

RM Synthesis: Application to (Spiral) Galaxies

George Heald, Robert Braun & Rainer Beck
DFG RU 1254 Kickoff, Irsee
4 October 2010



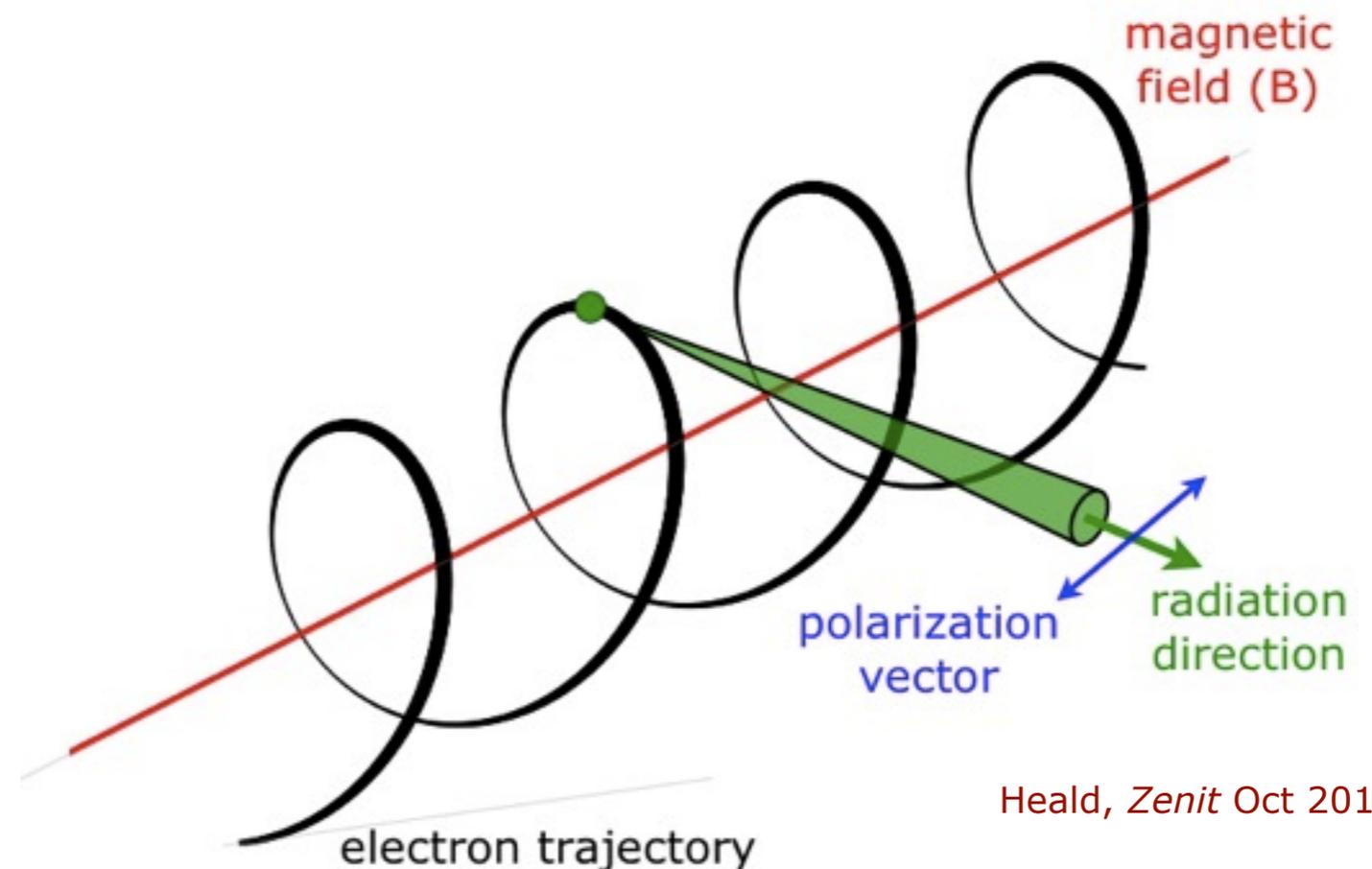


- Review of the RM Synthesis technique
 - WSRT-SINGS: data & analysis
 - Trends in the WSRT-SINGS observations
 - Interpretation: global magnetic field geometry in spiral galaxies
 - Predictions and future work
-
- See:
 - Brentjens & de Bruyn 2005 (A&A, 441, 1217) [RM Synthesis]
 - Braun et al. 2007 (A&A, 461, 455) [WSRT-SINGS survey description]
 - Heald et al. 2009 (A&A, 503, 409) [WSRT-SINGS polarization data analysis]
 - Braun et al. 2010 (A&A, 514, 42) [Global magnetic field geometries]



- cosmic ray electrons spiraling around magnetic field lines
- beamed radiation in direction of electron motion
- linearly polarized perpendicular to magnetic field
- continuum radiation with power law index related to power law index of electron energy spectrum

Polarized synchrotron radiation traces B_{\perp}

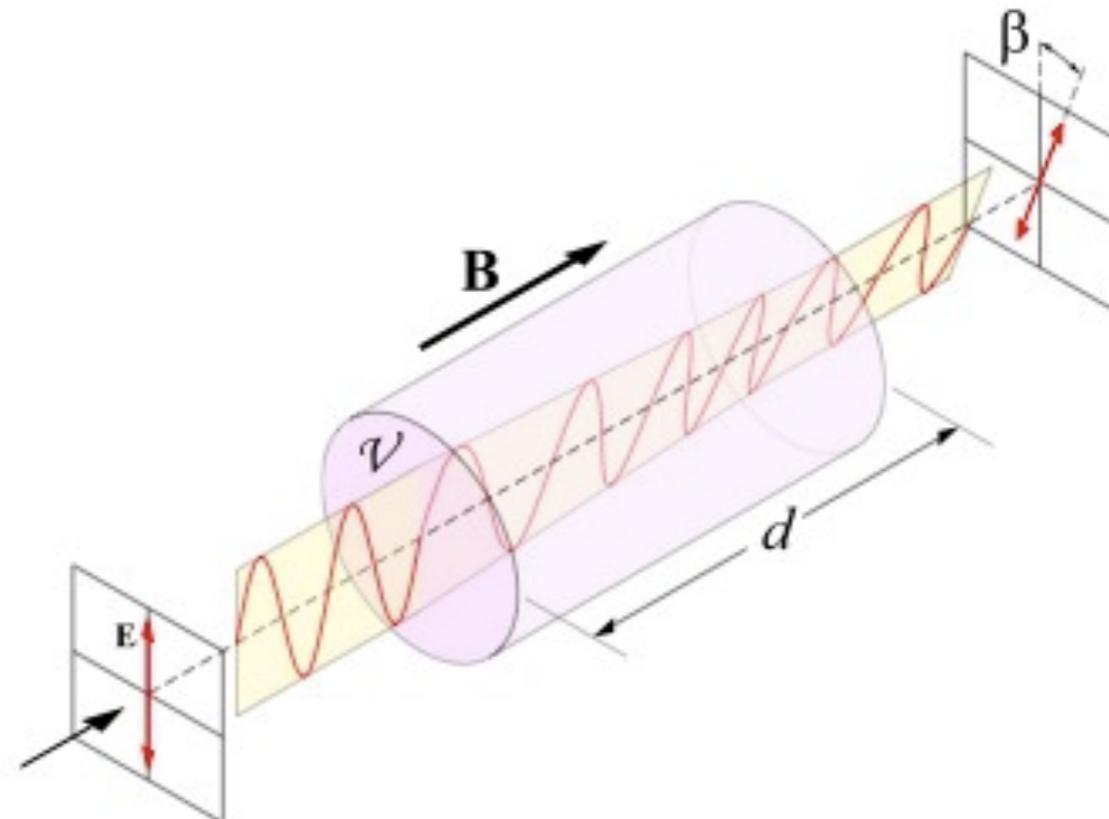


Heald, *Zenit* Oct 2010



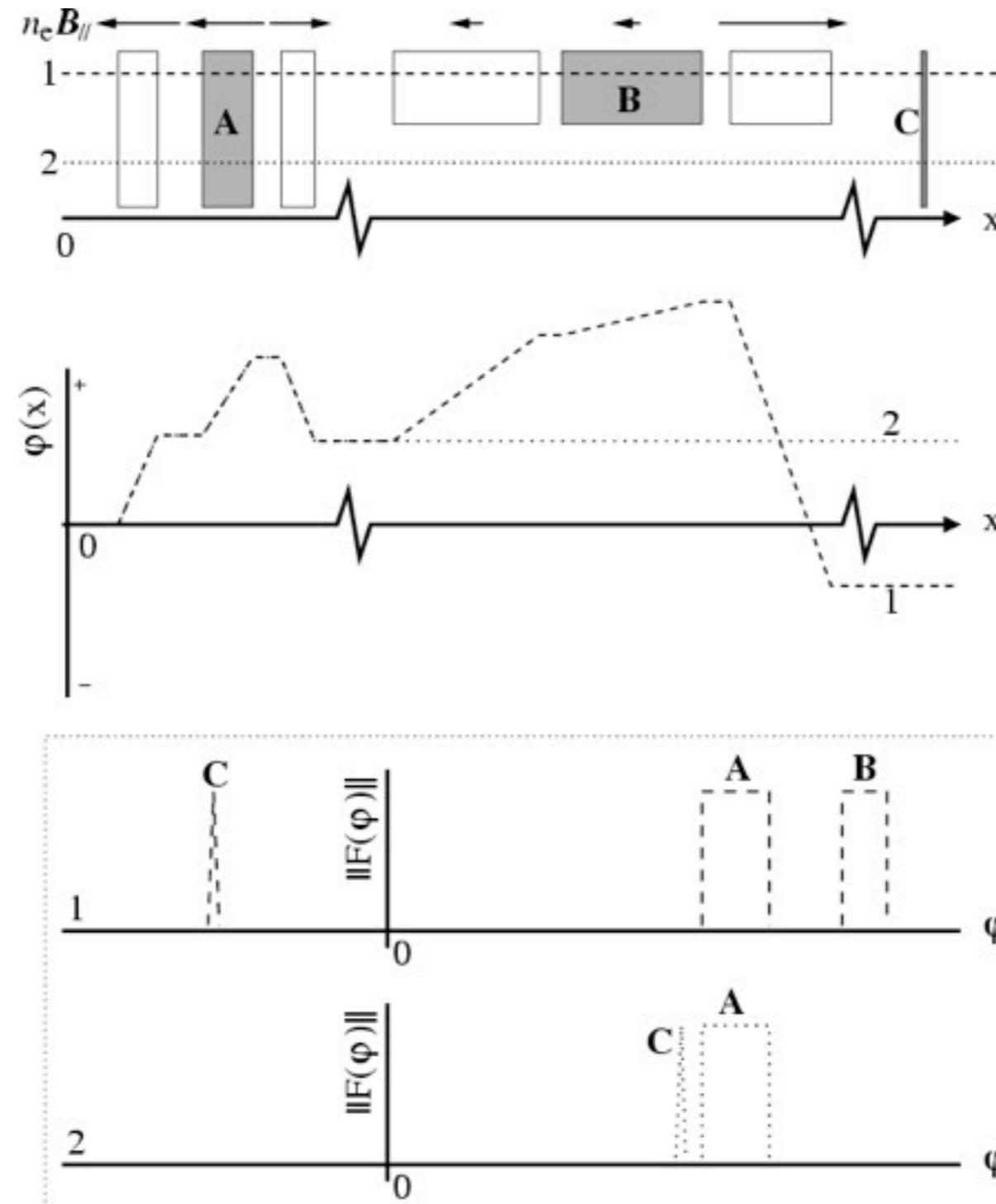
- Magnetized plasma is birefringent - causes Faraday rotation
- Speed of light different for right and left circular polarization
- Because RL phase difference is determined by
 - difference in c for R,L
 - wavelength of radiation
- and RL phase difference determines the polarization angle, we get a frequency-dependent change in linear polarization angle

Faraday rotation
traces $B_{||}$





- Not directly related to physical depth!



Brentjens & de Bruyn (2005)



- Depth depolarization / turbulent depolarization
- Beam depolarization
- Bandwidth depolarization

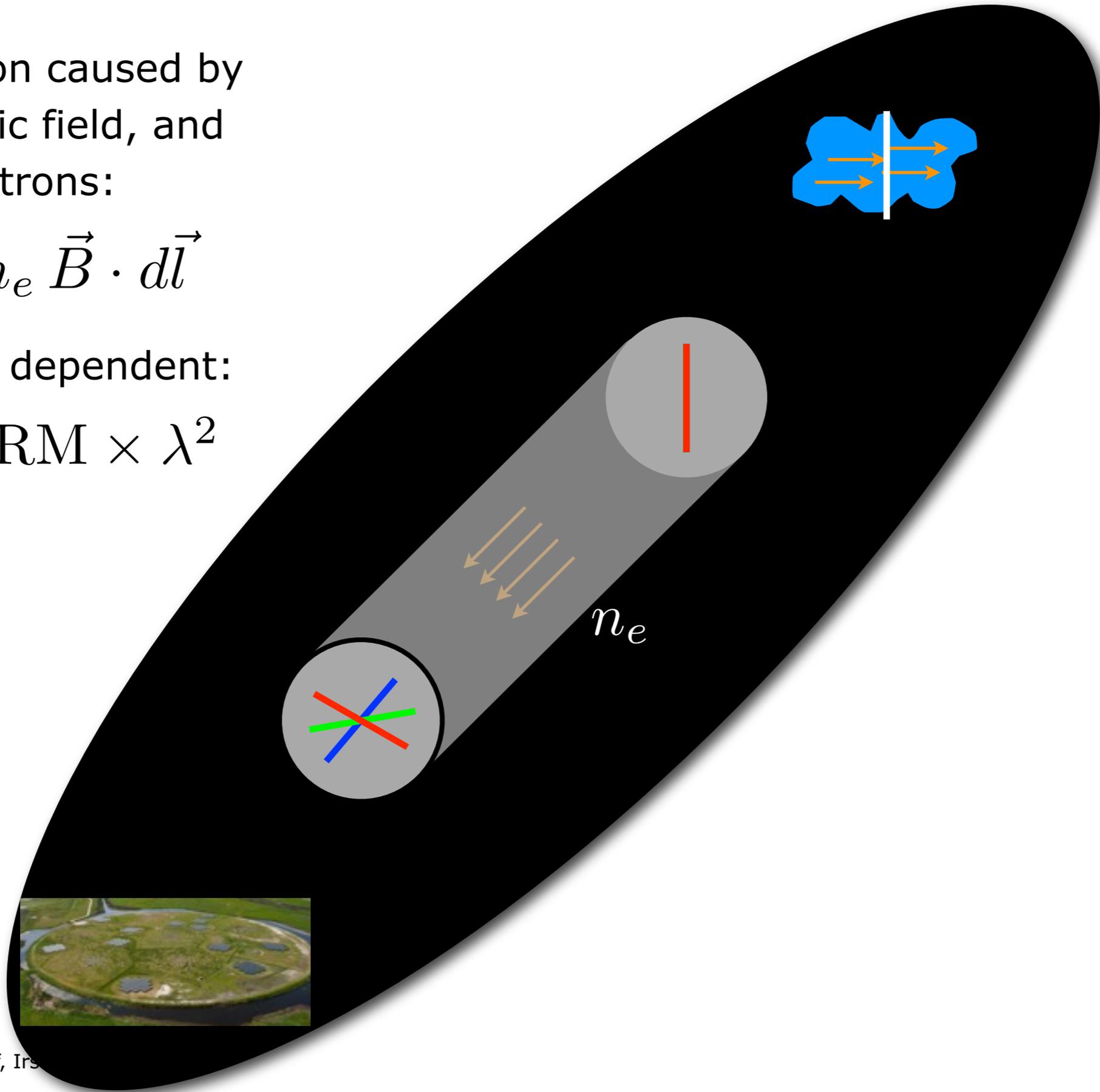


- Faraday rotation caused by LOS magnetic field, and thermal electrons:

