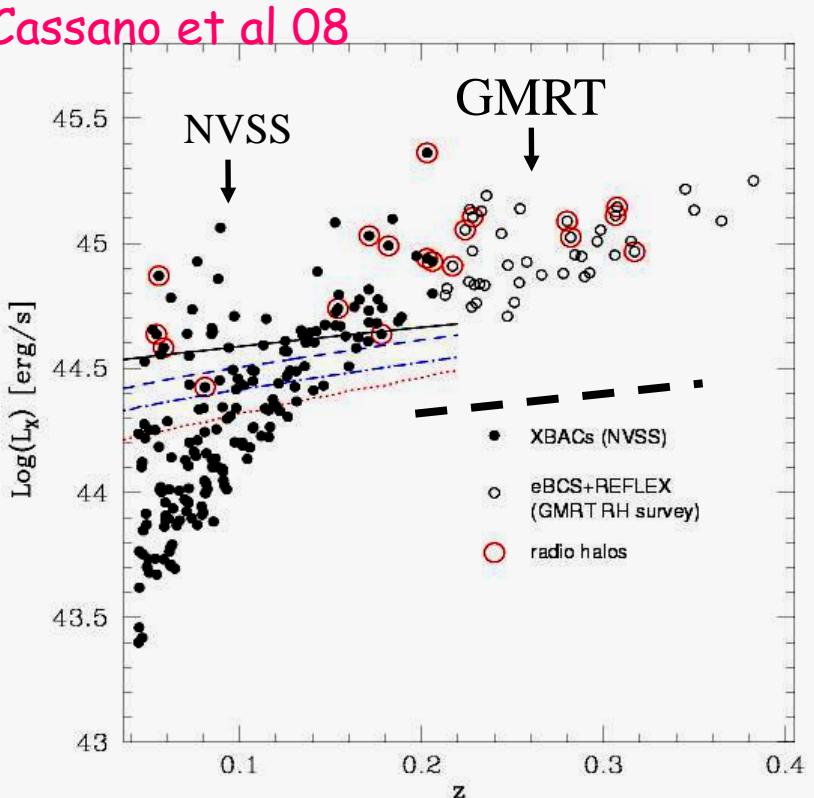
(eg. Jaffe 1977)

“*in situ*” (re)acceleration or injection of CR electrons ...



Statistics of Radio Halos

Cassano et al 08

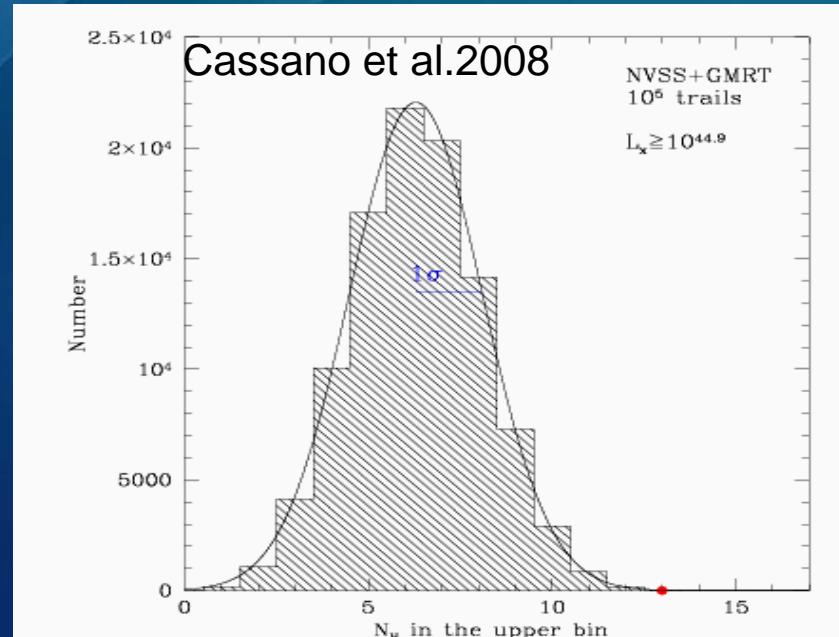
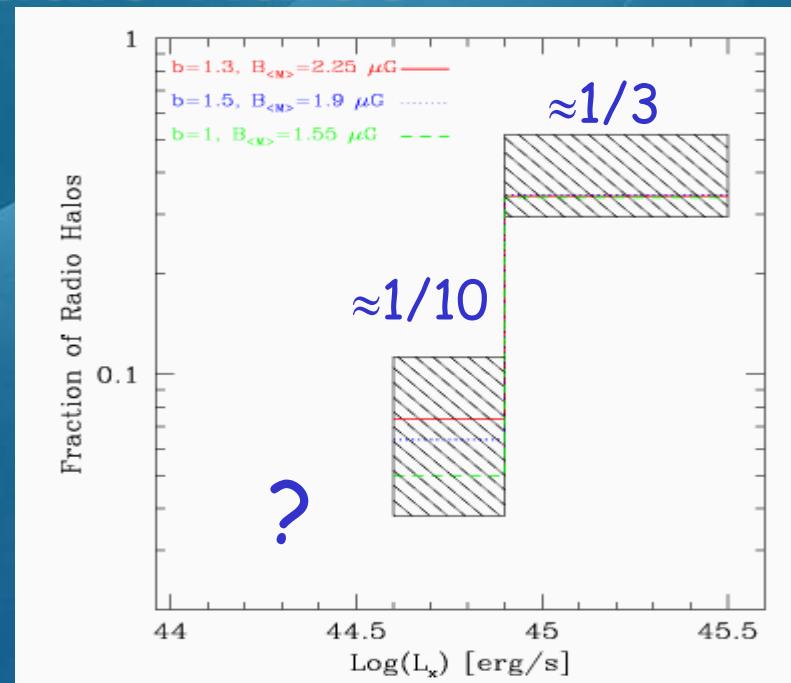


NVSS data (from Giovannini et al. 1999)
and deep GMRT observations.

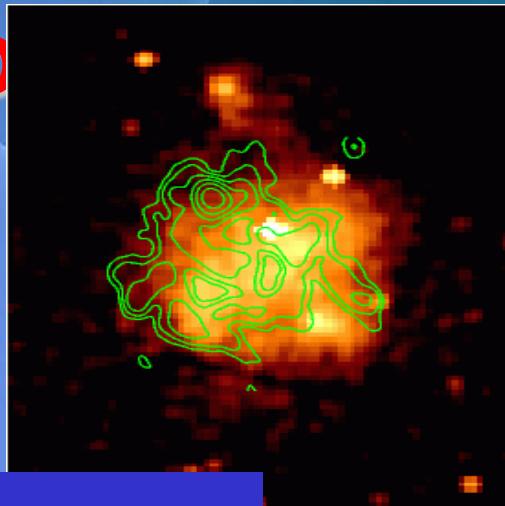
0.41 ± 0.11 for $L_x > 10^{44.9}$ erg/s $\approx 1/3$

0.08 ± 0.04 for $L_x < 10^{44.9}$ erg/s $\approx 1/10$

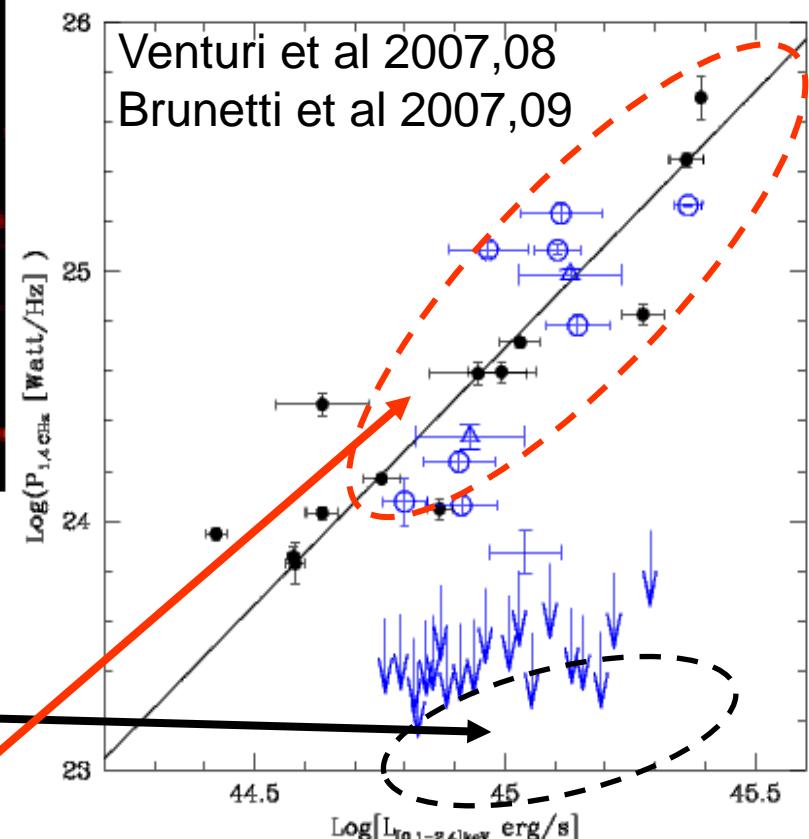
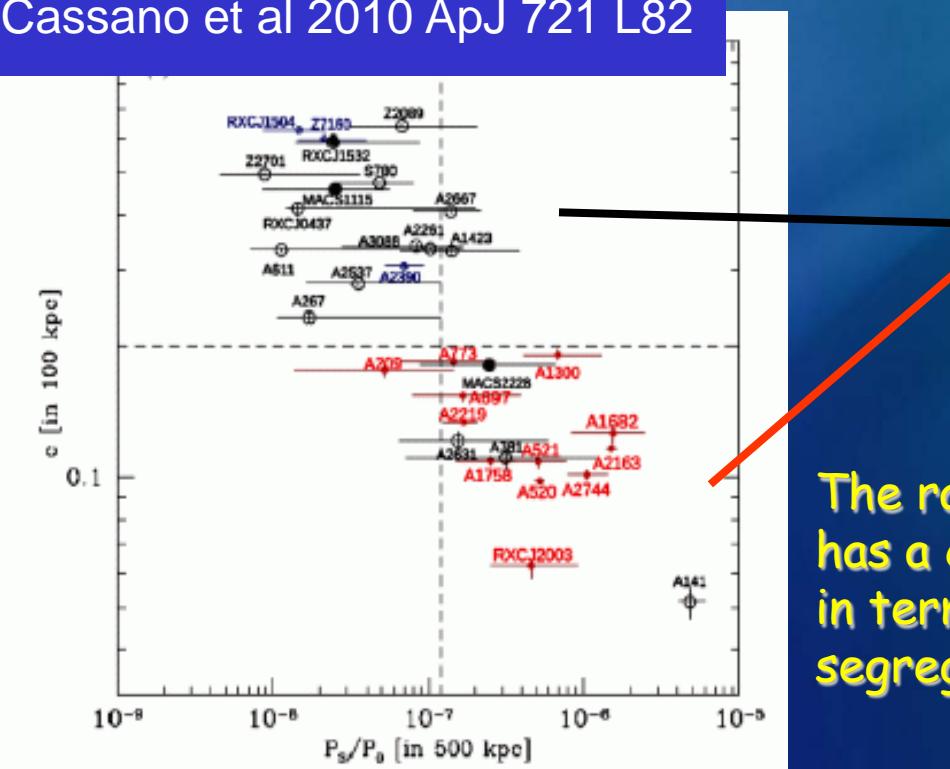
(Venturi et al. 2007, 2008; Cassano et al. 2008)