$$\text{RM} \propto \int n_e \vec{B} \cdot d\vec{l}$$

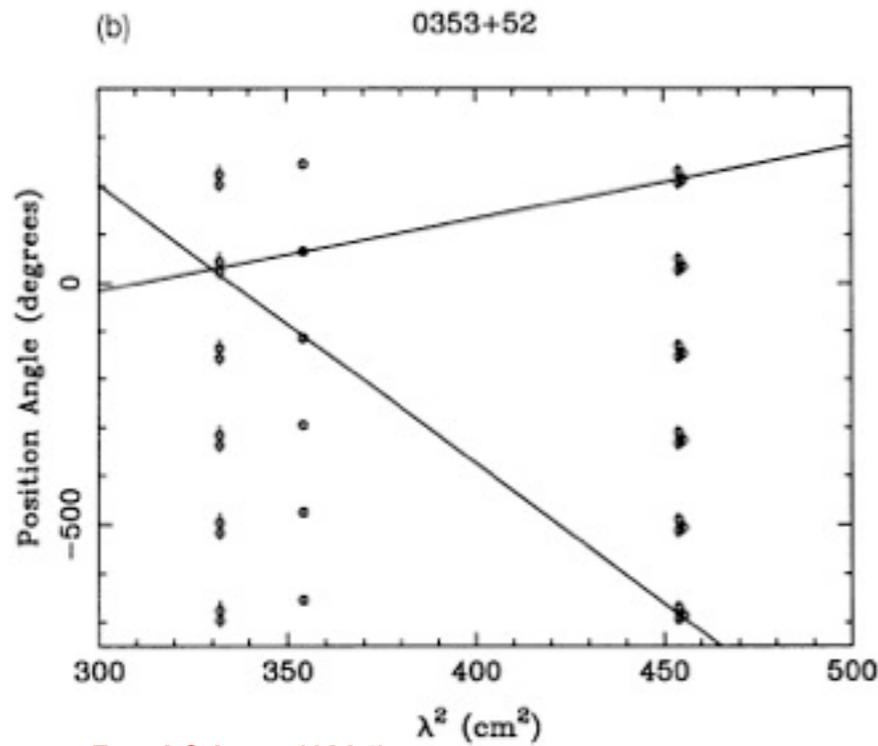
- It is frequency dependent:

$$\chi = \chi_0 + \text{RM} \times \lambda^2$$



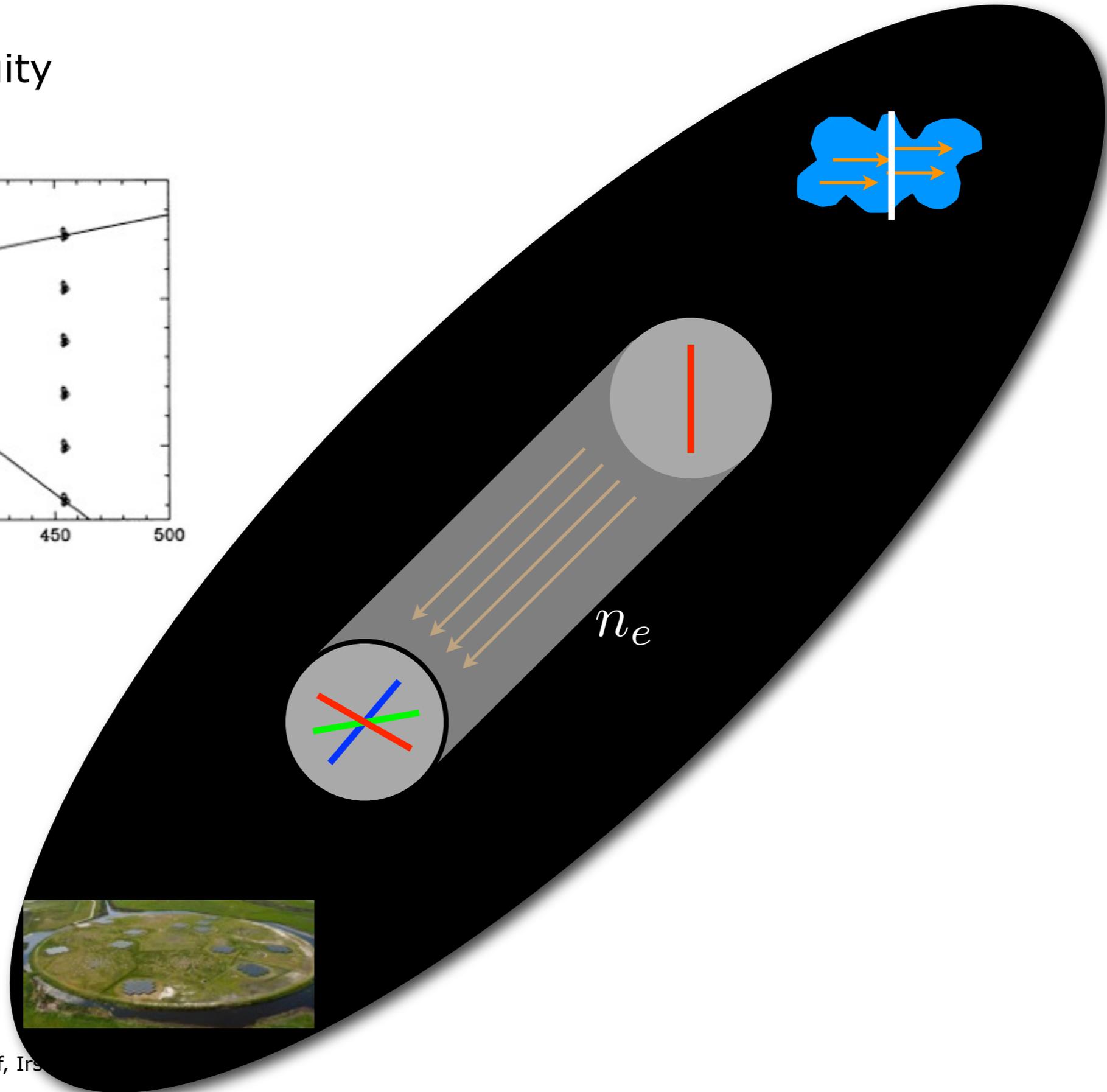


- The $n\pi$ ambiguity



Rand & Lyne (1994)

RM synthesis was developed to combat this problem.





- Polarization vector:

$$\vec{P} = p I e^{2i\chi}$$

but since

$$\chi = \text{RM} \times \lambda^2$$

and redefining

$$\phi \equiv \text{RM}$$

where ϕ is the “Faraday depth”, we can write a more general expression

$$P(\lambda^2) = \int_{-\infty}^{+\infty} F(\phi) e^{2i\phi\lambda^2} d\phi$$

(Burn 1966)

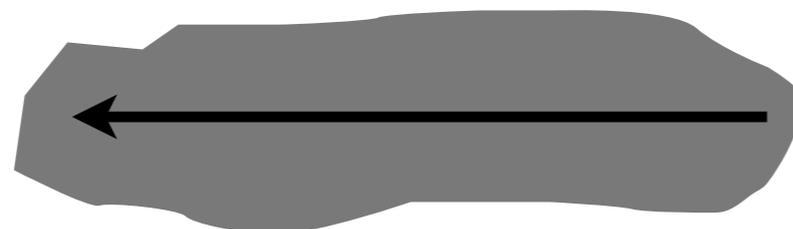


- Generic form of the expression for rotation measure is (Burn 1966):

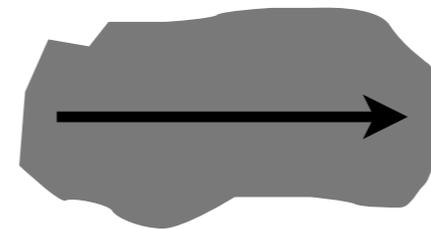
$$P(\lambda^2) = \int_{-\infty}^{+\infty} F(\phi) e^{2i\phi\lambda^2} d\phi$$

where ϕ (the **Faraday depth**) has taken the place of RM, and F is the **Faraday dispersion function**.

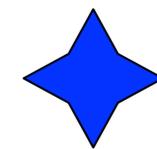
- Faraday dispersion function of a Burn slab is a tophat function.
- Note: Faraday depth is **not** the same as physical depth! (Hence "2.5D")
Nor is it like optical depth.



4 rad/m²



-2 rad/m²





- The equation

$$P(\lambda^2) = \int_{-\infty}^{+\infty} F(\phi) e^{2i\phi\lambda^2} d\phi$$

is like a Fourier transform, and can (in principle) be inverted to determine the physical situation from the observables.

- However there are some complications:
 - We do not measure $\lambda^2 < 0$
 - We do not measure all $\lambda^2 > 0$



- This leads to a sampling (window) function, and to a finite point spread function (called the **Rotation Measure Spread Function, or RMSF**). Examples are shown in following slides.

- The formal expression

$$P(\lambda^2) = \int_{-\infty}^{+\infty} F(\phi) e^{2i\phi\lambda^2} d\phi$$

becomes

$$\tilde{P}(\lambda^2) = W(\lambda^2) \int_{-\infty}^{+\infty} F(\phi) e^{2i\phi\lambda^2} d\phi$$

This can be inverted (note the addition of λ_0^2):

$$\tilde{F}(\phi) = K \int_{-\infty}^{+\infty} \tilde{P}(\lambda^2) e^{-2i\phi(\lambda^2 - \lambda_0^2)} d\lambda^2 = F(\phi) * R(\phi) \neq F(\phi)$$



- The expression for the (reconstructed) Faraday dispersion function

$$\tilde{F}(\phi) = K \int_{-\infty}^{+\infty} \tilde{P}(\lambda^2) e^{-2i\phi(\lambda^2 - \lambda_0^2)} d\lambda^2$$

can be written as a sum (if channel width is small),

$$\tilde{F}(\phi) = K \sum_{c=1}^N \tilde{P}_c e^{-2i\phi(\lambda_c^2 - \lambda_0^2)}$$

("trial RM" interpretation)

- The RMSF is then

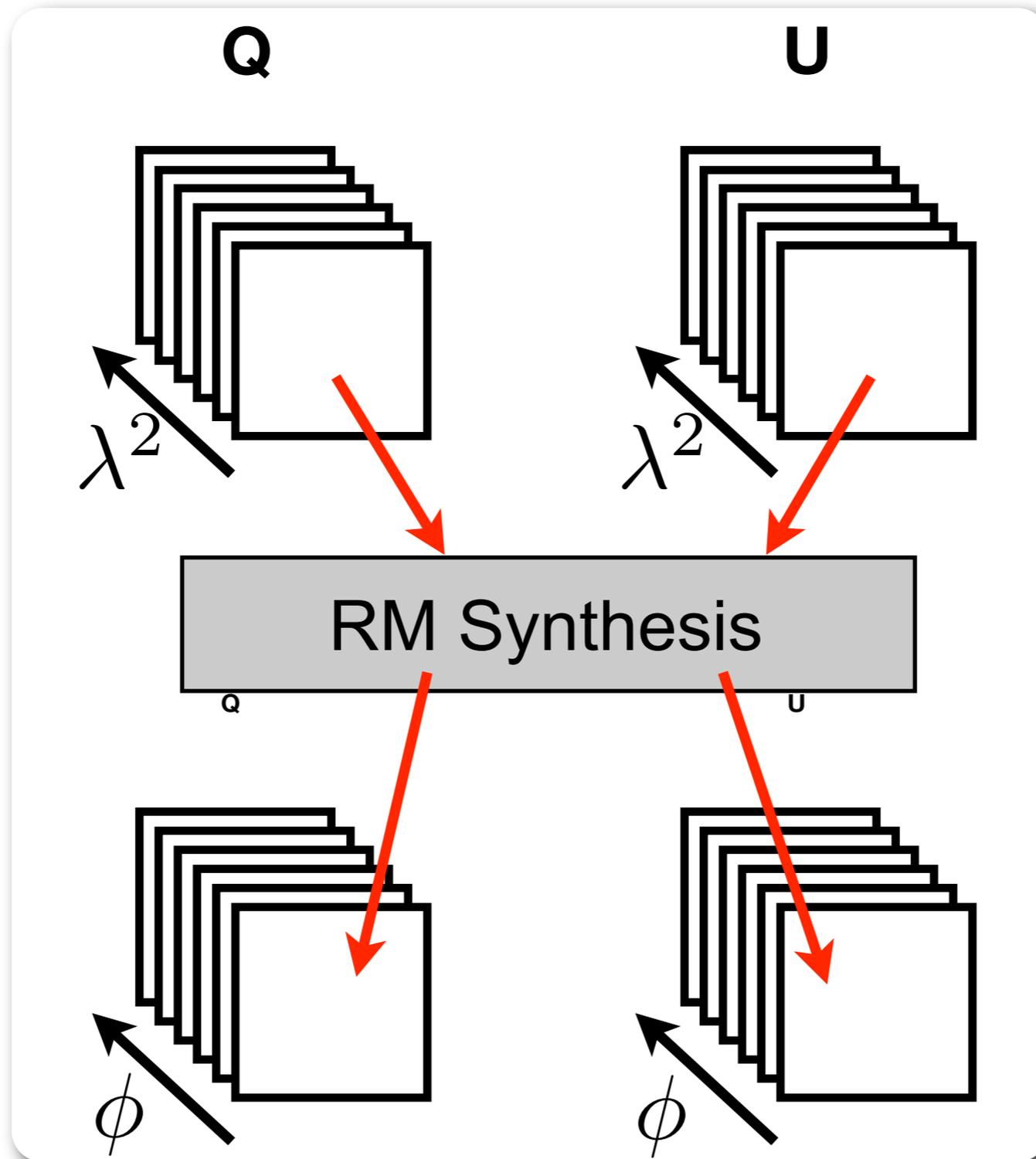
$$R(\phi) = K \sum_{c=1}^N w_c e^{-2i\phi(\lambda_c^2 - \lambda_0^2)}$$

$$K = \left(\sum_{c=1}^N w_c \right)^{-1}$$

- This operation can be done for a whole field of view (producing an **RM-cube**).