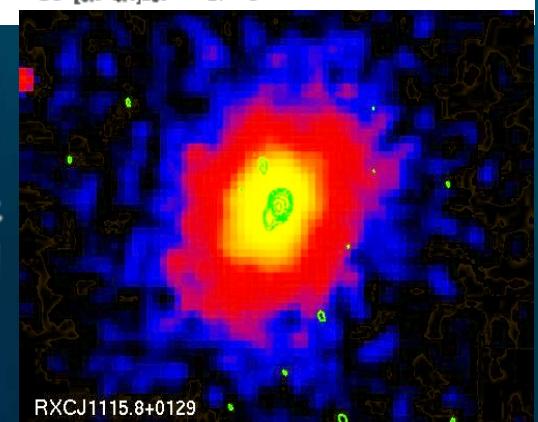
Cluster mergers - radio halos connection



Cassano et al 2010 ApJ 721 L82

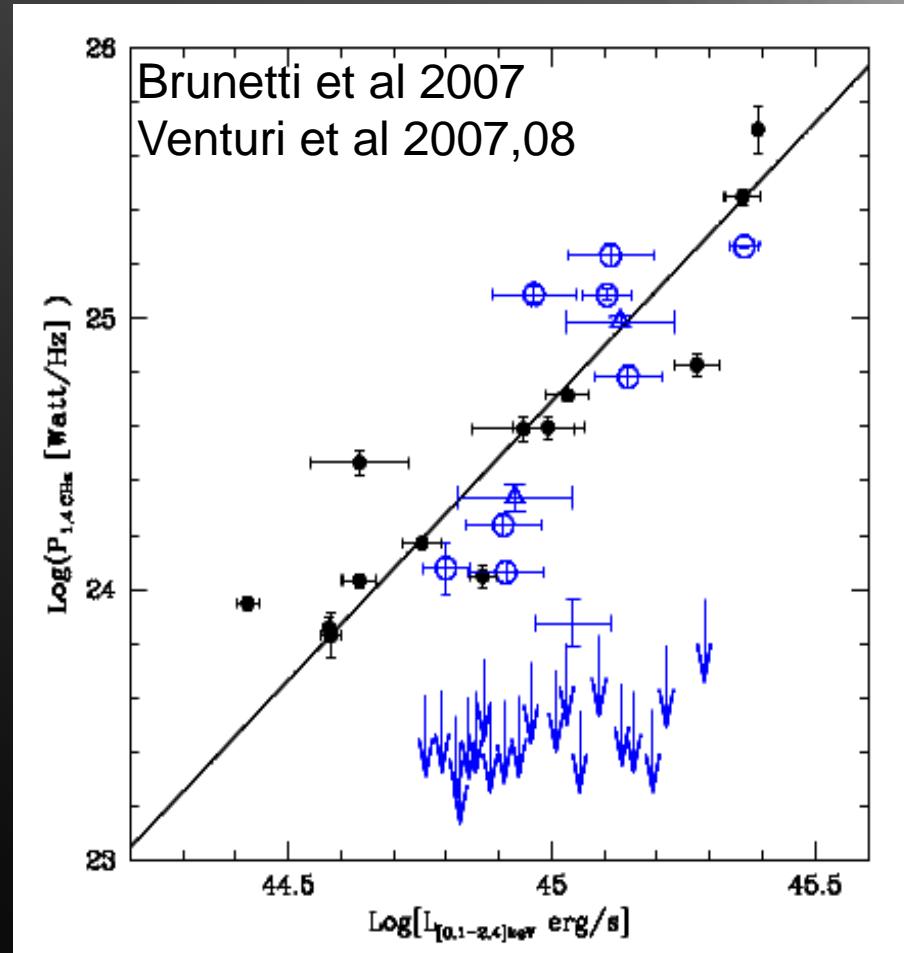
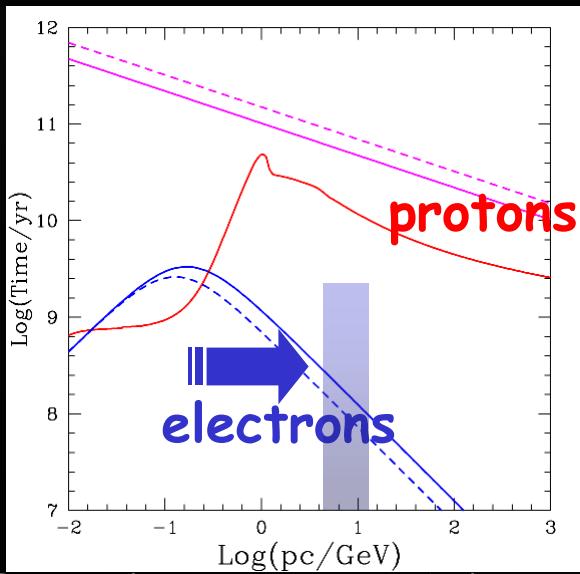
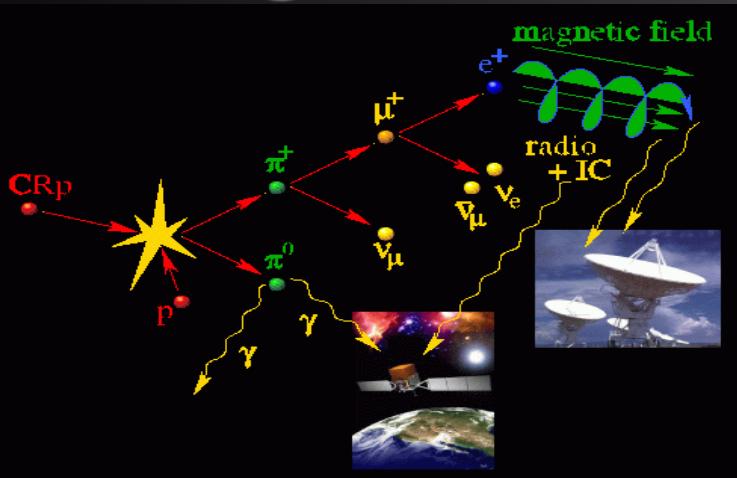


The radio bimodality
has a correspondence
in terms of dynamical
segregation



RXCJ1115.8+0129

Origin of Radio Halos: turbulence ?

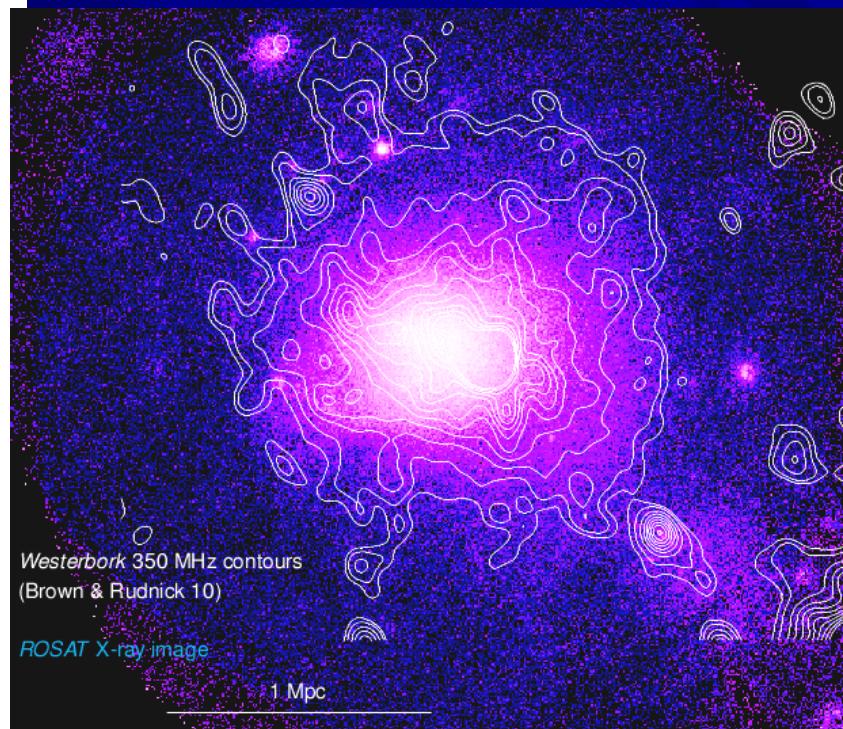
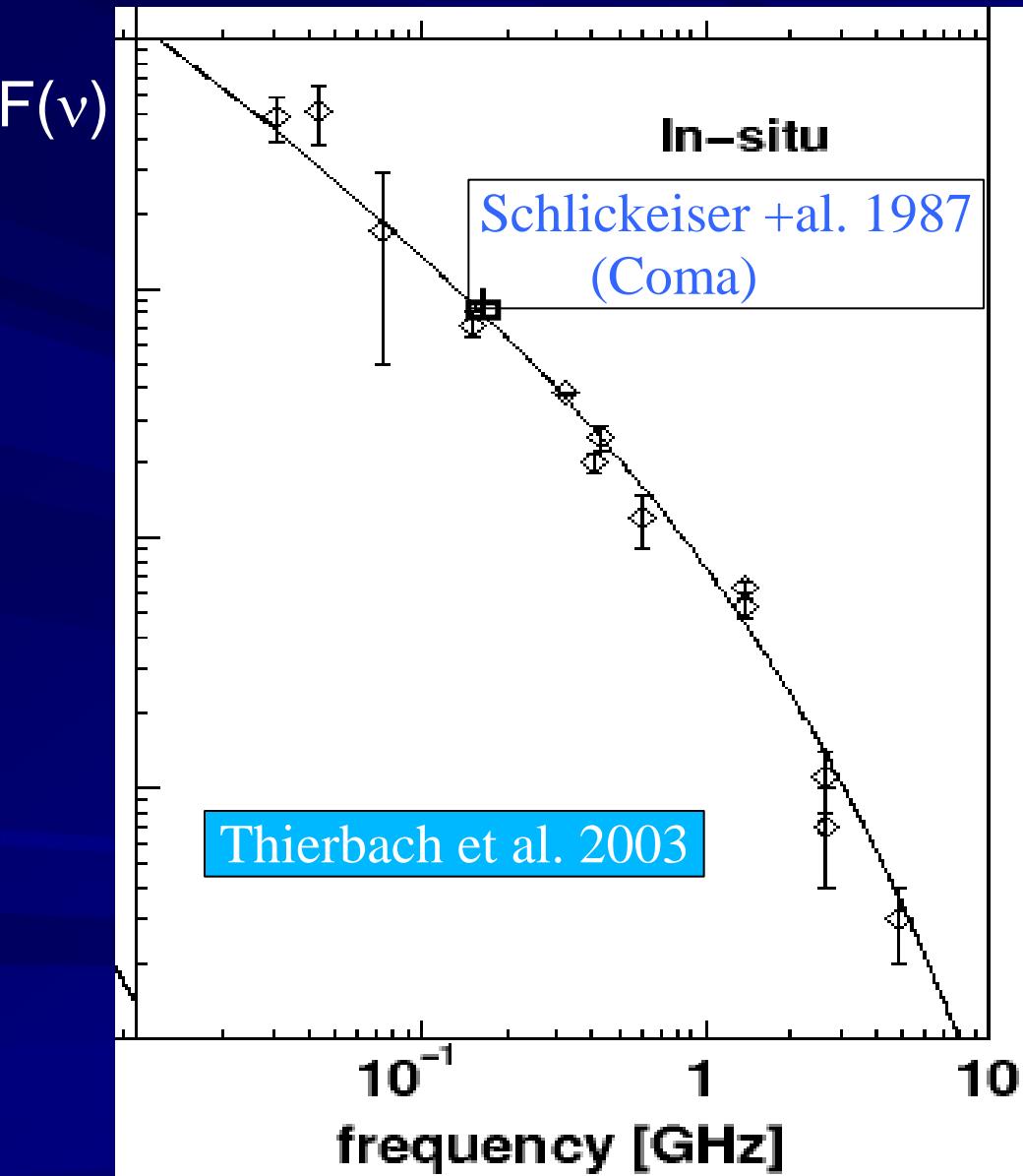


REacceleration models (eg Brunetti et al 01, Petrosian 01, ...)

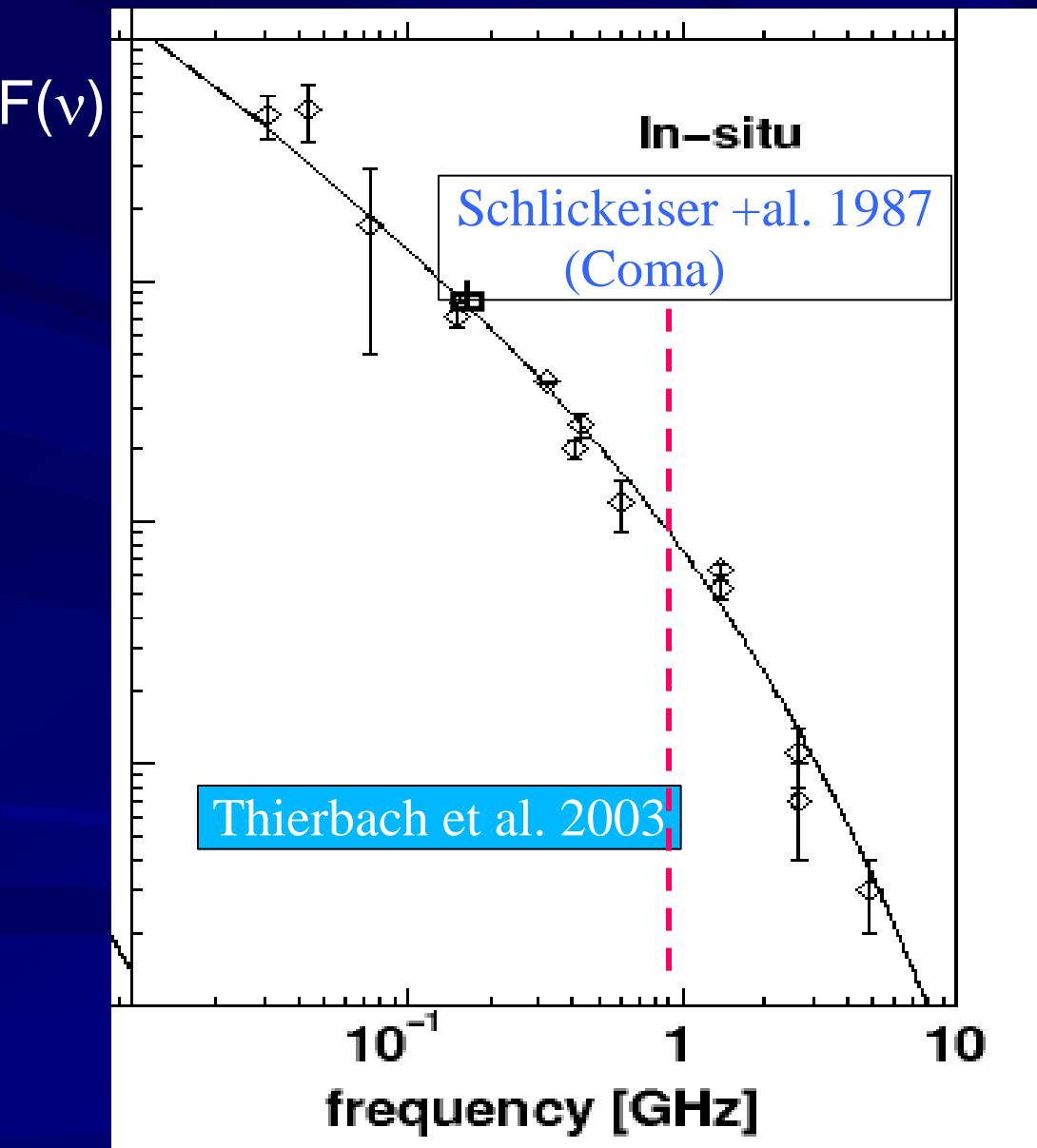
A mechanism distributed on Mpc scales channels a fraction of the gravitational energy dissipated during mergers into high energy particles

Turbulence ??

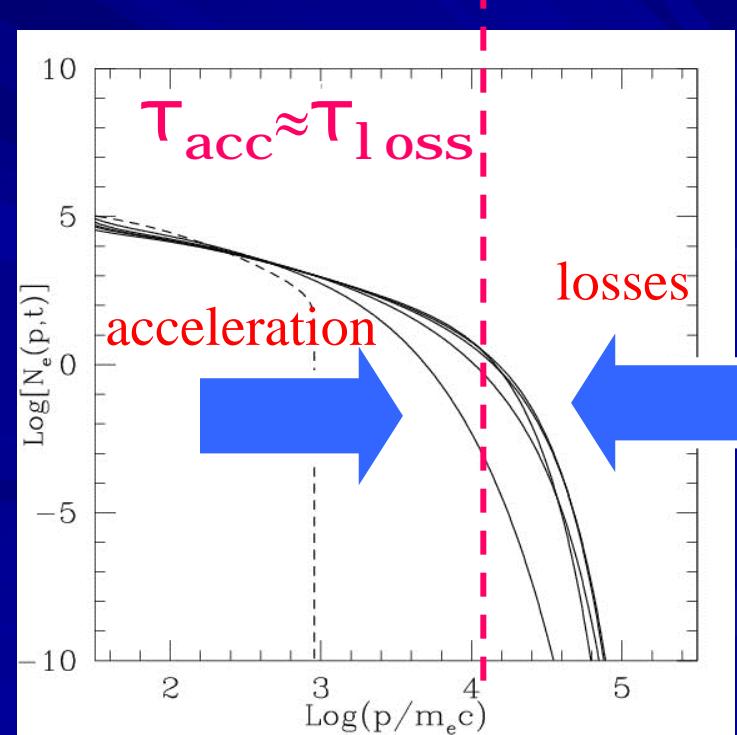
Radio Halos : are they generated by "inefficient" mechanism of CRe acceleration ?



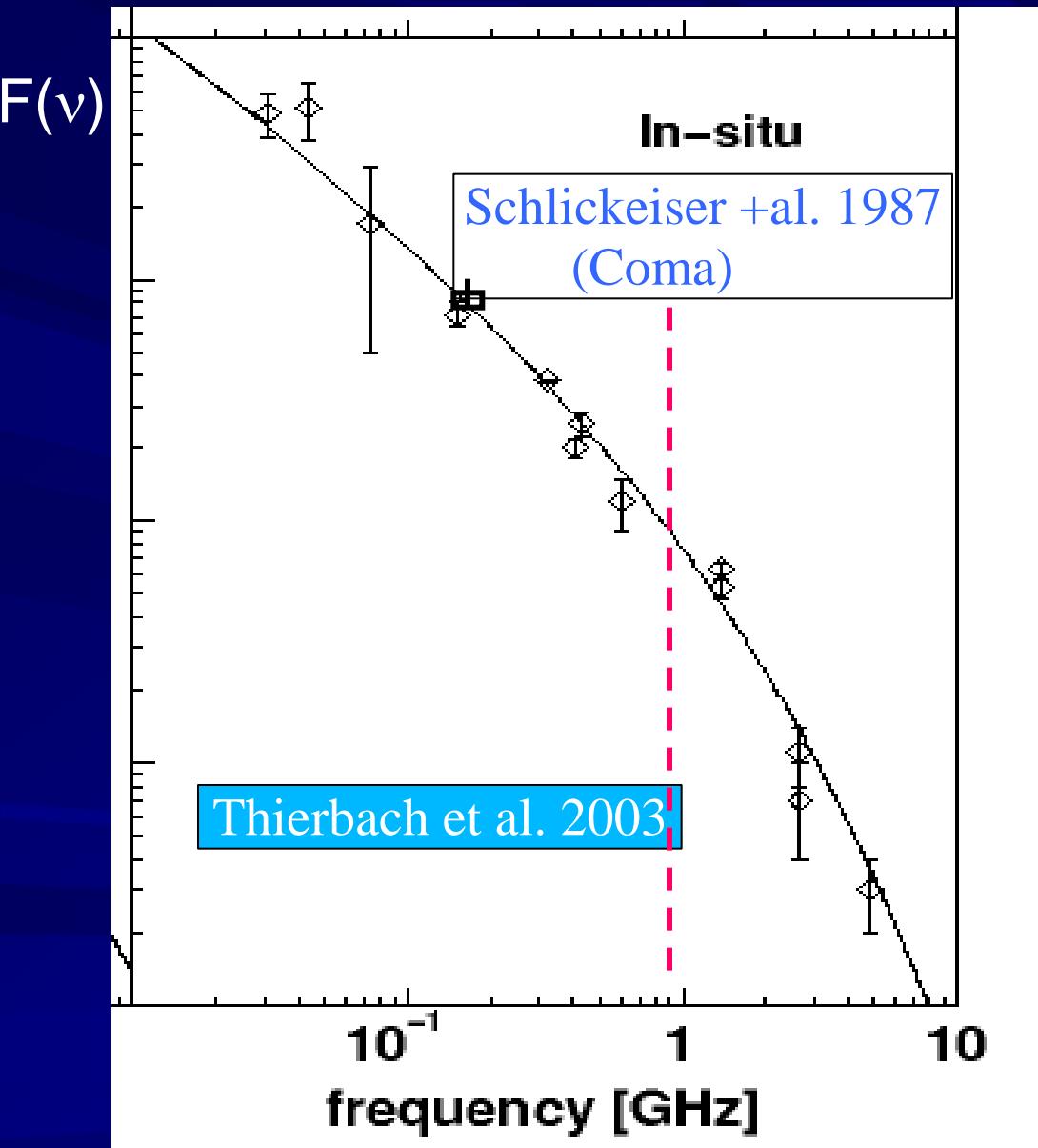
Radio Halos : are they generated by "inefficient" mechanism of CRe acceleration ?



Evidence of break in the spectrum of the emitting electrons at energies of few GeV

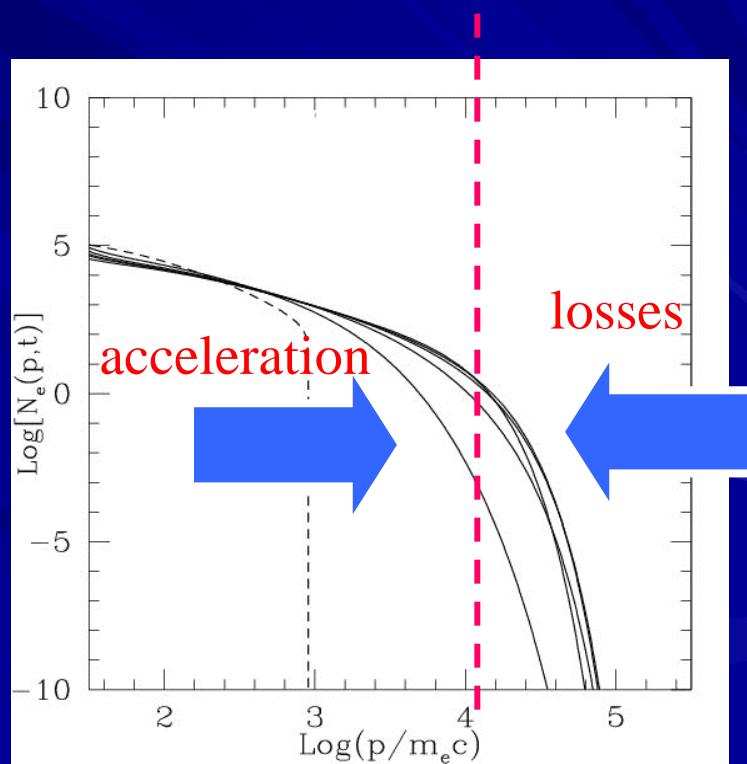


Radio Halos : are they generated by "inefficient" mechanism of CRe acceleration ?