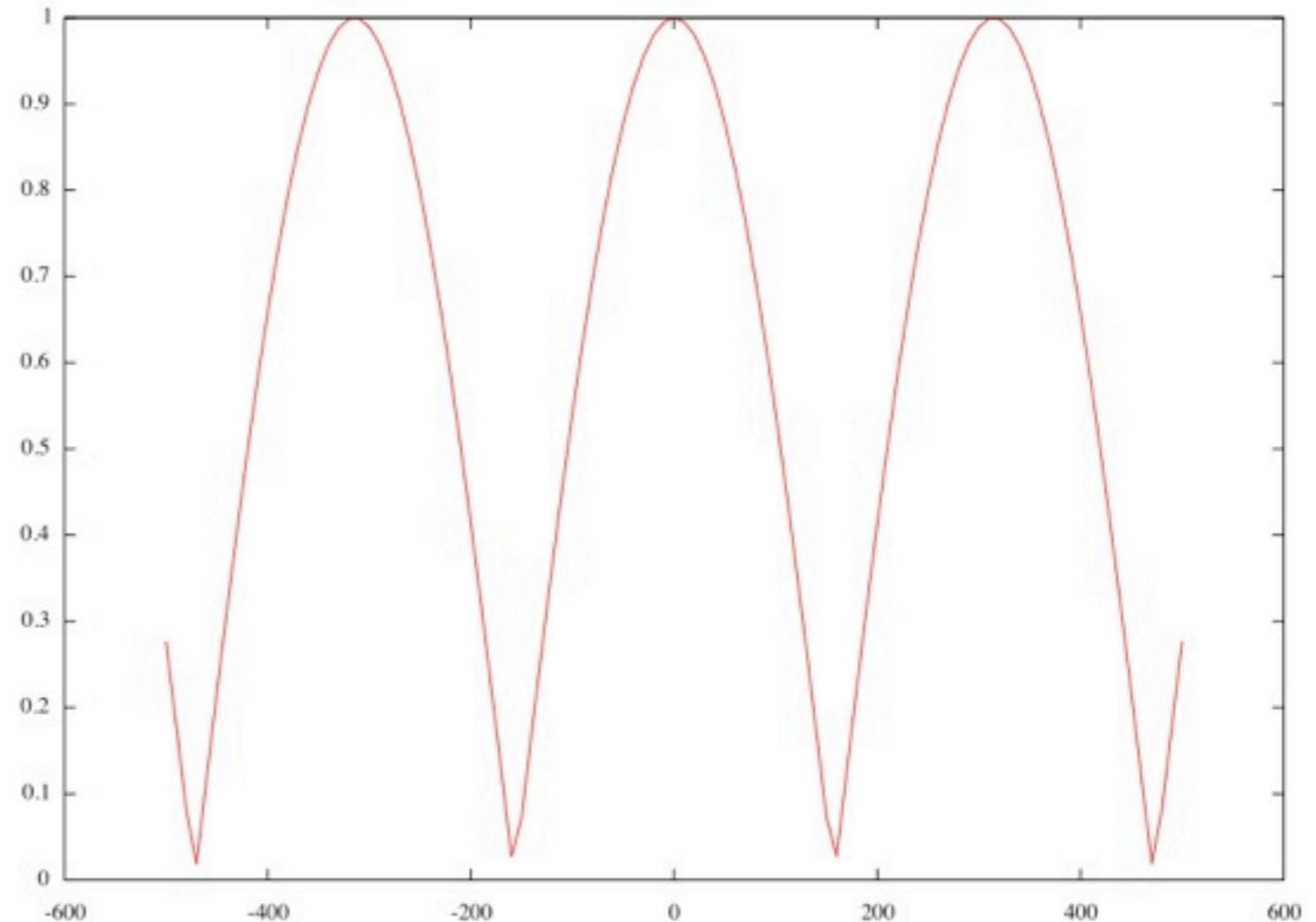
- RM synthesis works on observed Q,U cubes to produce **RM-cubes**:





- Example, two observing bands: 18cm + 21cm
 $\lambda^2 = .0355, .0455 \text{ m}^2$
- If observed $d\chi = \pi$
- $n\pi$ ambiguity becomes
 $\pi/.01 = 314 \text{ rad/m}^2$
- Fringes in RMSF are exactly spaced by this amount.
- If RM synthesis gives same as traditional method, why bother?
- As with visibilities, do **not** need to detect sources in every channel. The transform maximizes S/N.

$$R(\phi) = K \sum_{c=1}^N w_c e^{-2i\phi(\lambda_c^2 - \lambda_0^2)}$$





- Example, two observing bands: 18cm + 22cm with 512 channels per band

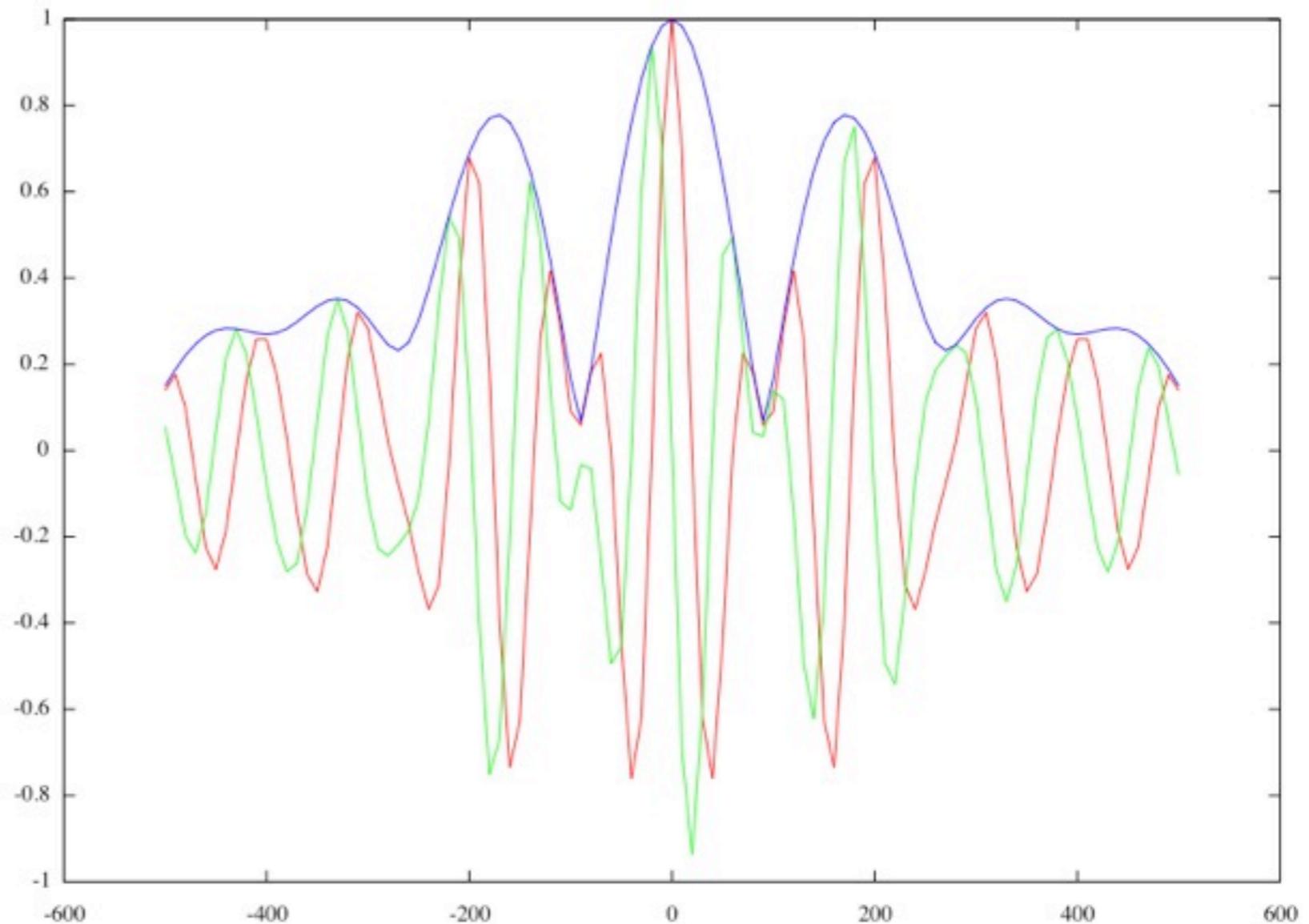
$$R(\phi) = K \sum_{c=1}^N w_c e^{-2i\phi(\lambda_c^2 - \lambda_0^2)}$$

real (Q)

imaginary (U)

absolute value (P)

- One can show that the optimal value of λ_0^2 is the weighted mean of the sampled λ^2 values (Brentjens & de Bruyn 2005)





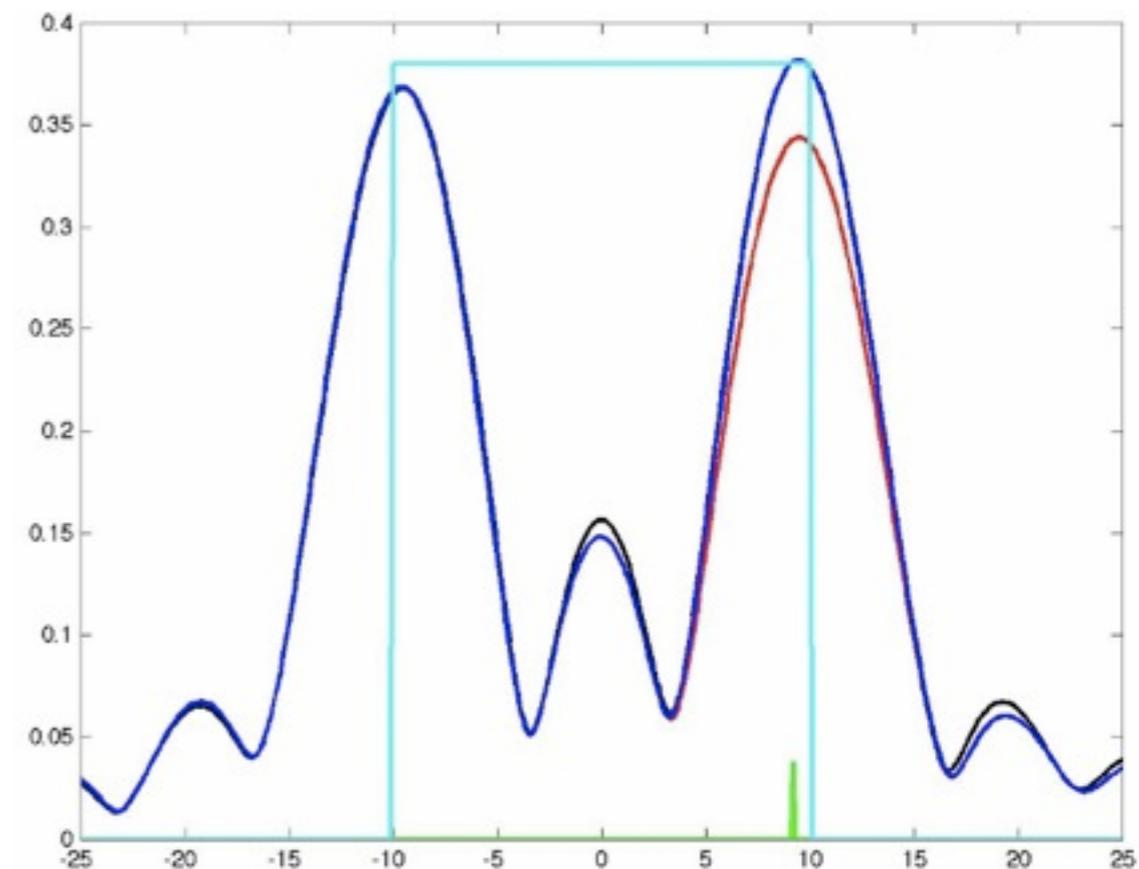
- From Brentjens & de Bruyn (2005):

$$\sigma_{\phi}^2 = \frac{\sigma^2}{4(N-2) \|P\|^2 \sigma_{\lambda^2}^2}$$

- Precision in RM determination is achieved by
 - low noise per channel
 - many channels
 - broad frequency (actually, wavelength squared) coverage



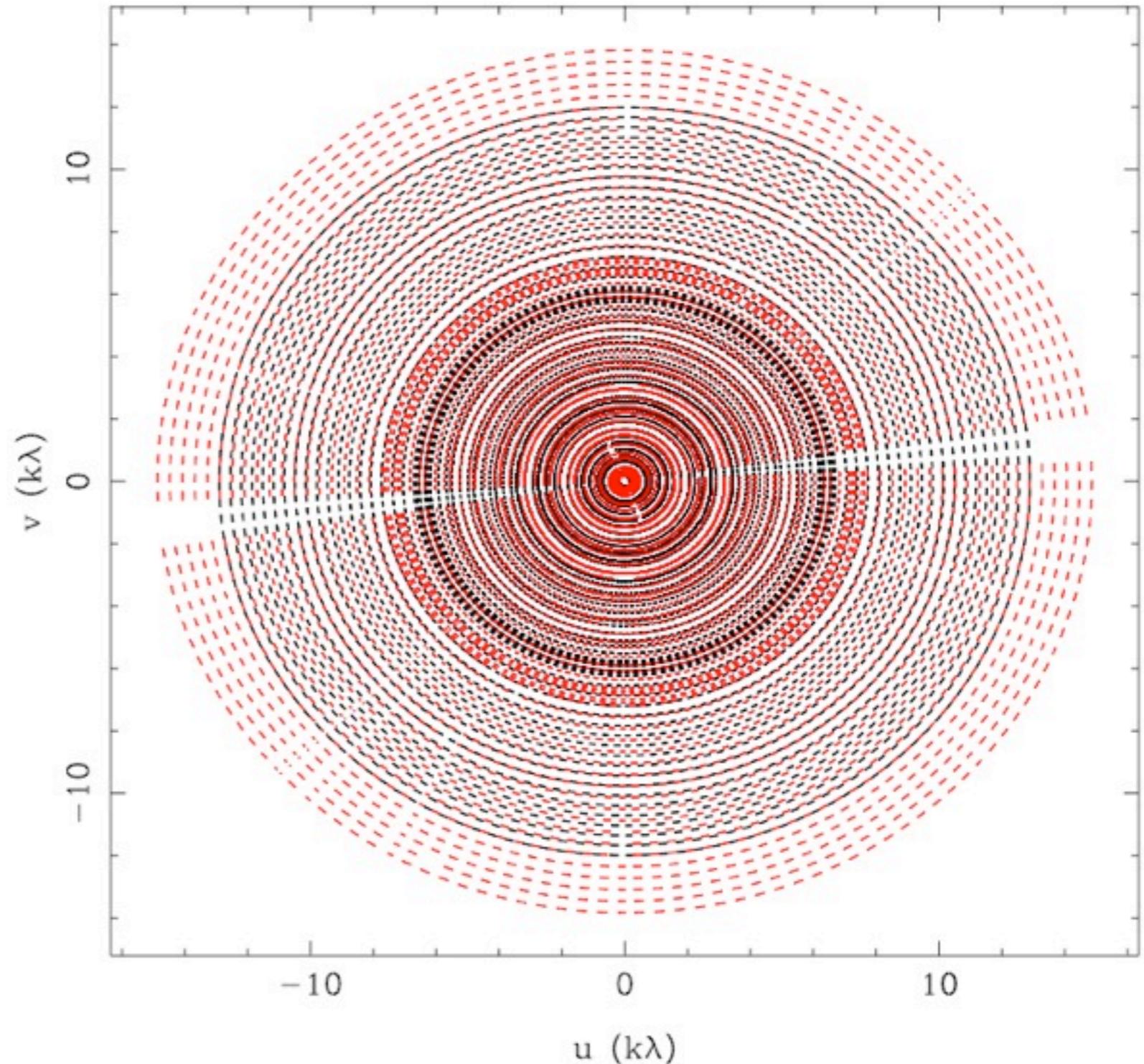
- The performance of RM synthesis is **strongly** dependent on the frequency coverage of the observations.
- Key characteristics:
 - Width of RMSF: sensitivity to weak magnetic fields: $\propto \Delta\lambda^2$ (full coverage)
 - Sensitivity to extended Faraday structures (e.g. Burn slabs): $\propto 1/(\min \lambda^2)$
 - Maximum rotation measure before bandwidth depolarization: $\propto 1/\delta\lambda^2$
 - Sidelobe level: “smoothness” of λ^2 coverage (avoid gaps!!)