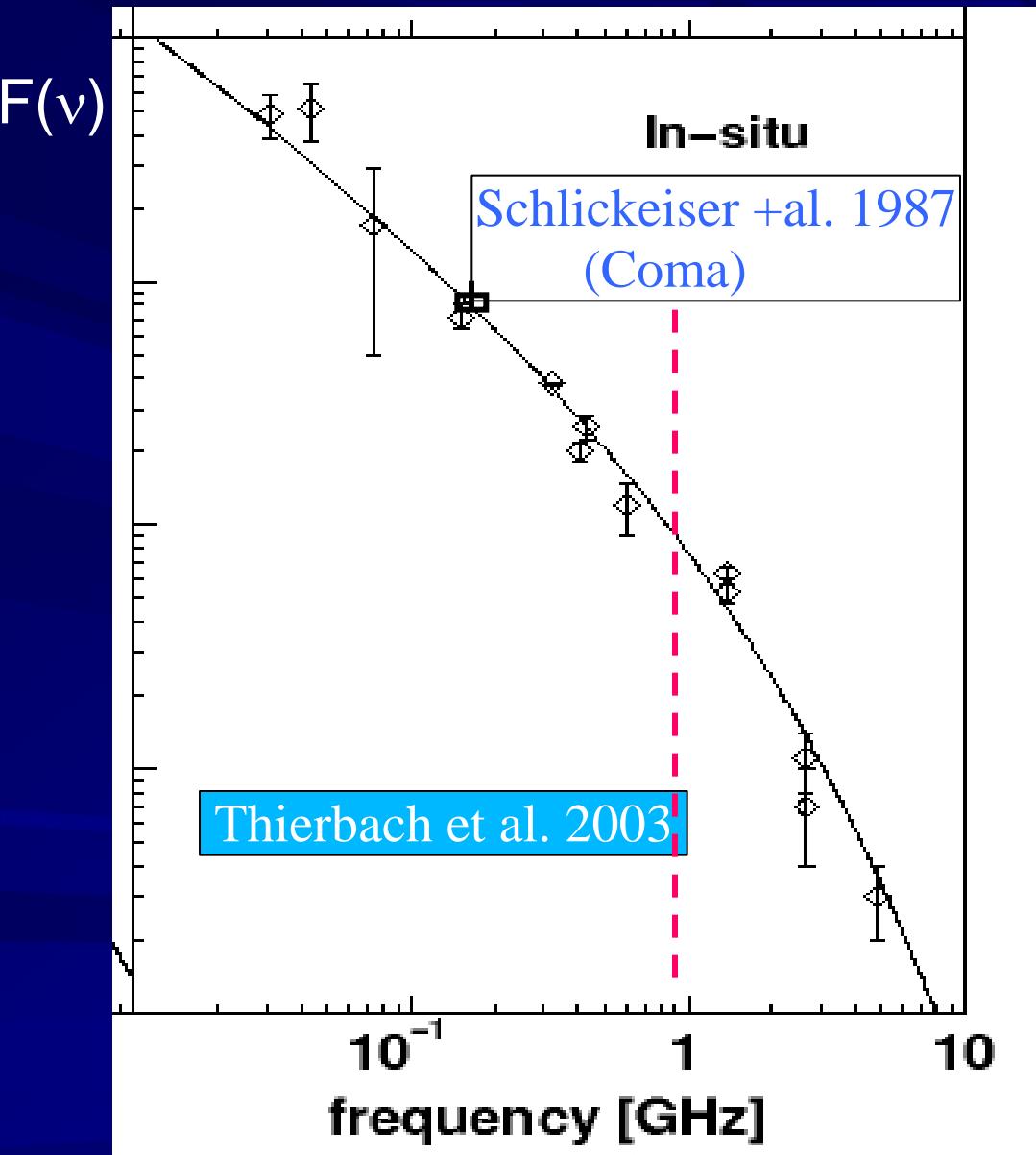


$$\tau_e(\text{Gyr}) \sim 4 \times \left\{ \frac{1}{3} \left(\frac{\gamma}{300} \right) \left[\left(\frac{B_{\mu G}}{3.2} \right)^2 \frac{\sin^2 \theta}{2/3} + (1+z)^4 \right] \right. \\ \left. + \left(\frac{n_{\text{th}}}{10^{-3}} \right) \left(\frac{\gamma}{300} \right)^{-1} \left[1.2 + \frac{1}{75} \ln \left(\frac{\gamma/300}{n_{\text{th}}/10^{-3}} \right) \right] \right\}^{-1}.$$

Acceleration time-scale
 $\approx 10^8$ years



Radio Halos : are they generated by "inefficient" mechanism of CRe acceleration ?



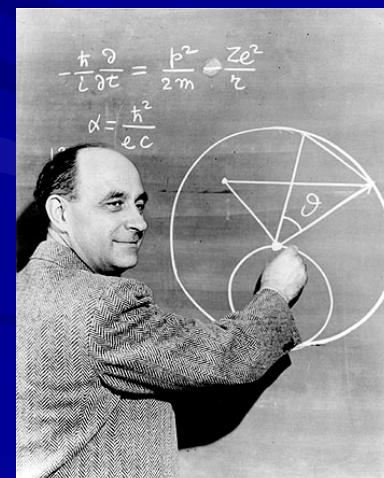
$$\tau_e(\text{Gyr}) \sim 4 \times \left\{ \frac{1}{3} \left(\frac{\gamma}{300} \right) \left[\left(\frac{B_{\mu G}}{3.2} \right)^2 \frac{\sin^2 \theta}{2/3} + (1+z)^4 \right] \right. \\ \left. + \left(\frac{n_{\text{th}}}{10^{-3}} \right) \left(\frac{\gamma}{300} \right)^{-1} \left[1.2 + \frac{1}{75} \ln \left(\frac{\gamma/300}{n_{\text{th}}/10^{-3}} \right) \right] \right\}^{-1}.$$

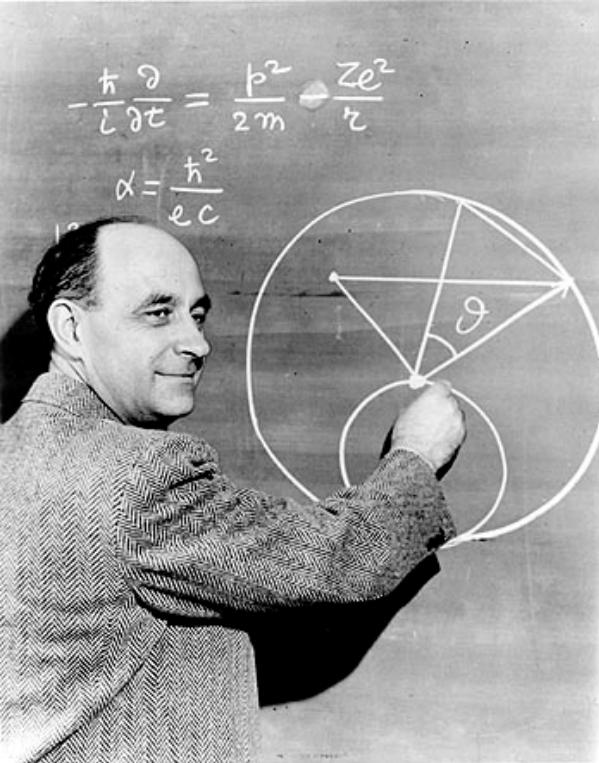
Acceleration time-scale
 $\approx 10^8$ years

e.g., "classical" Fermi II

$$\tau_{\text{acc}} \approx \frac{L_t c}{V_t^2}$$

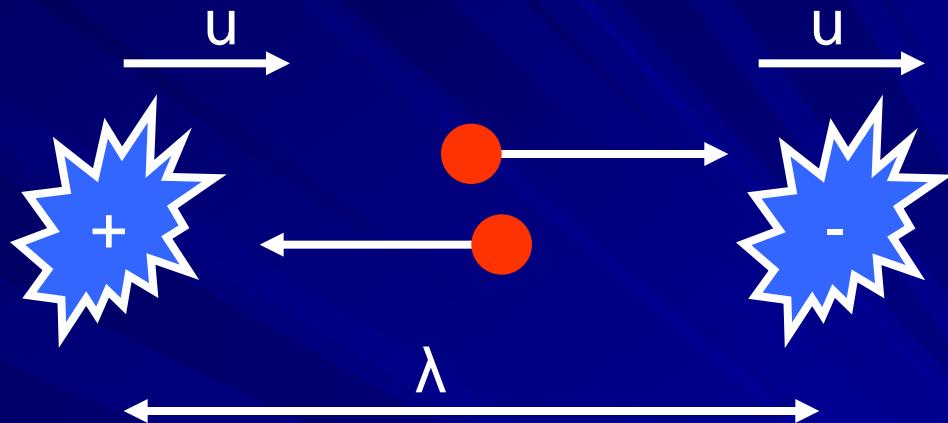
$> 10^7$ yrs





Second order Fermi Mechanisms

(Fermi 1949)



Frequency of collisions:

Energy gain per collisions:

Cosmic rays interact with magnetic turbulence

Cosmic Rays \longleftrightarrow Magnetized medium

In case of small angle scattering, Fokker-Planck equation can be used to describe the particles' evolution:

$$\frac{\partial F}{\partial t} + v\mu \underbrace{\frac{\partial F}{\partial Z}}_{\text{transport}} - \Omega \underbrace{\frac{\partial F}{\partial \phi}}_{\text{transport}} = S + \frac{1}{p^2} \frac{\partial}{\partial x} \left(p^2 D_{xy} \frac{\partial F}{\partial y} \right)$$

S : Sources and sinks of particles

2nd term on rhs: diffusion in phase space specified by
Fokker -Planck coefficients D_{xy}

Stochastic particle acceleration due to particle-mode coupling

(Book reviews : Melrose 1980, Berezinskii et al 1990,
Schlickeiser 2002)

The diffusion coefficients define characteristics of particle propagation and acceleration

Propagation $\nu = 2D_{\mu\mu}/(1 - \mu^2) \quad \lambda_{\parallel} = \frac{3}{4} \int d\mu \frac{v(1 - \mu^2)^2}{D_{\mu\mu}}$

Stochastic Acceleration $A(E) = \frac{\partial [vp^2 D(p)]}{4p^2 \partial p}, D(p) = \frac{1}{2} \int_{-1}^1 D_{pp} d\mu$

$$\boxed{D_{\mu\mu} \longleftrightarrow \delta B, \\ D_{pp} \longleftrightarrow \delta E = \delta v \times B_0/c}$$

Acceleration is sensitive to our model of turbulence

Where do δB , δv come from? MHD turbulence!

- The diffusion coefficients are determined by the statistical properties of turbulence

Stochastic acceleration of fast particles diffusing in turbulence (Ptuskin 1988)

$$D_{pp} \simeq \frac{2}{9} D p^2 \frac{V_o^2}{L_o^{2/3}} \int_{1/L_o}^{1/l_{cut}} \frac{dy y^{1/3}}{c_s^2 + D^2 y^2}$$

Stochastic particle acceleration due to particle-mode coupling

(Book reviews : Melrose 1980, Berezinskii et al 1990, Schlickeiser 2002)

The diffusion coefficients define characteristics of particle propagation and acceleration

Propagation $\nu = 2D_{\mu\mu}/(1 - \mu^2) \quad \lambda_{||} = \frac{3}{4} \int d\mu \frac{v(1 - \mu^2)^2}{D_{\mu\mu}}$

Stochastic Acceleration $A(E) = \frac{\partial [vp^2 D(p)]}{4p^2 \partial p}, D(p) = \frac{1}{2} \int_{-1}^1 D_{pp} d\mu$

$$\begin{aligned} D_{\mu\mu} &\leftarrow \delta B, \\ D_{pp} &\leftarrow \delta E = \delta v \times B_0/c \end{aligned}$$

Acceleration is sensitive to our model of turbulence

Where do δB , δv come from? MHD turbulence!

- The diffusion coefficients are determined by the statistical properties of turbulence

Stochastic acceleration of fast particles diffusing in turbulence (Ptuskin 1988)

$$D_{pp} \simeq \frac{2}{9} D p^2 \frac{V_o^2}{L_o^{2/3}} \int_{1/L_o}^{1/l_{cut}} \frac{dy y^{1/3}}{c_s^2 + D^2 y^2}$$

Gyroresonance scattering depends on the properties of turbulence

Gyroresonance

$$\omega - k_{||} v_{||} = n\Omega, \quad (n = \pm 1, \pm 2 \dots),$$

Which states that the MHD wave frequency (Doppler shifted) is a multiple of gyrofrequency of particles ($v_{||}$ is particle speed parallel to B).

So, $k_{||,res} \sim \Omega/v = 1/r_L$



Transit Time Damping (TTD)

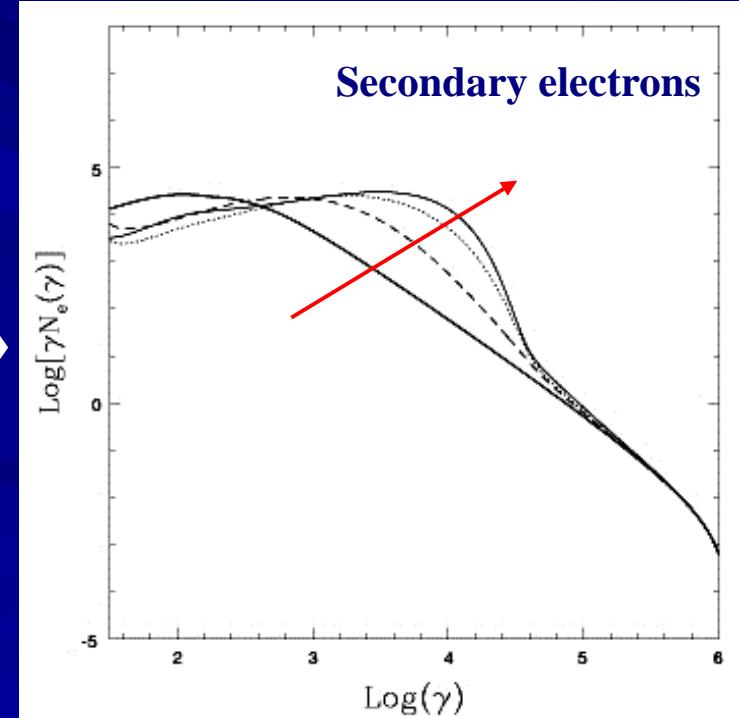
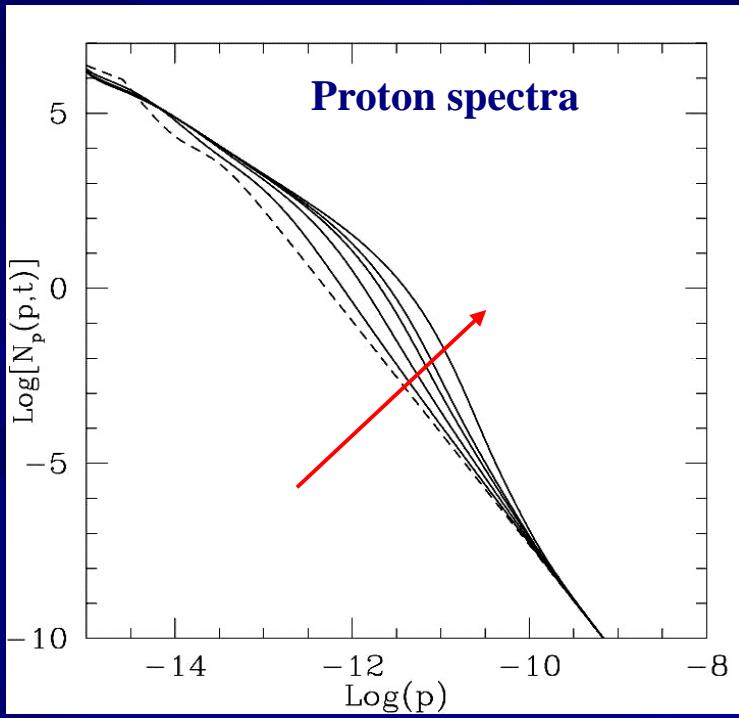
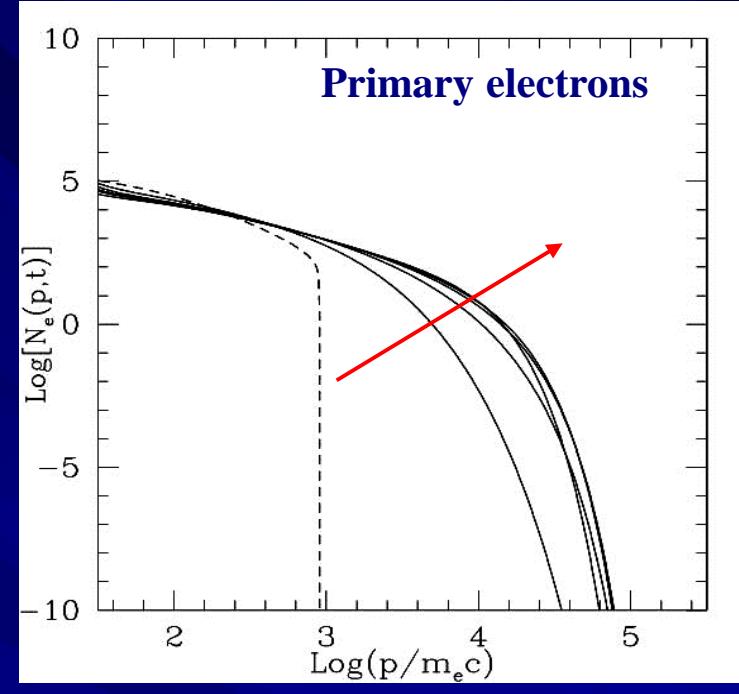
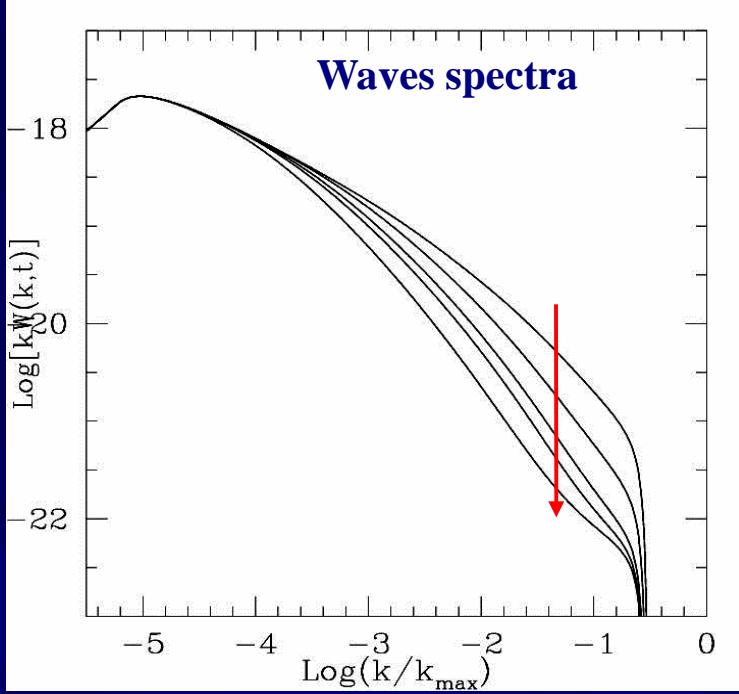
$$\omega - k_{||} v_{||} = 0$$

Interaction btw magnetic moment of particle and parallel gradient of B

Suitable for IGM !

Isotropic fast modes

(Cassano & Brunetti 05, Yan et al 10, Brunetti & Lazarian 07, 11)