- Because of the RMSF, the recovered FDF **must** be deconvolved in situations where multiple components are present
- Technique:
 - Find the peak in the reconstructed Faraday dispersion function
 - Subtract a scaled version of the RMSF, centered at that location
 - Store a delta-function component at that location
 - Iterate until noise floor is reached
 - Convolve delta-function model with restoring RMSF, and add residuals

- 2 broad (160 MHz) bands at 18cm and 22cm (high Faraday depth regime)
- Typical noise levels $\sim 10 \mu\text{Jy}/\text{beam rms}$ (6h/galaxy/band)

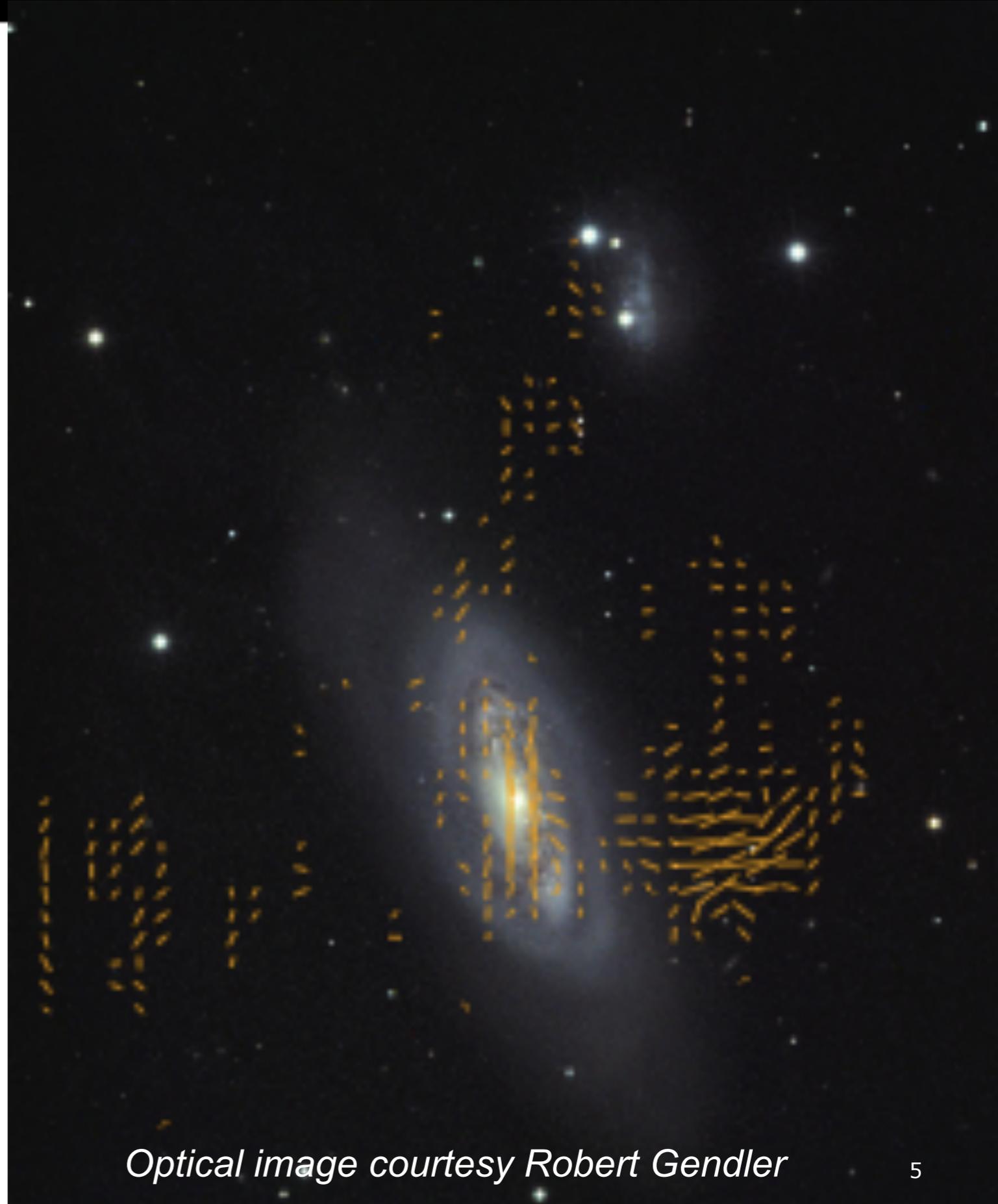




- Data analysed using Rotation Measure Synthesis (RM Synthesis) (see Brentjens & de Bruyn 2005)
 - Fourier transform of observed Stokes (Q,U) over wavelength-squared; provides complex polarization vector as a function of Faraday depth
 - Avoids $n\pi$ ambiguity problems (given sufficient frequency sampling)
 - Coherently adds across the full band, optimizing sensitivity regardless of rotation measure value
- RMSF FWHM $\sim 144 \text{ rad/m}^2$
- Faraday dispersion functions deconvolved using RM-CLEAN (see Heald et al. 2009; code available online)
- Polarized flux and rotation measure values extracted using moment-map techniques standard in the emission line (e.g. HI) community



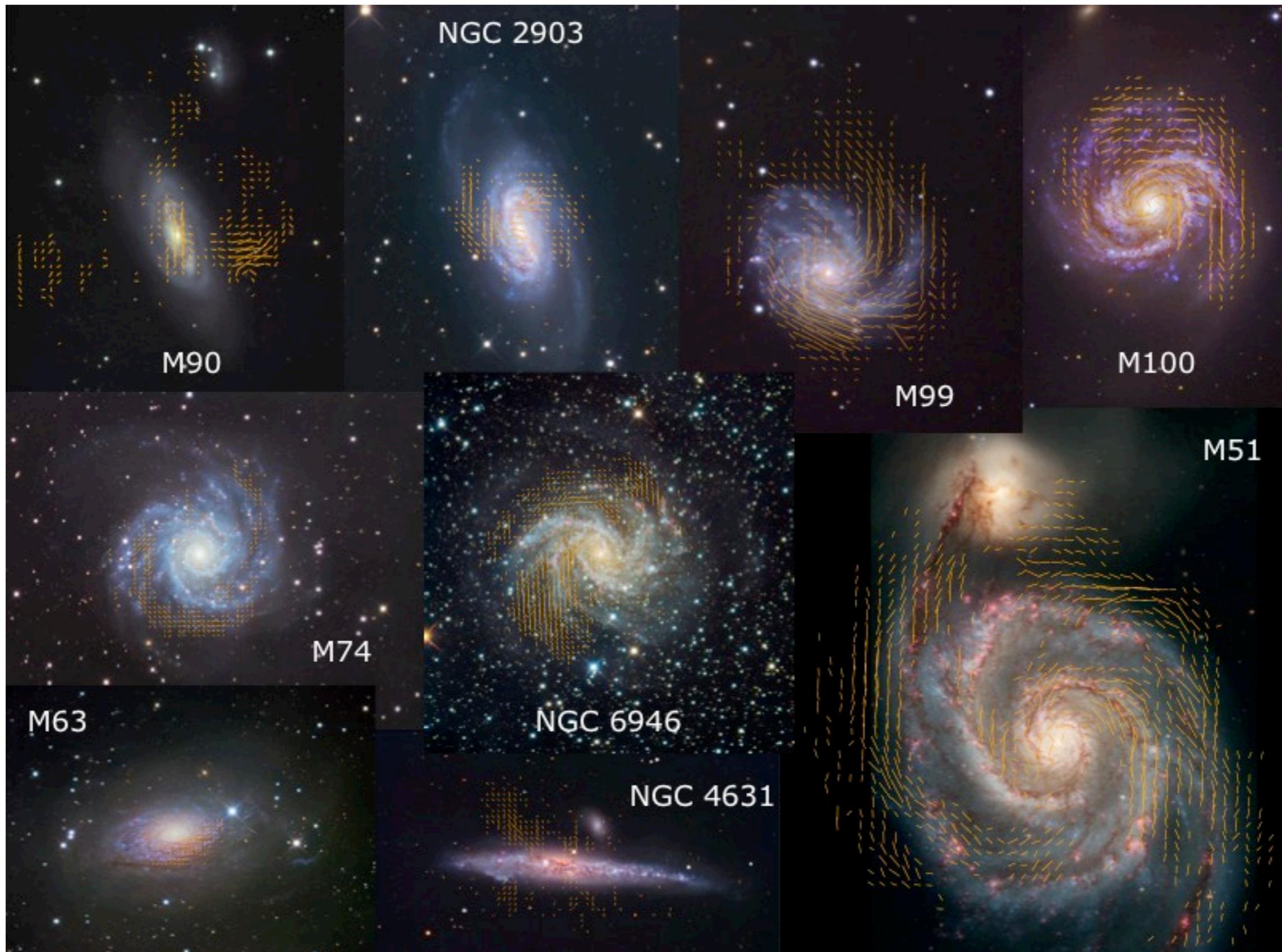
- 28 galaxies studied
 - 21 detected in polarization
 - 0/4 Magellanic/elliptical
 - 21/24 spirals



Resulting images



LOFAR ASTRON



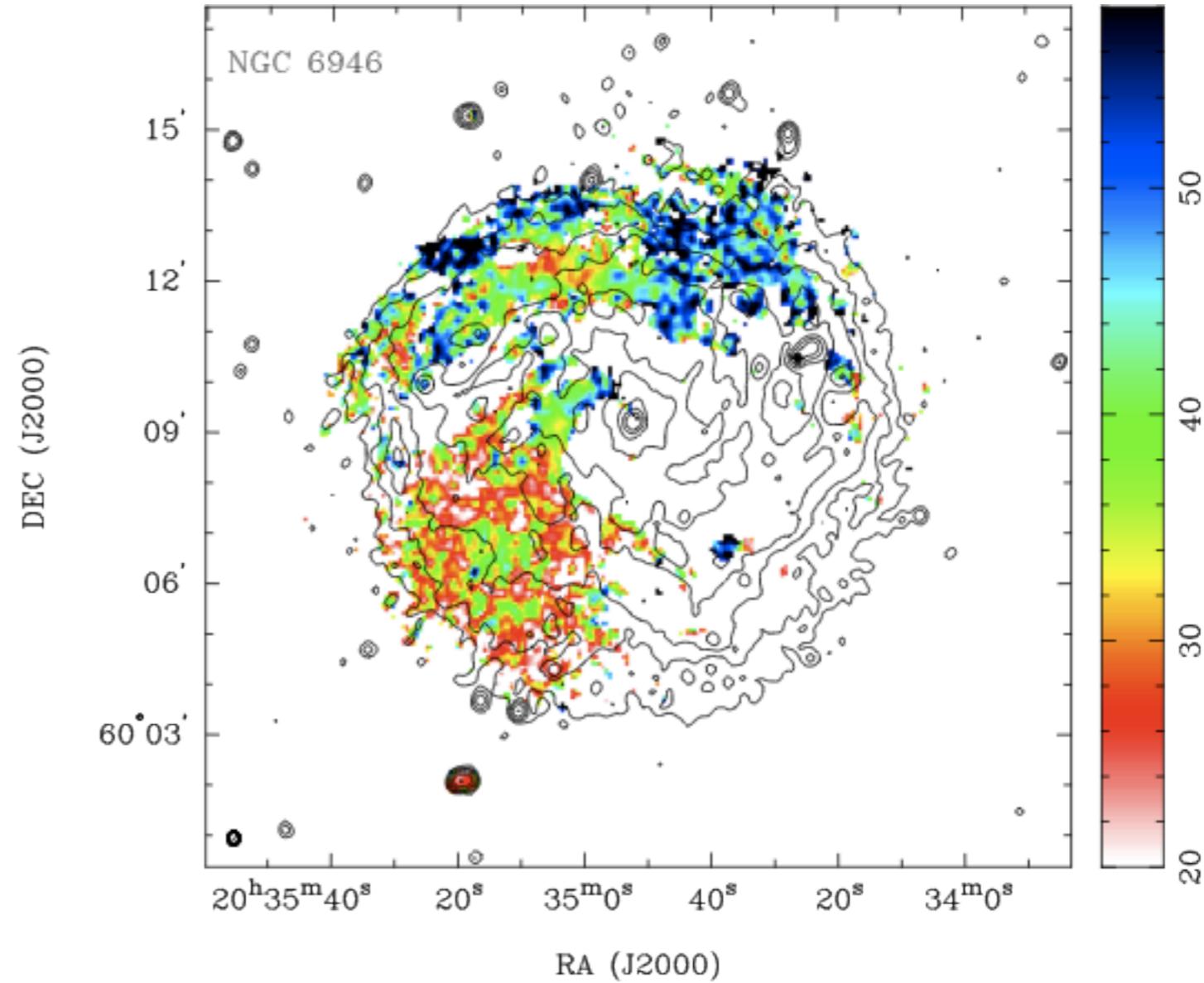
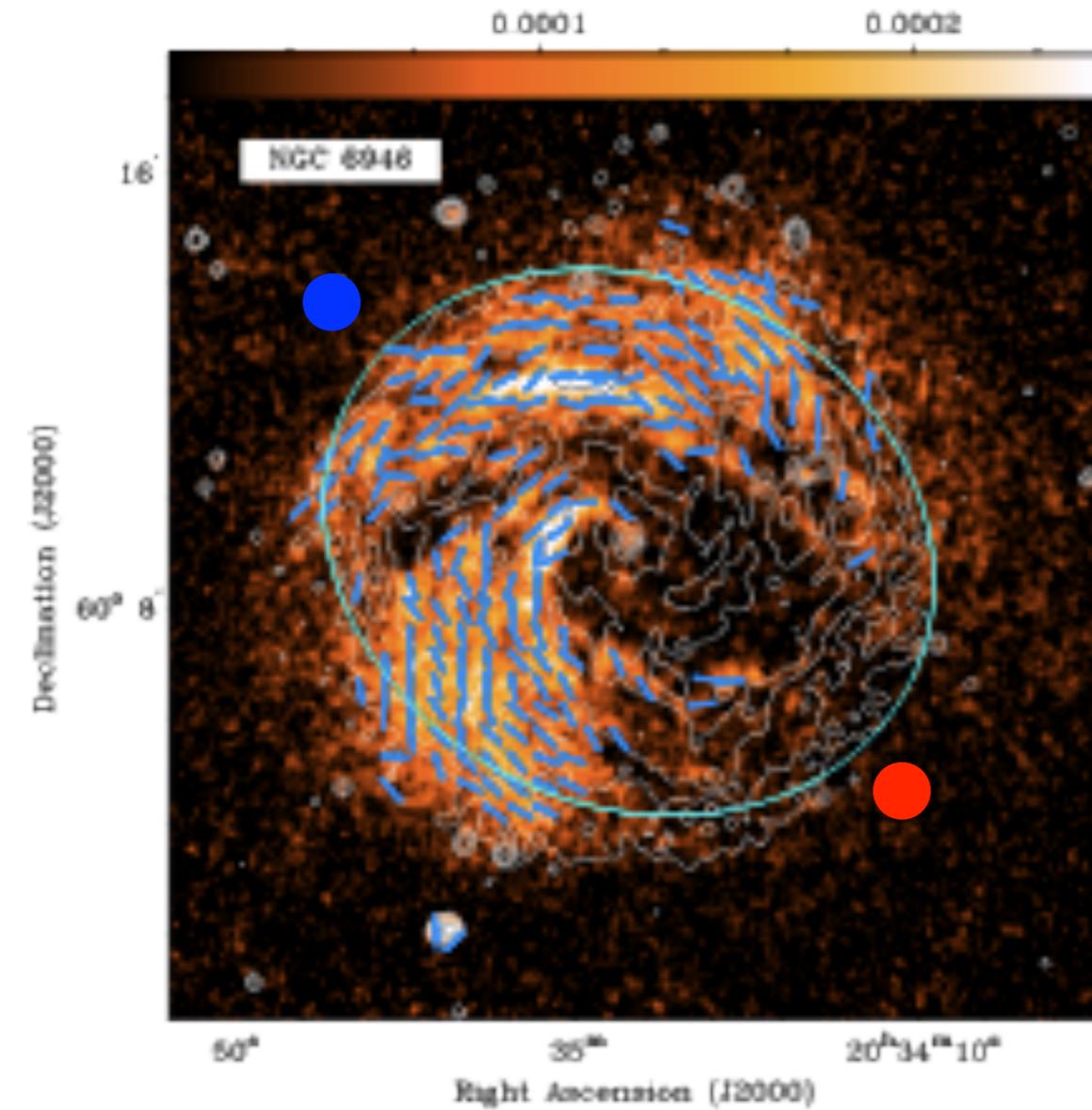
NGC 6946

- approaching side
- receding side



LOFAR ASTRON

PA = 243°



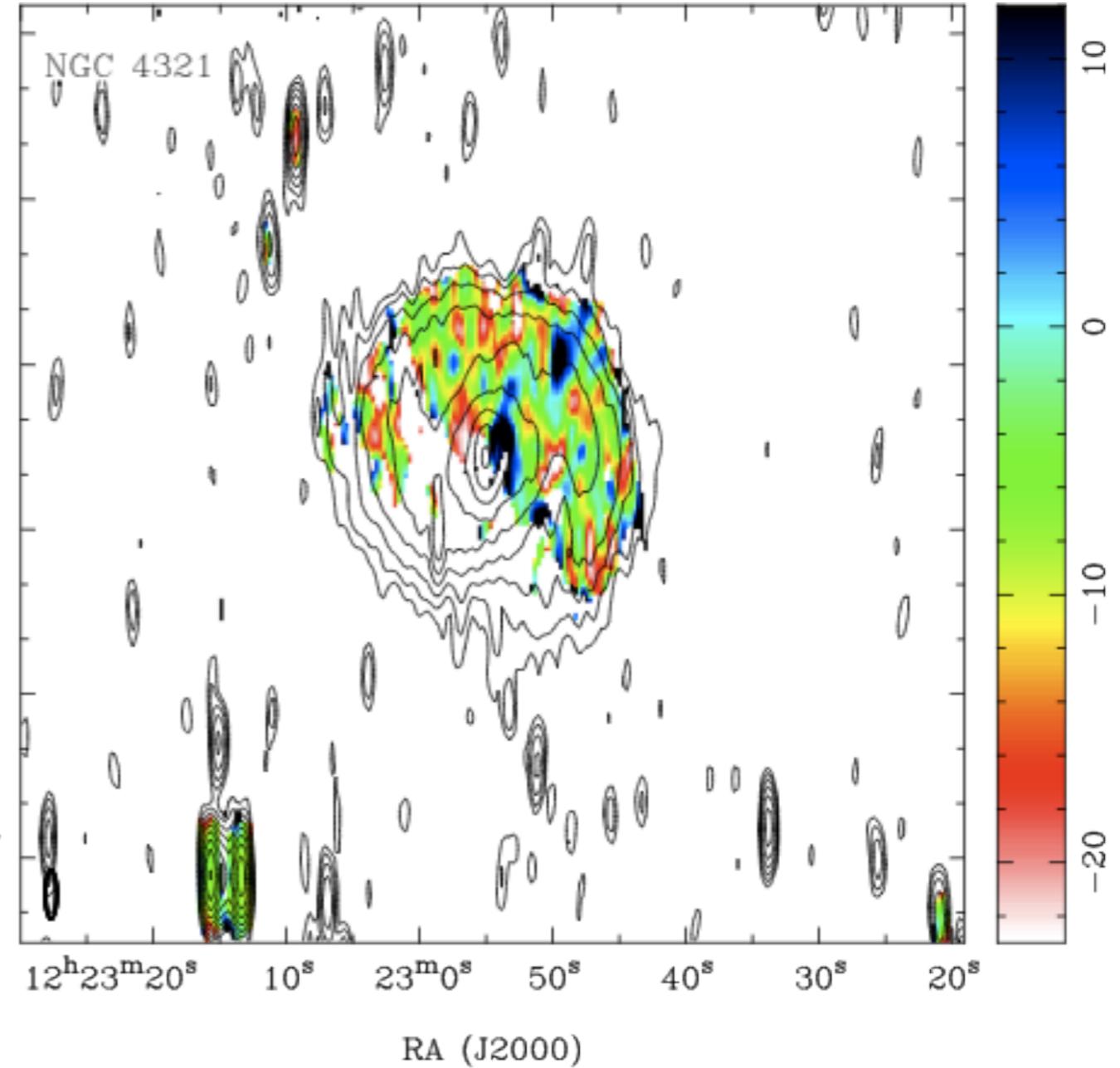
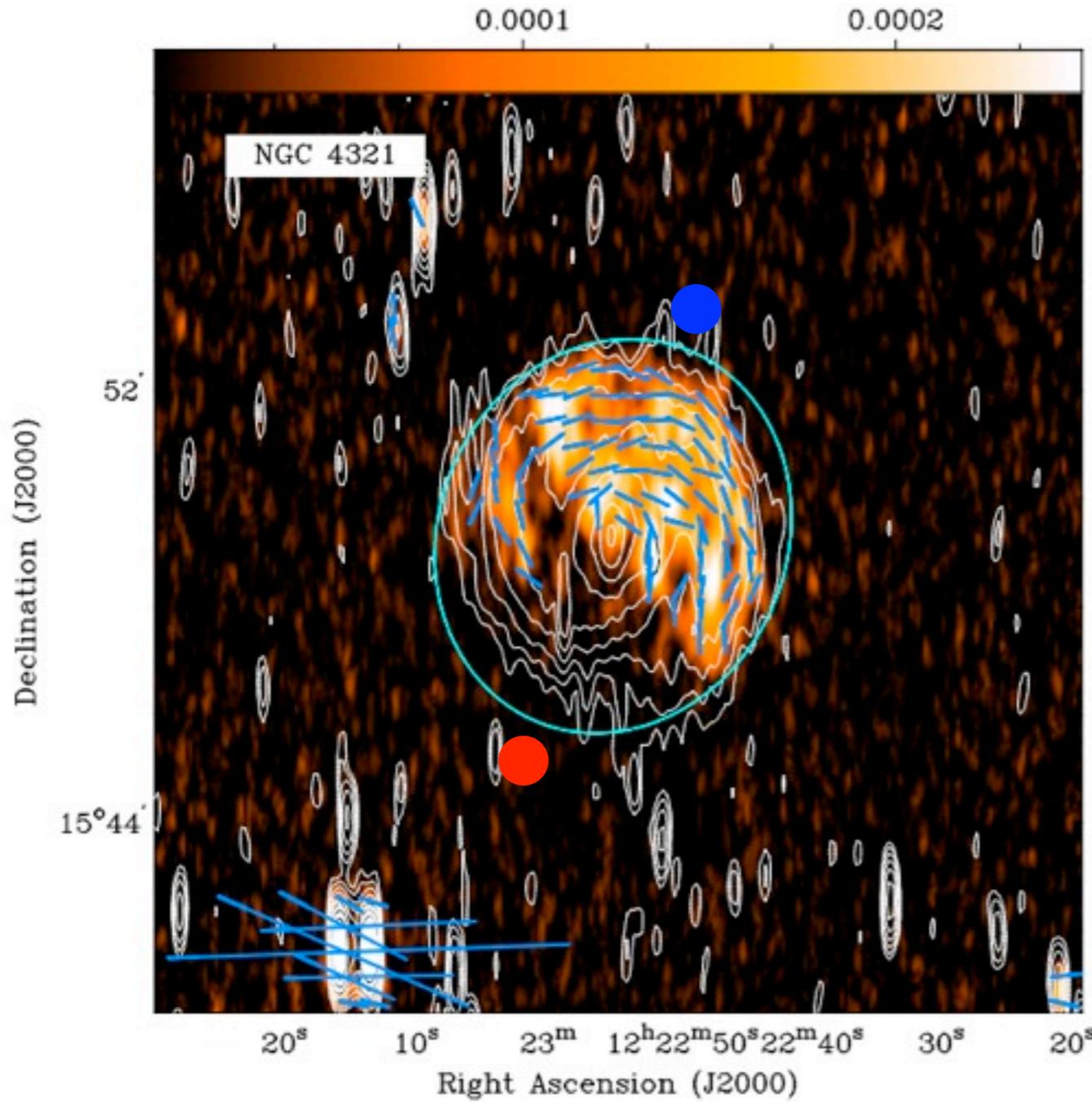
NGC 4321

- approaching side
- receding side



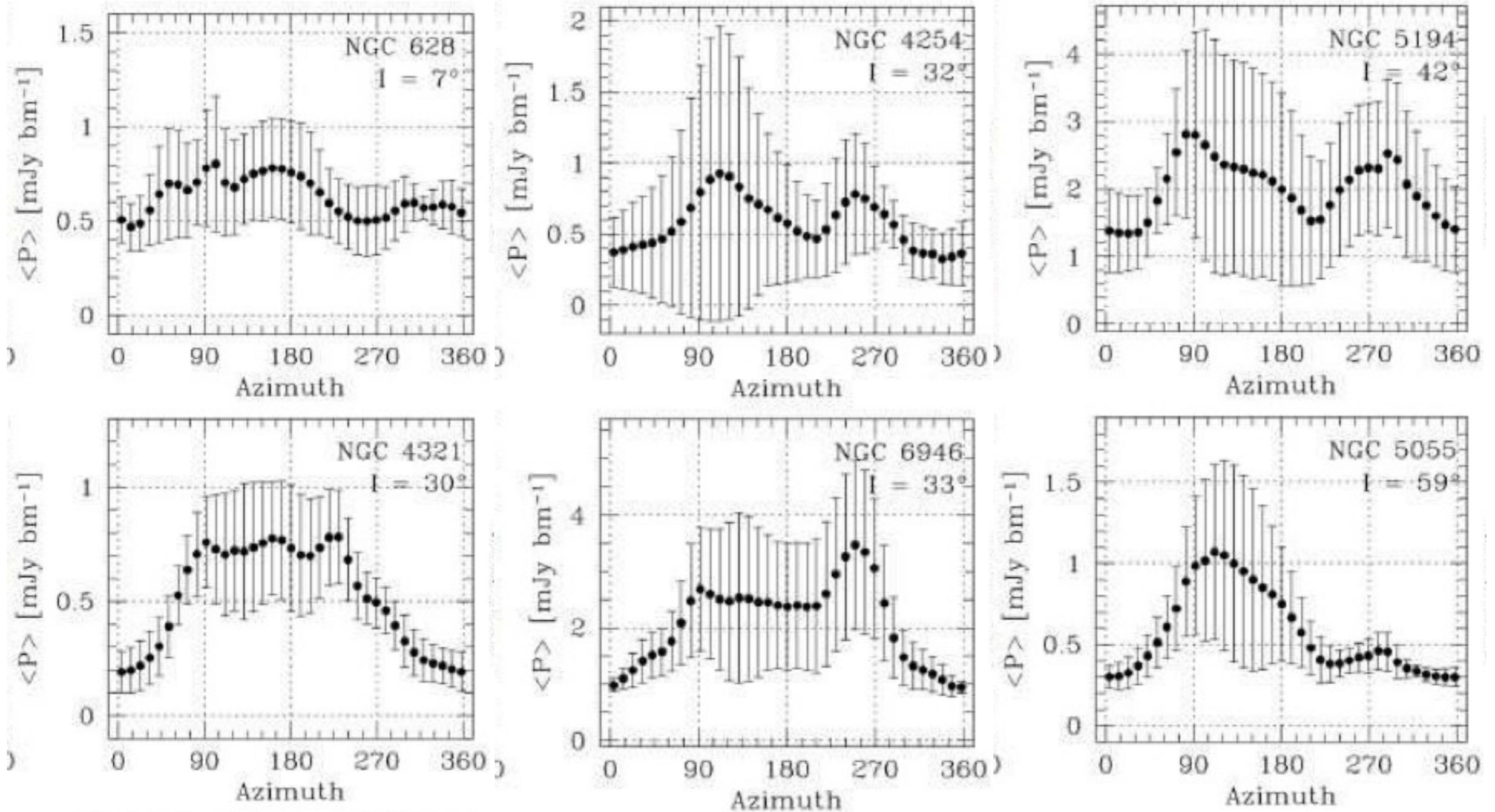
LOFAR ASTRO

PA = 159°



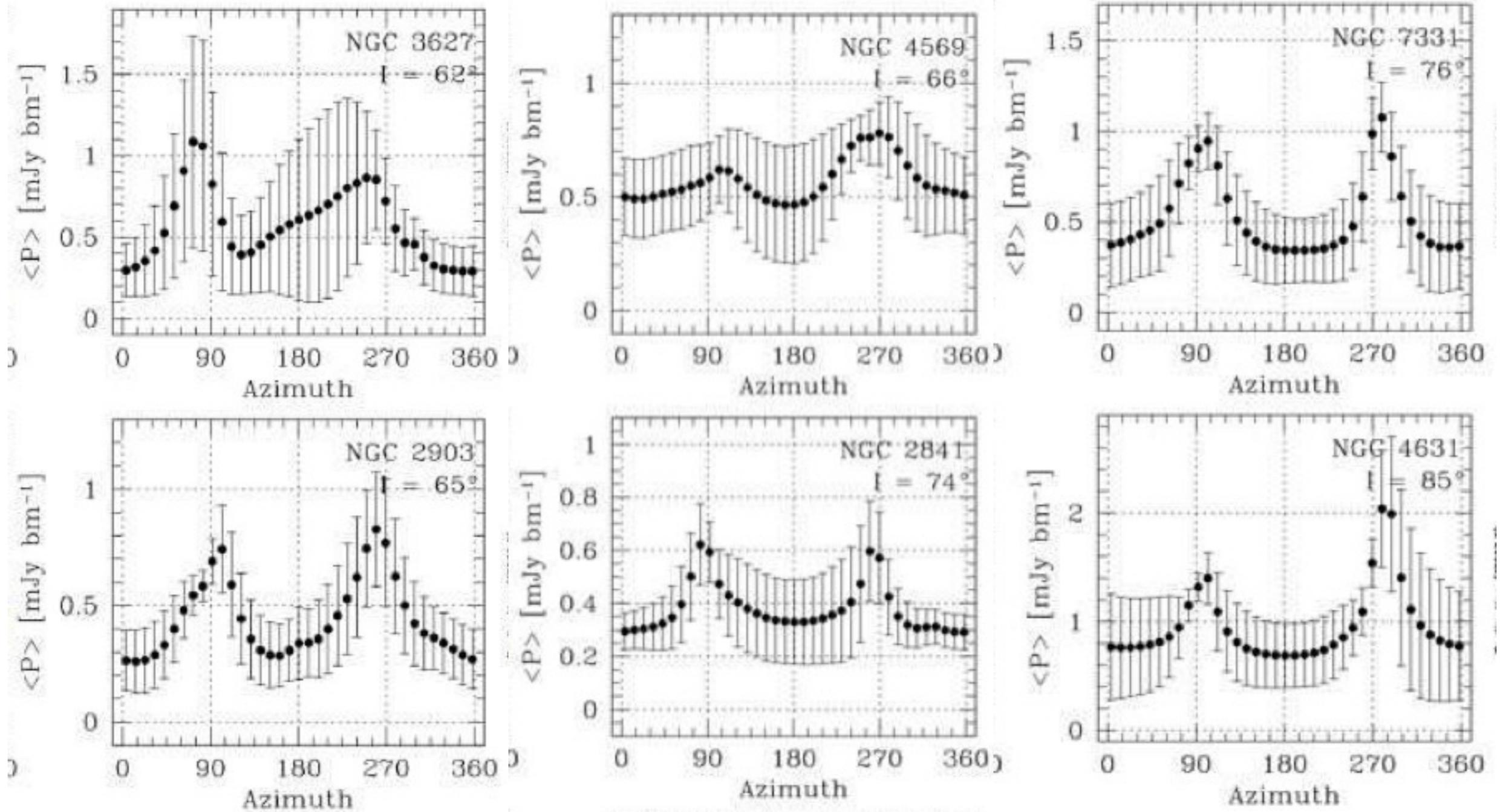


- Minimum in P consistently found on the receding major axis -- WHY?