Spectra of radio halos & turbulence

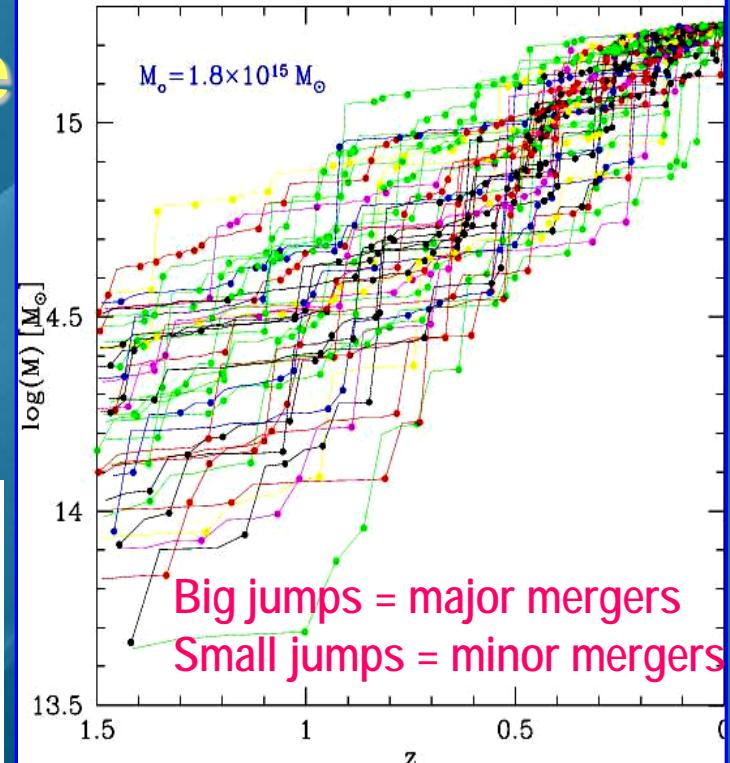
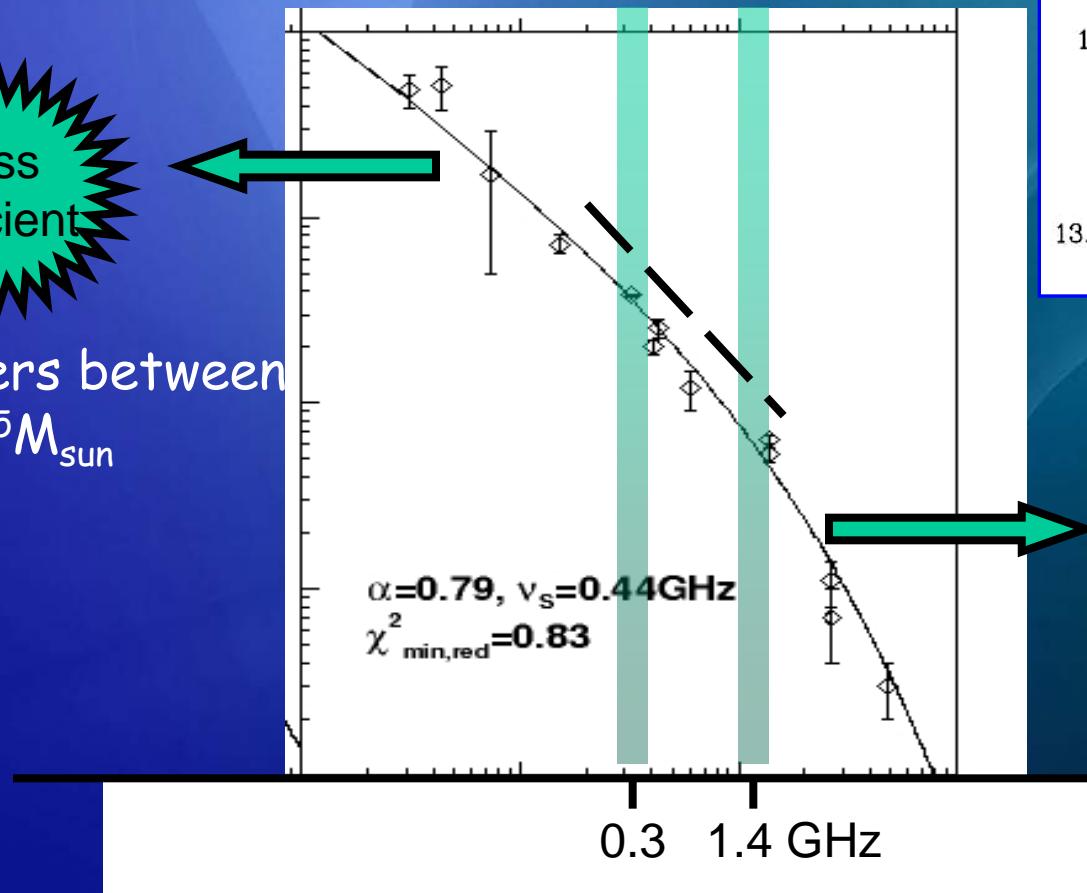
Steepening frequency

$$\nu_b \propto \langle B \rangle \gamma_{\max}^2 \propto \frac{\langle B \rangle \chi^2}{(\langle B \rangle^2 + B_{\text{cmb}}^2)^2}$$

$$\chi \approx 1/\tau_{acc}$$



Mergers between
 $M < 10^{15} M_{\text{sun}}$



Mergers between
 $M > 10^{15} M_{\text{sun}}$



Observed spectra of radio halos & turbulence

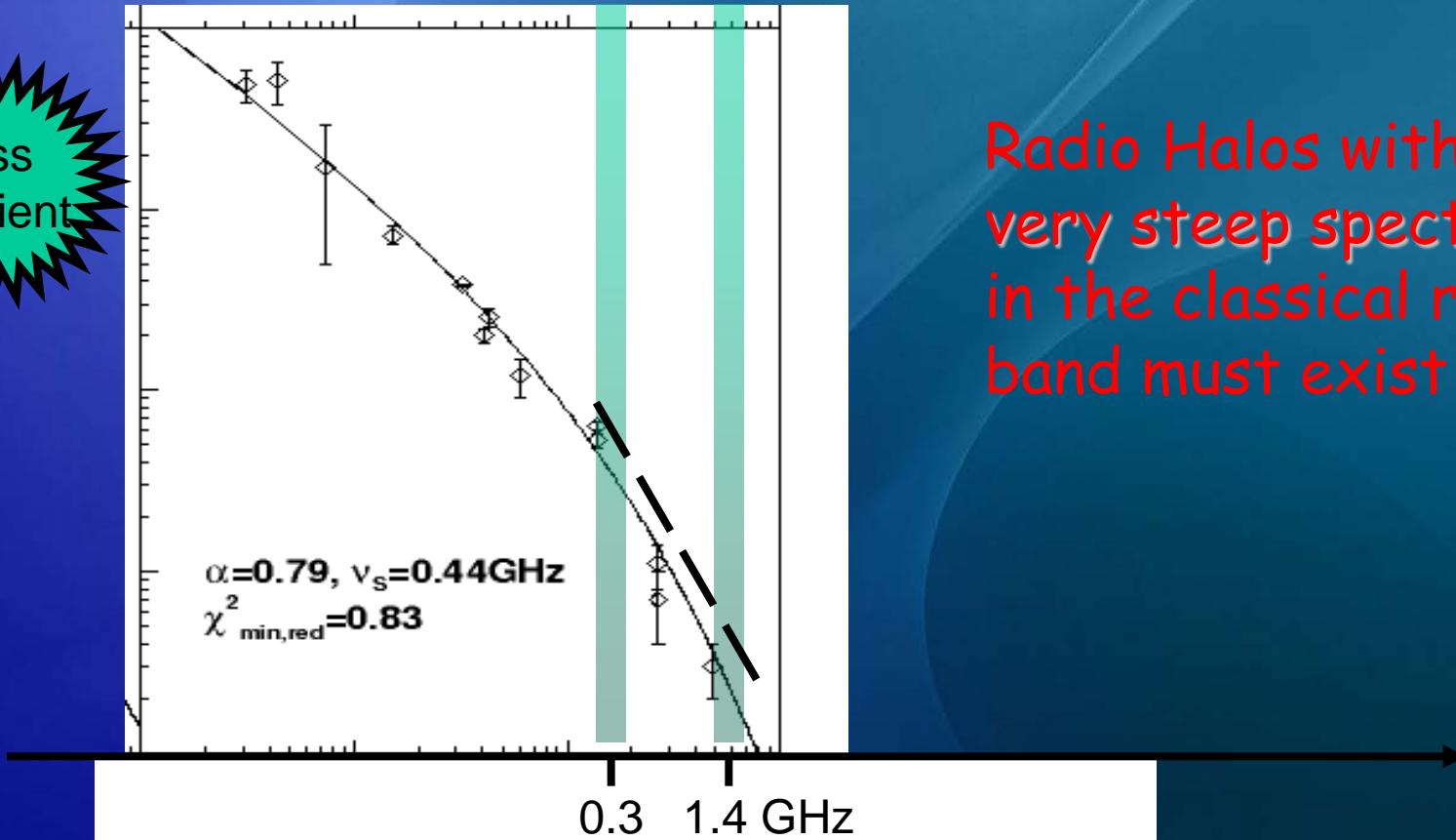
Cassano, GB, Setti (2006)

Steepening frequency

$$\nu_b \propto \langle B \rangle \gamma_{\max}^2 \propto \frac{\langle B \rangle \chi^2}{(\langle B \rangle^2 + B_{\text{cmb}}^2)^{\frac{1}{2}}}$$

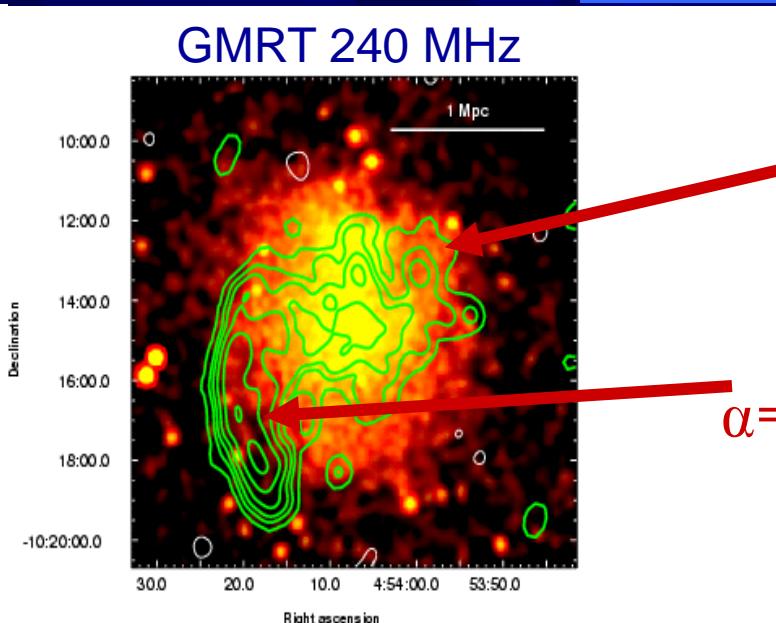
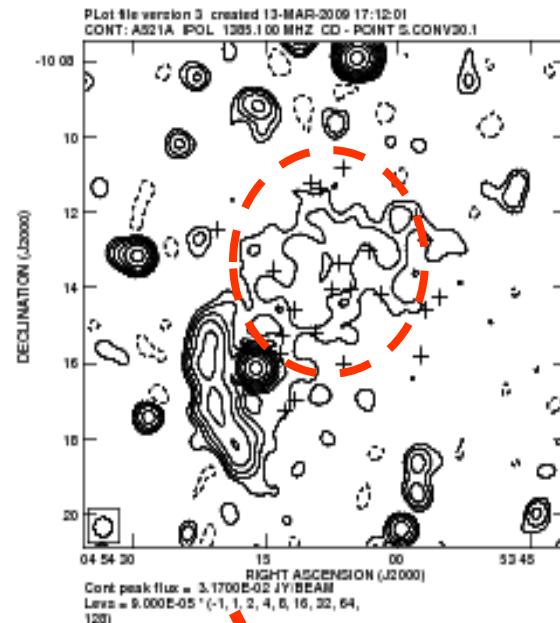
$$\chi \approx 1/\tau_{acc}$$

less
efficient



Turbulent acceleration?