- Minimum in P consistently found on the receding major axis -- WHY?





- Combination quadrupolar field + axisymmetric spiral (NB: *geometry only*)



Observer

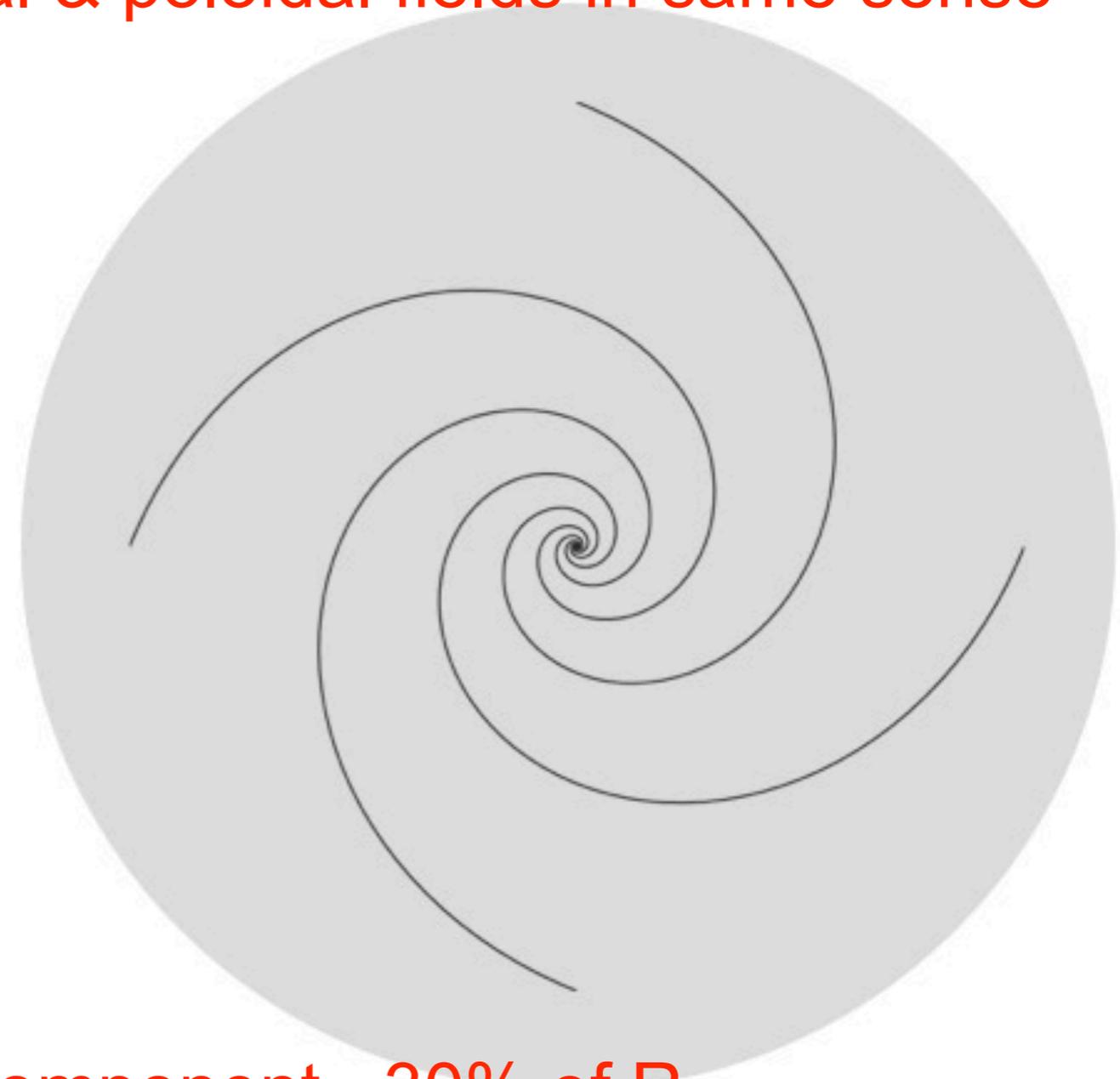
Toroidal & poloidal fields in same sense

Faraday rotation

synchrotron

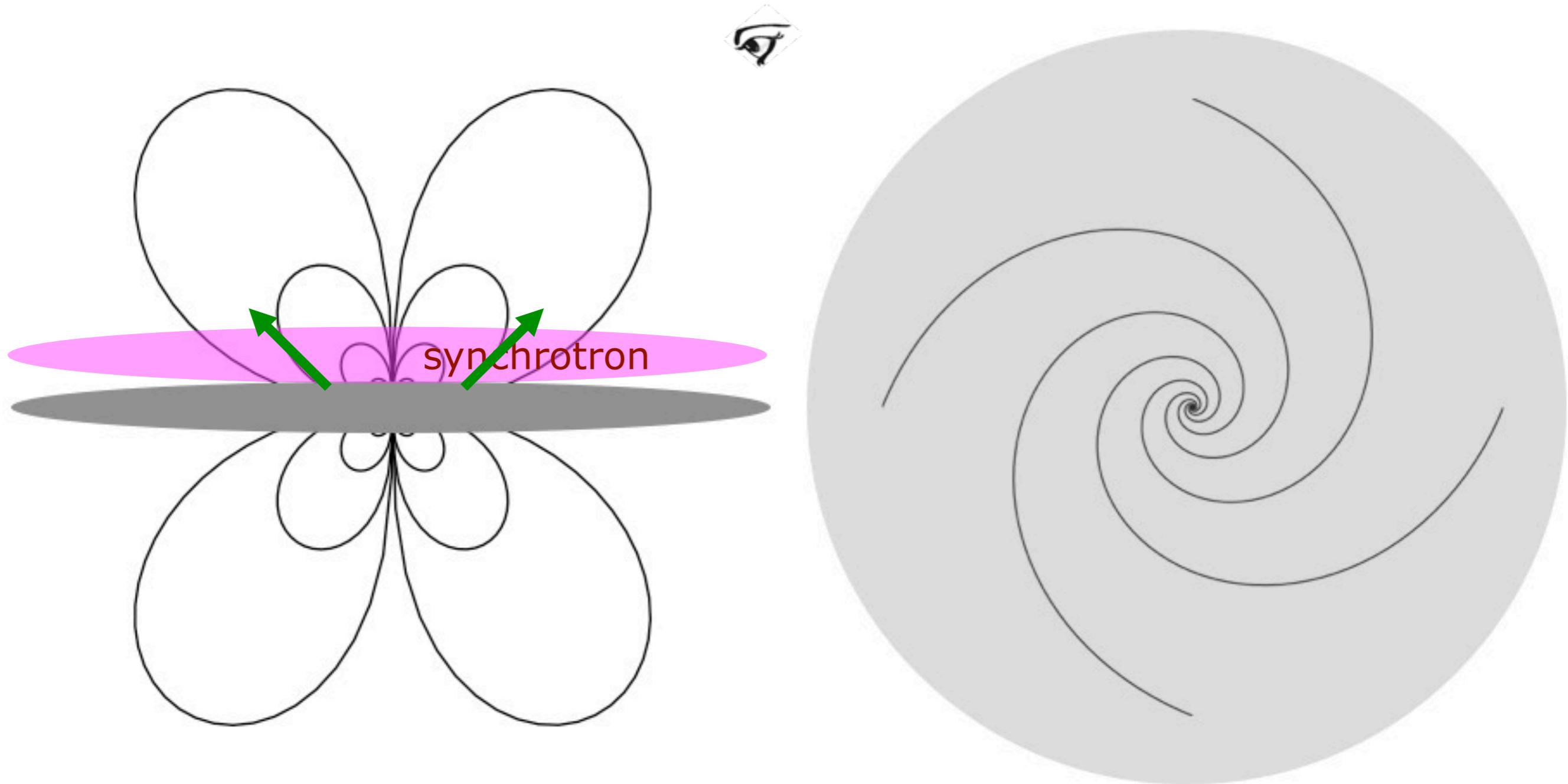
SF disk

strong depolarization

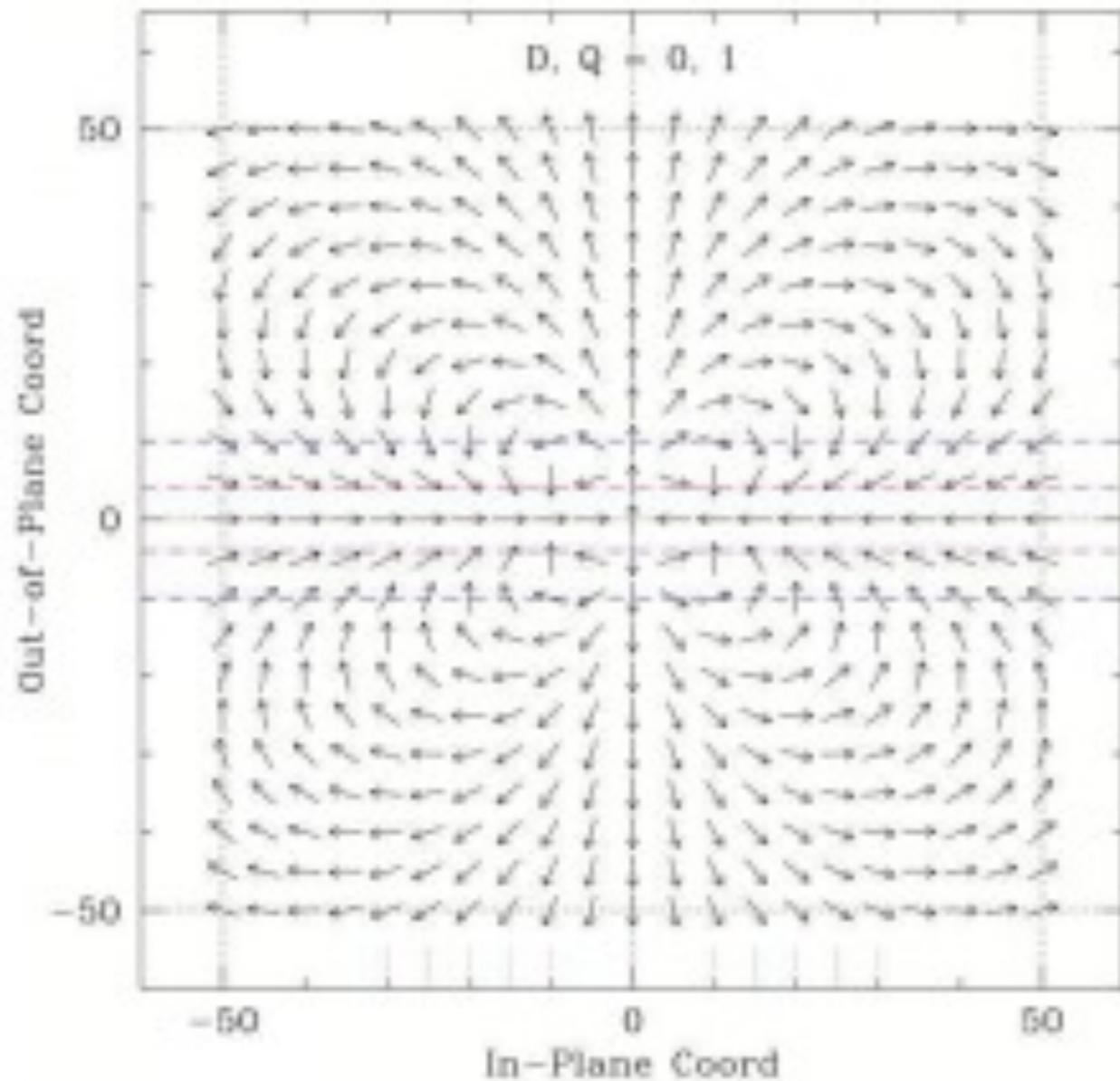


Vertical extent of spiral component $\sim 30\%$ of R

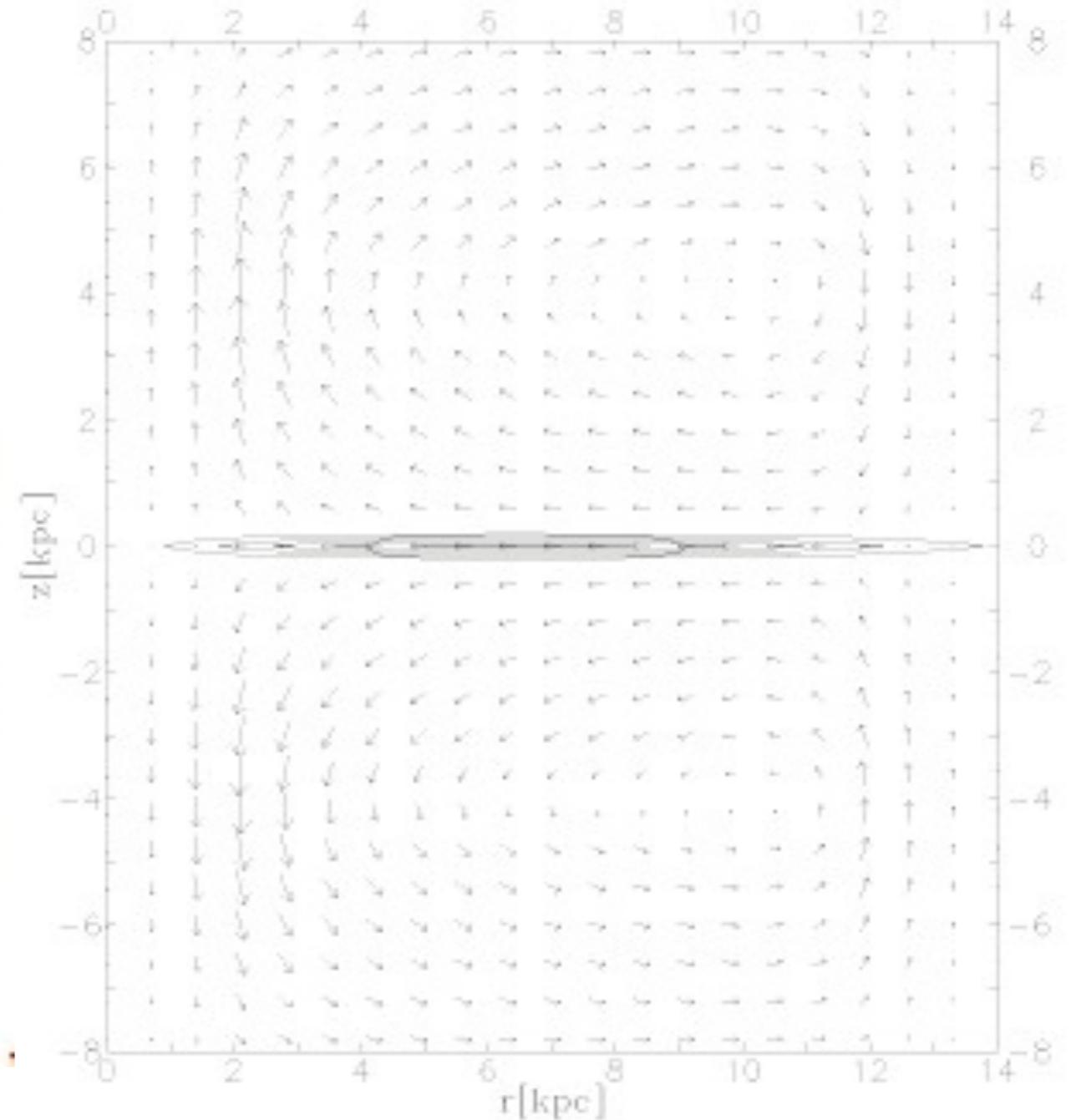
- Azimuthal asymmetry by field projection ("square styrogalaxy model")



- Such a geometrical model reproduces the correct effect
- (see also Urbanik et al. 1997, who showed a similar model)



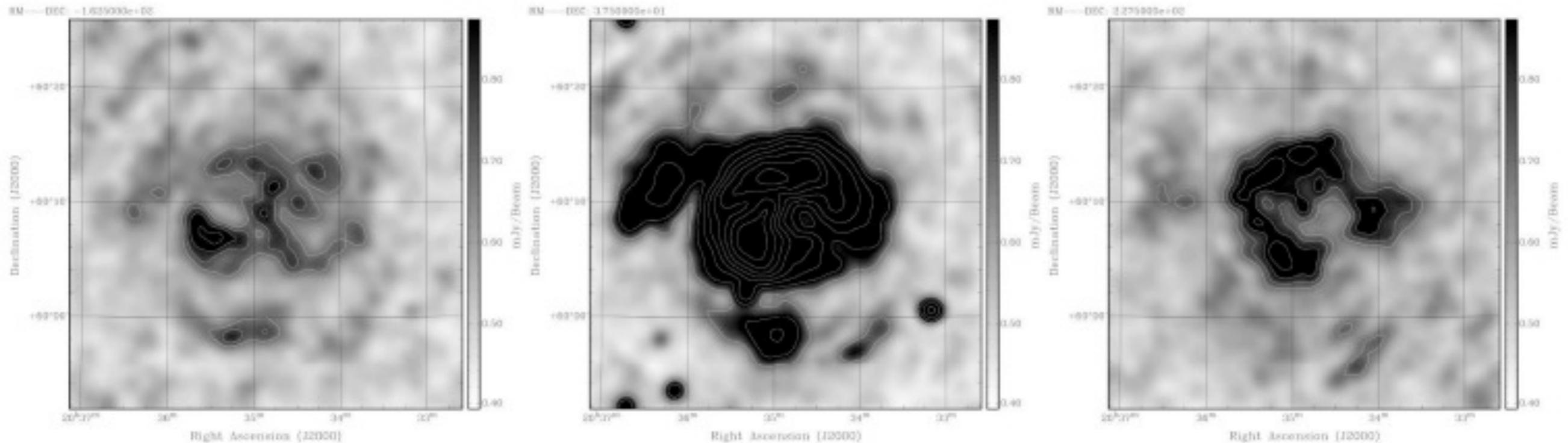
Braun et al. (2010)



Urbanik et al. (1997)



- RM Synthesis reveals polarized emission at extreme values of Faraday depth – possibly originating from behind the depolarizing medium



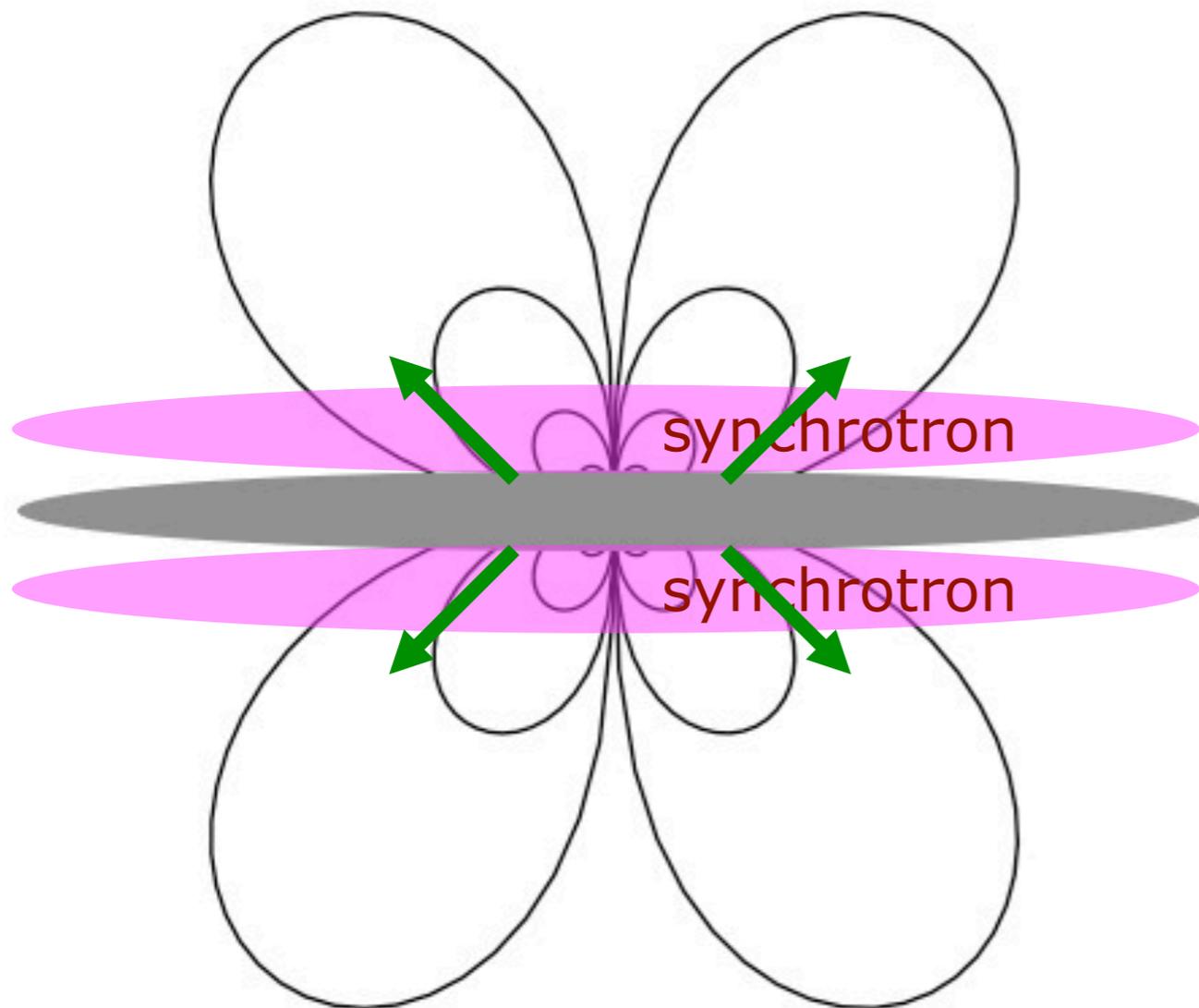
-162 rad/m²

+38 rad/m²

+228 rad/m²

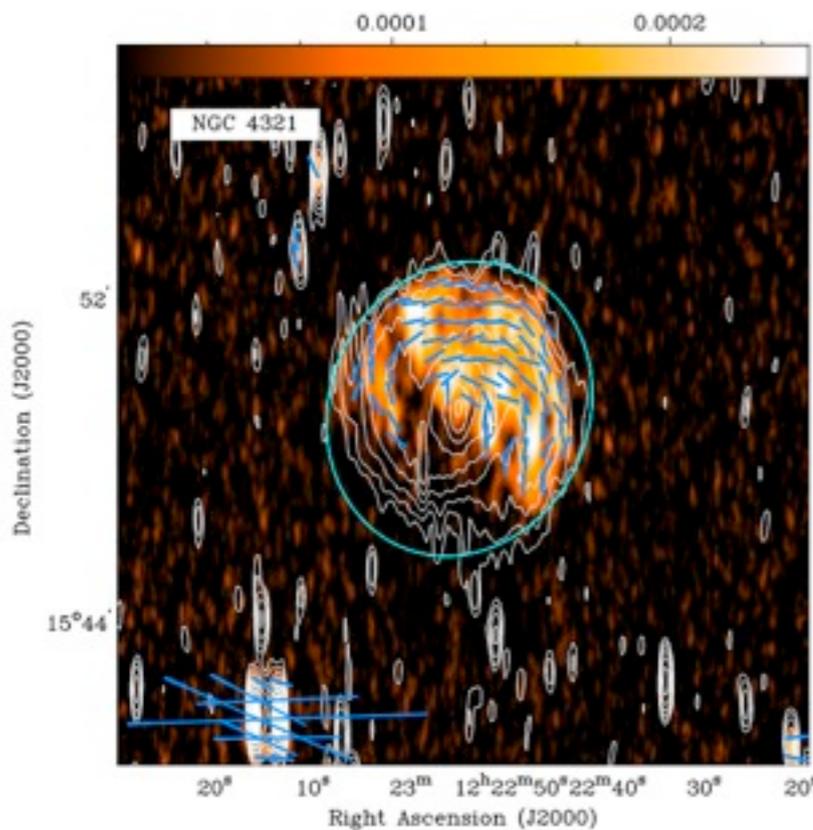
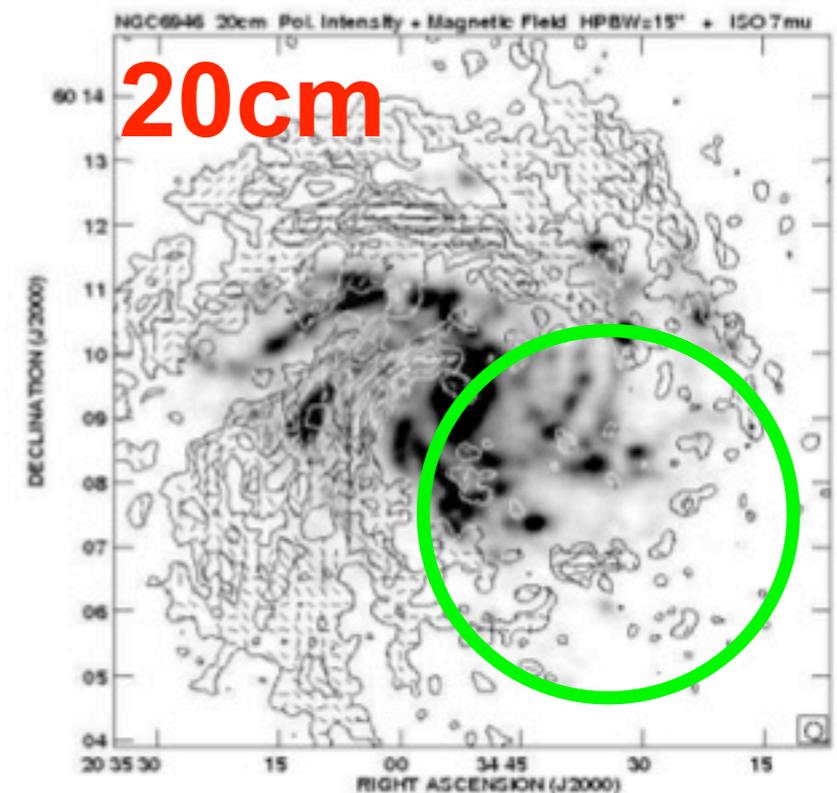
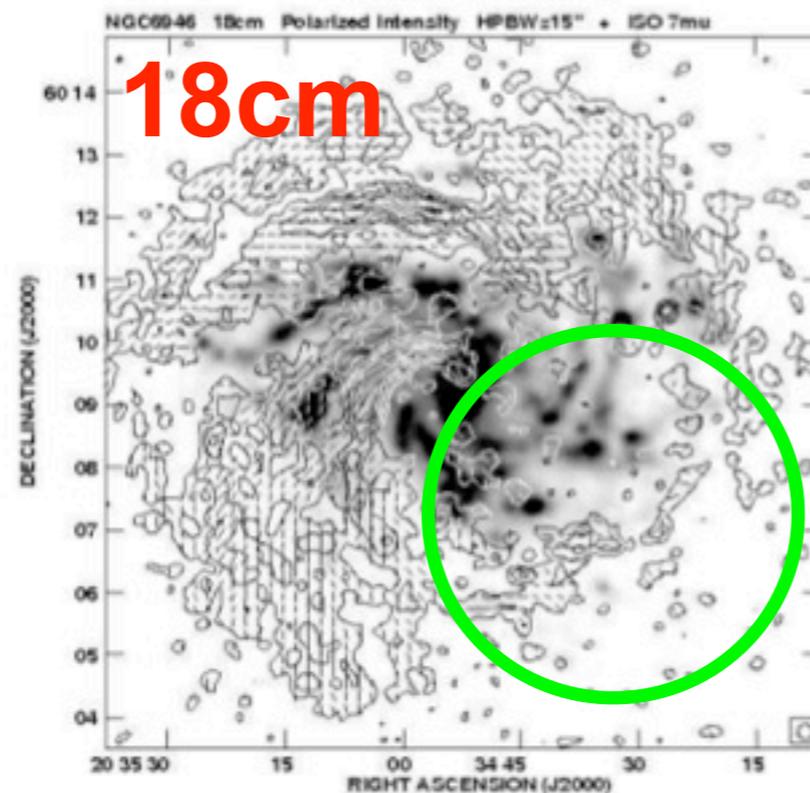
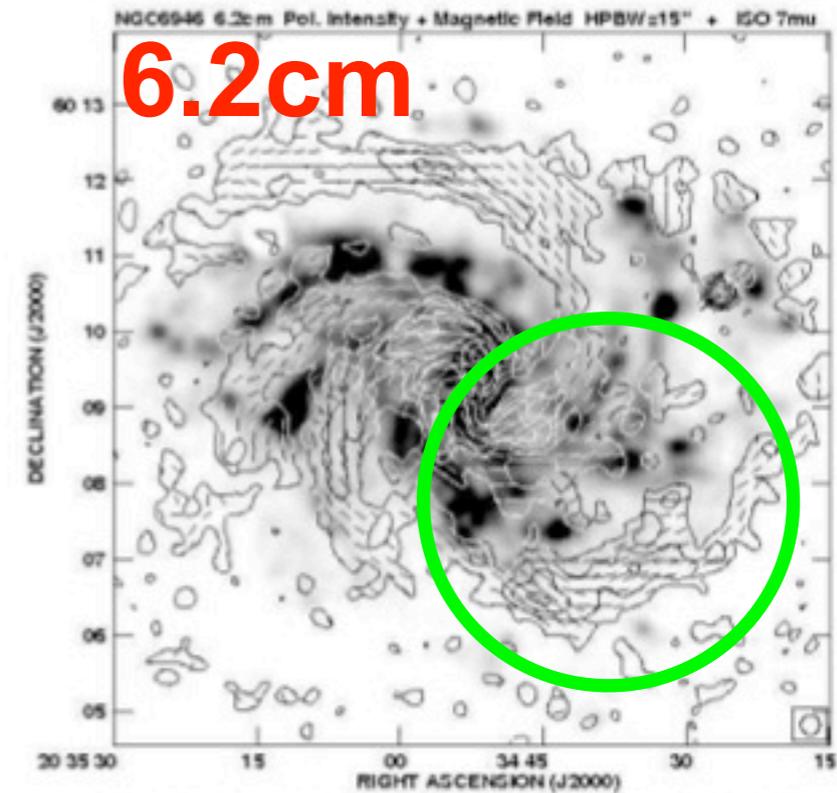
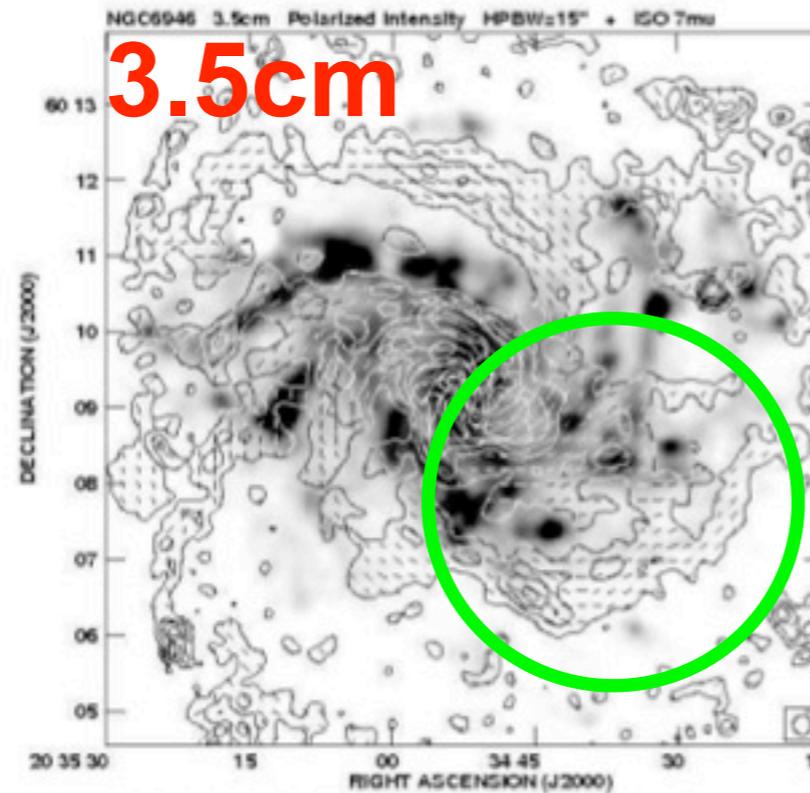