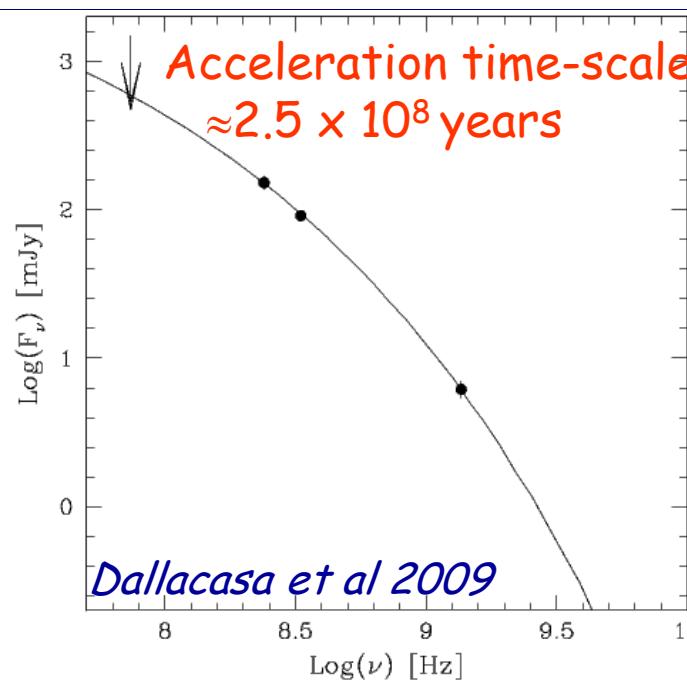
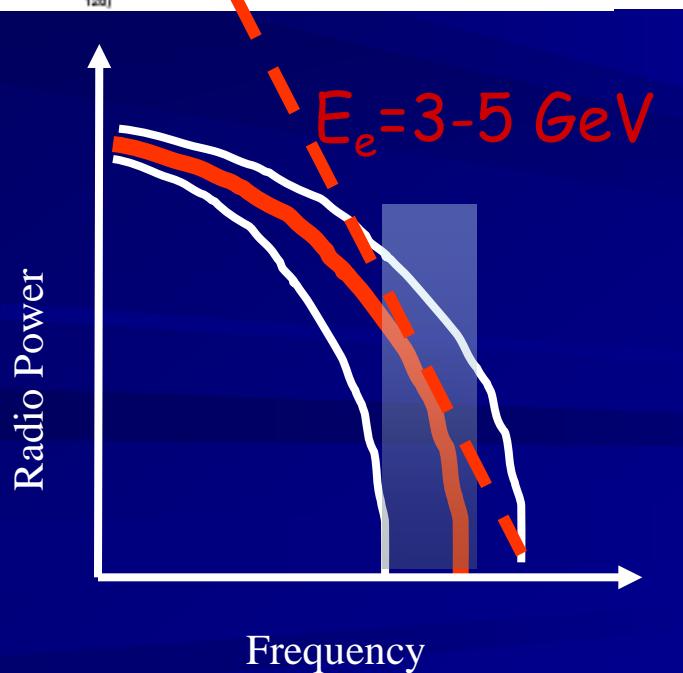
Brunetti +al 2008, Nature 455, 944



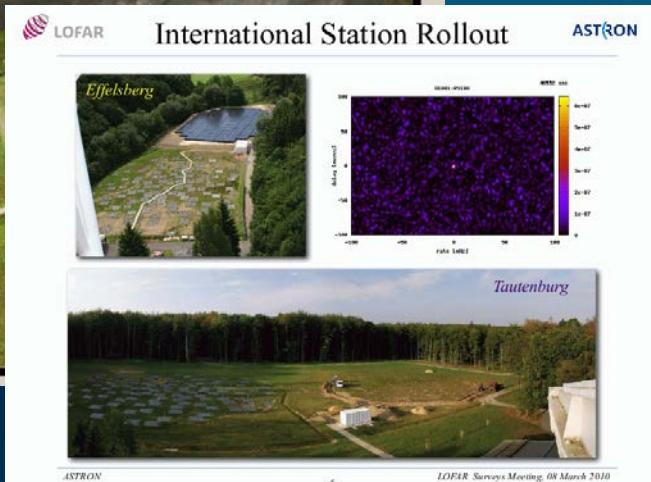
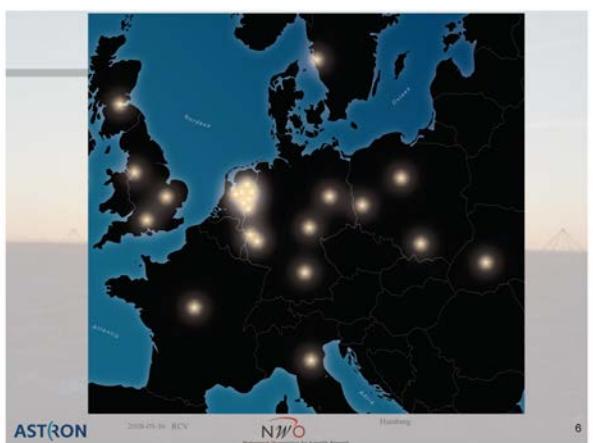
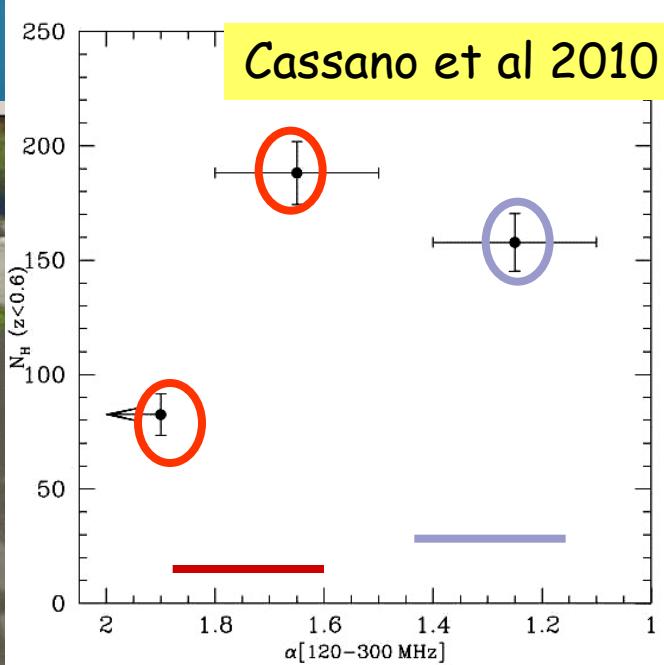
$$N(E) = k E^{-4.8}$$

$\alpha = 1.9$

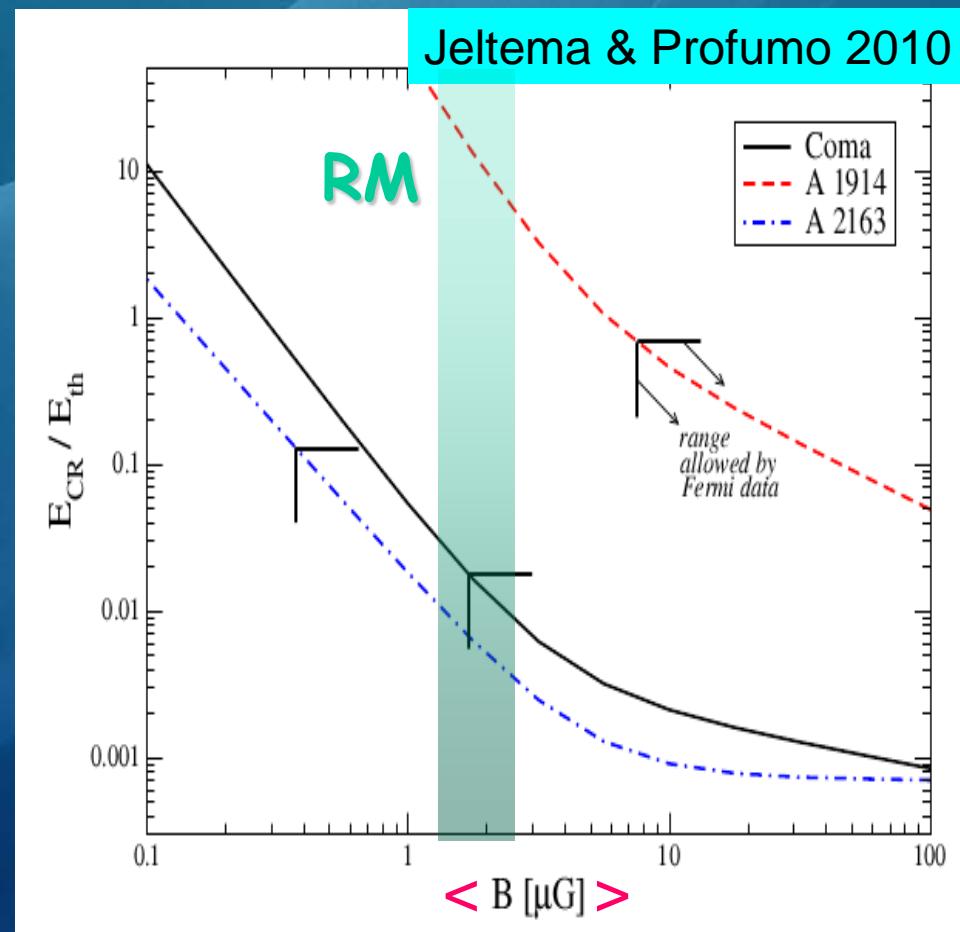
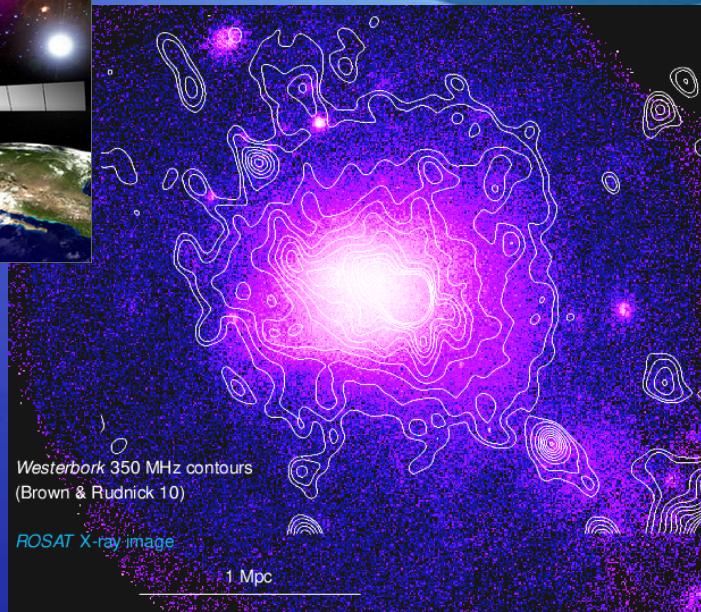
$\alpha = 1.5$



LOFAR ...



Gamma rays : energy content of CRp & origin of Radio Halos

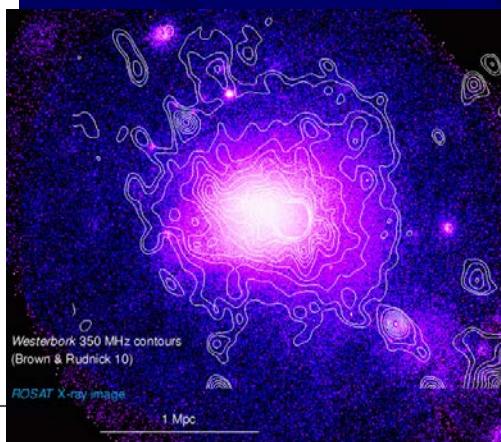
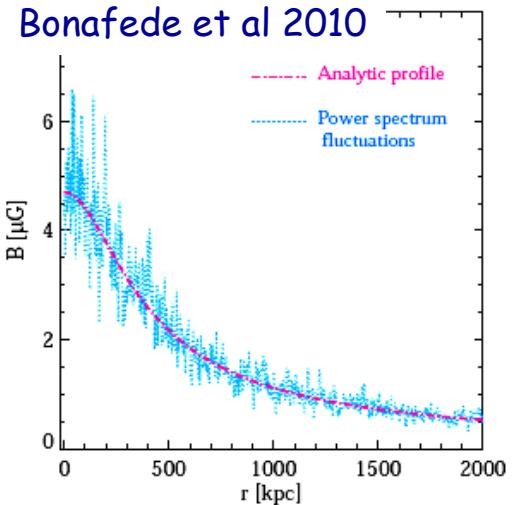


$$L_{\gamma,\pi} \sim f_\gamma(\delta) \langle E_{CR} \rangle \langle E_{th}/T \rangle V_\gamma$$

$$L_R \sim f_R(\delta) \langle E_{CR} \rangle \langle E_{th}/T \rangle \langle B^{\delta/2+1}/(B^2+B_{cmb}^2) \rangle V_R$$

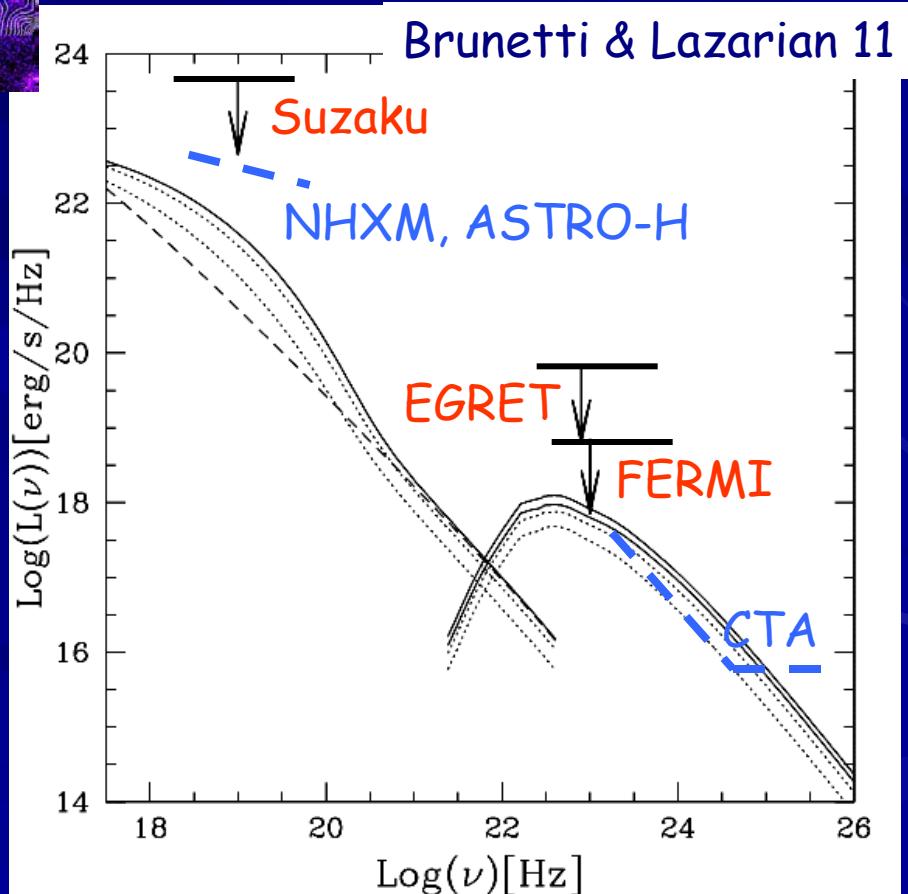
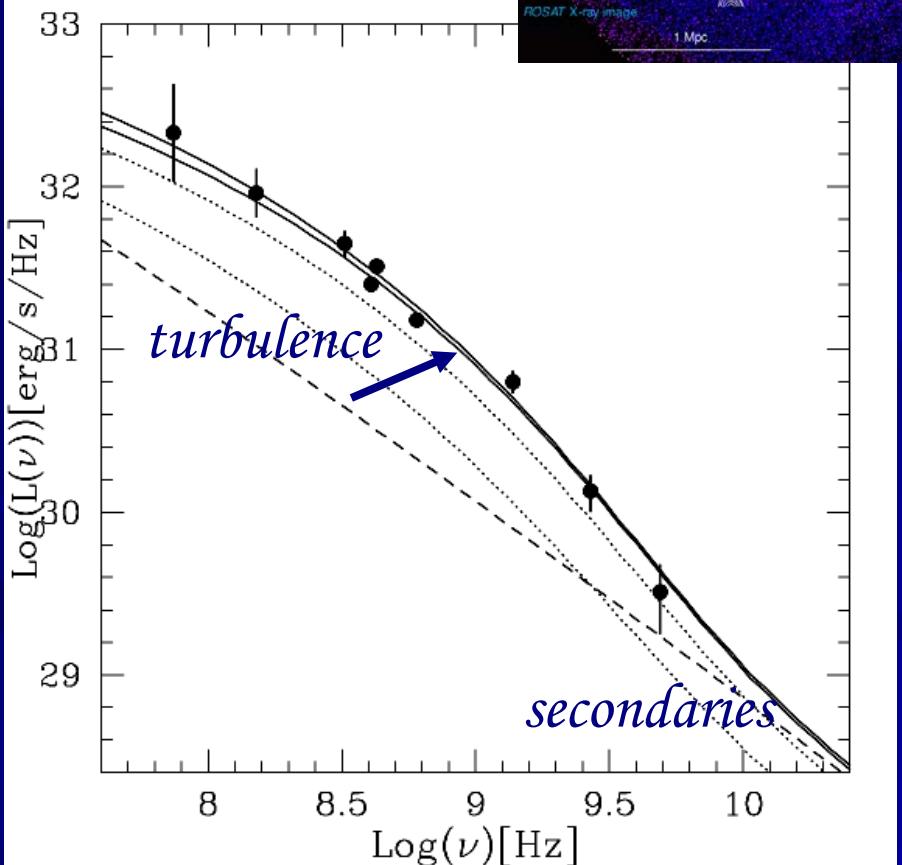
$$L_R / L_{\gamma,\pi} \rightarrow \langle B^{\delta/2+1}/(B^2+B_{cmb}^2) \rangle \quad \text{Also Donnert et al 10, Brunetti et al ...}$$

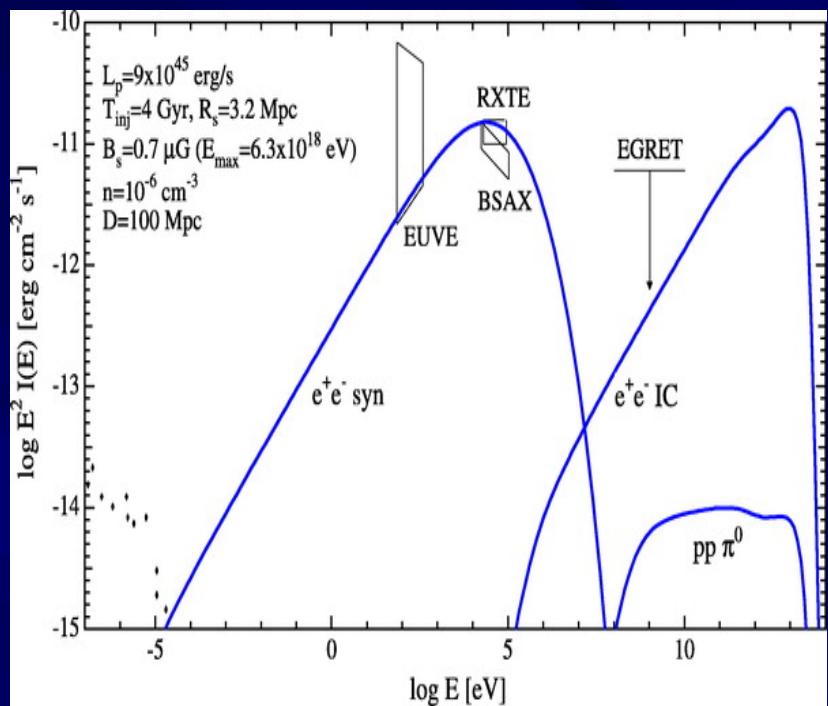
Bonafede et al 2010



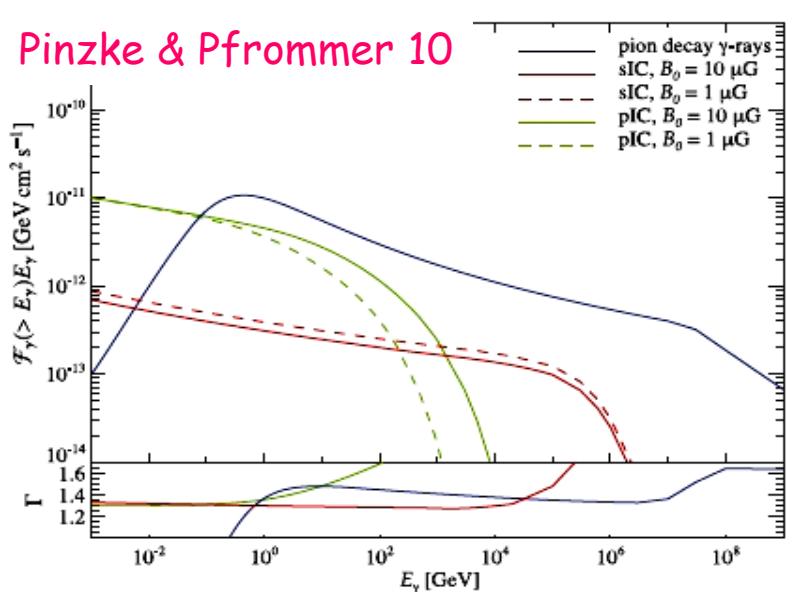
Turbulent models and Coma SED

$$E_{\text{tur}} \approx 10 \% E_{\text{th}} \quad @ k^{-1} \sim 100 \text{ kpc}$$
$$E_{\text{CR}} = 3 \% E_{\text{th}} \quad (\text{flat profile})$$

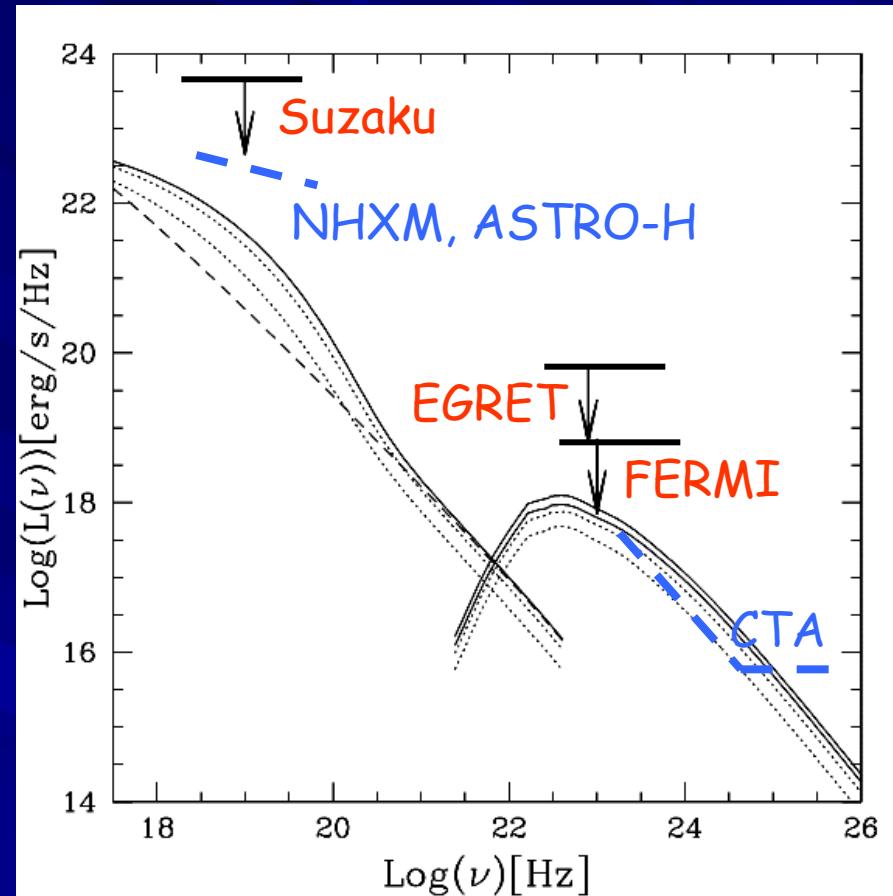




Pinzke & Pfrommer 10



Additional processes



If B is smaller than that estimated from RM (reasonable?) ... more gamma rays