- Prediction: azimuthal asymmetry vanishes at higher frequency





- Prediction: azimuthal asymmetry vanishes at higher frequency
- Seems to be the case in NGC 6946 (Beck)
- True for others? (NGC 4321?)





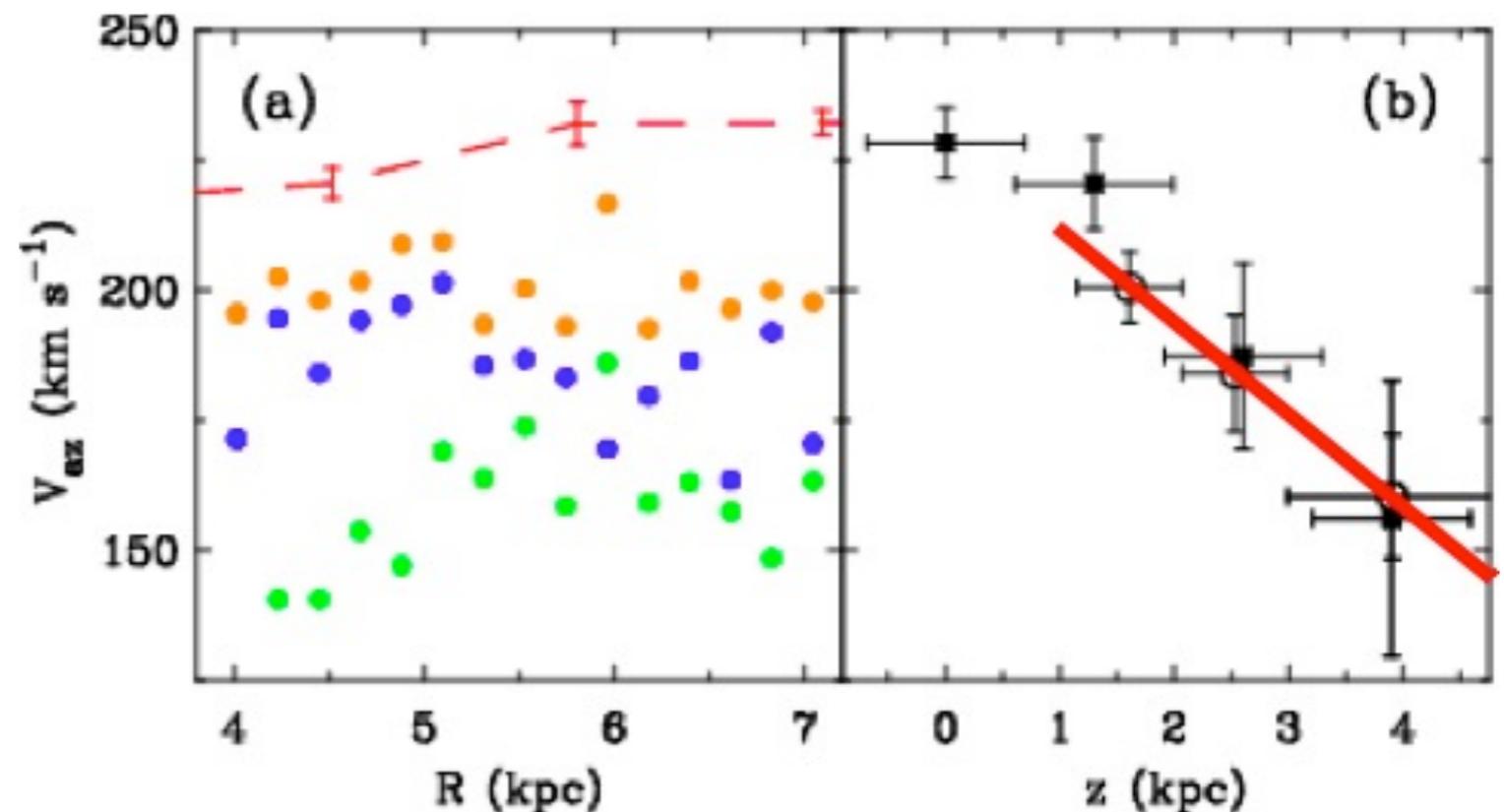
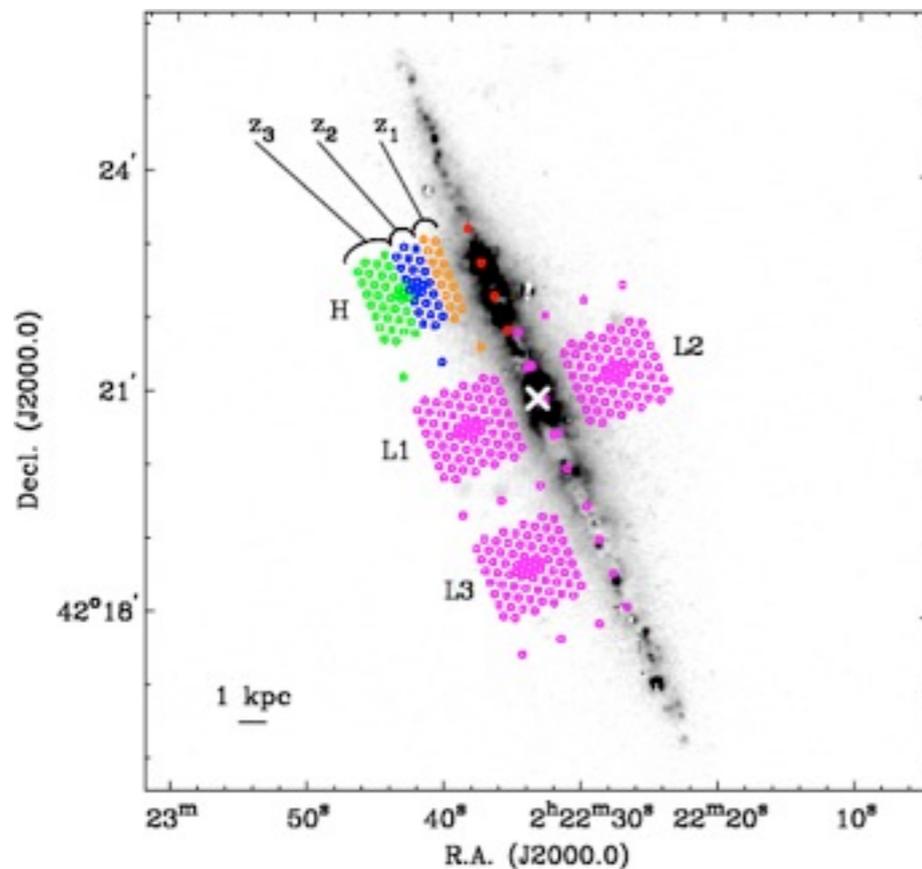
- A combination of planar and poloidal field such as this is predicted by dynamo theory (e.g. Widrow 2002)
- Dominance of axisymmetric over bisymmetric, and quadrupolar over dipolar, should give strong constraints to dynamo models



- A combination of planar and poloidal field such as this is predicted by dynamo theory (e.g. Widrow 2002)
- Dominance of axisymmetric over bisymmetric, and quadrupolar over dipolar, should give strong constraints to dynamo models
- Note that our edge-on targets actually show evidence for *dipolar* magnetic fields in the outer halo - again, predicted by dynamo theory. Why the difference? Signature of dipolar outflow?

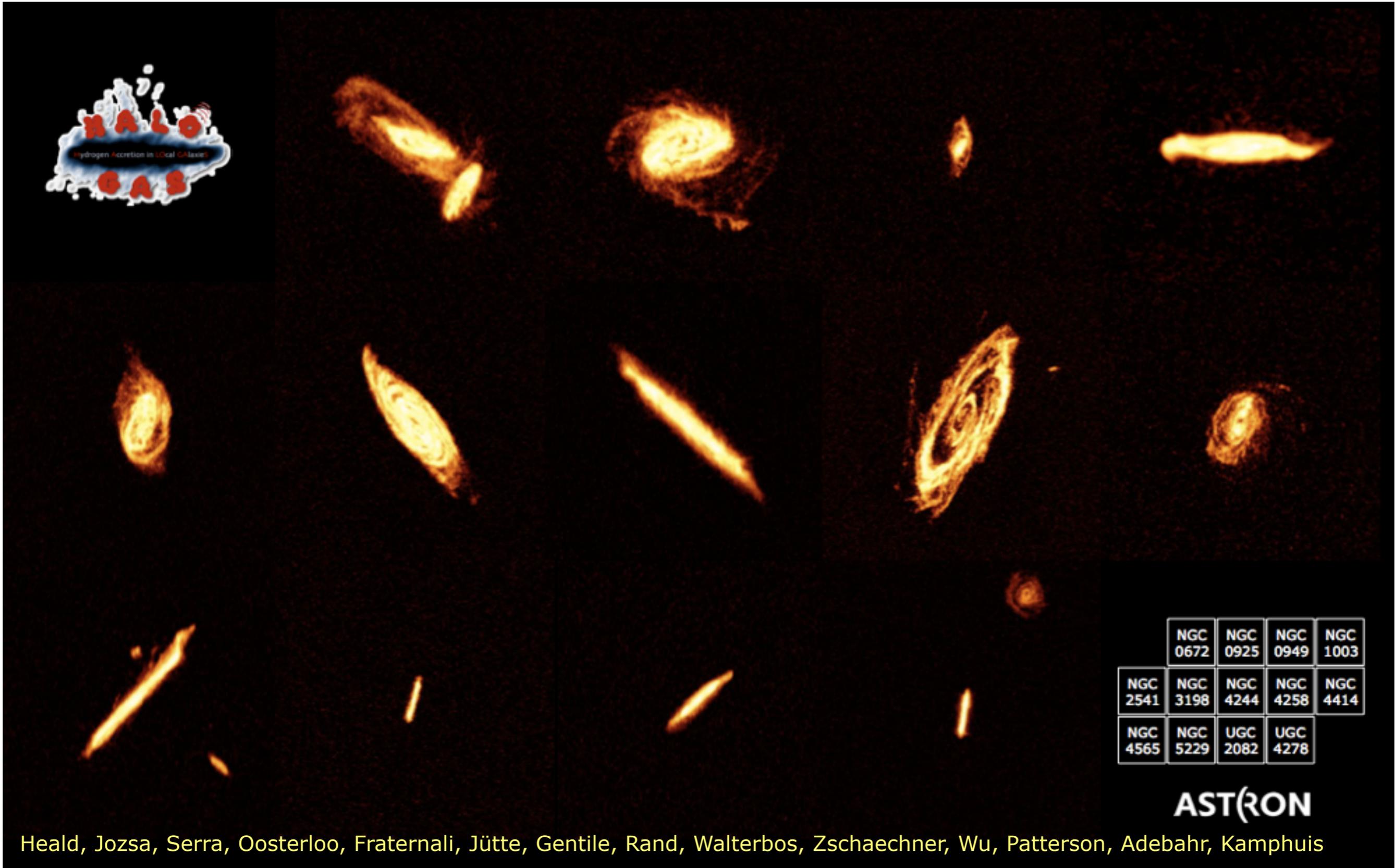


- Multiphase gas at large vertical distances above the midplane commonly observed in nearby galaxies
- Rotation of this extraplanar gas reveals a linear decrease in rotation speed with height – halos differentially rotate, but with a slower amplitude than the underlying disk (Fraternali et al. 2005; Heald et al. 2006, 2007)
- Connection between kinematics of gaseous halos and the vertical structure of the halo gas? (see Heald et al. 2007)



- LOFAR will probe the outer disks and halos of a large number of nearby galaxies, characterizing the global magnetic field geometry
- Do halo fields become predominantly dipolar in the far outer parts?
- How far do the halo fields extend?
- Complementarity between LOFAR, and other higher-frequency instruments (APERTIF, ASKAP, MeerKAT, EVLA, ...)
 - each probes a different 'zone' of the galaxy
 - gives an onion-peel view of galactic magnetic field structure!





	NGC 0672	NGC 0925	NGC 0949	NGC 1003
NGC 2541	NGC 3198	NGC 4244	NGC 4258	NGC 4414
NGC 4565	NGC 5229	UGC 2082	UGC 4278	

ASTRON

Heald, Jozsa, Serra, Oosterloo, Fraternali, Jütte, Gentile, Rand, Walterbos, Zschaechner, Wu, Patterson, Adebahr, Kamphuis

- LOFAR station status visible online at <http://www.astron.nl/~heald/lofarStatusMap.html>
- Interferometry mode works well (fringes and images on 600-km baselines @ 30 MHz!); Imaging pipeline in good shape (Heald+ arXiv:1008.4693)

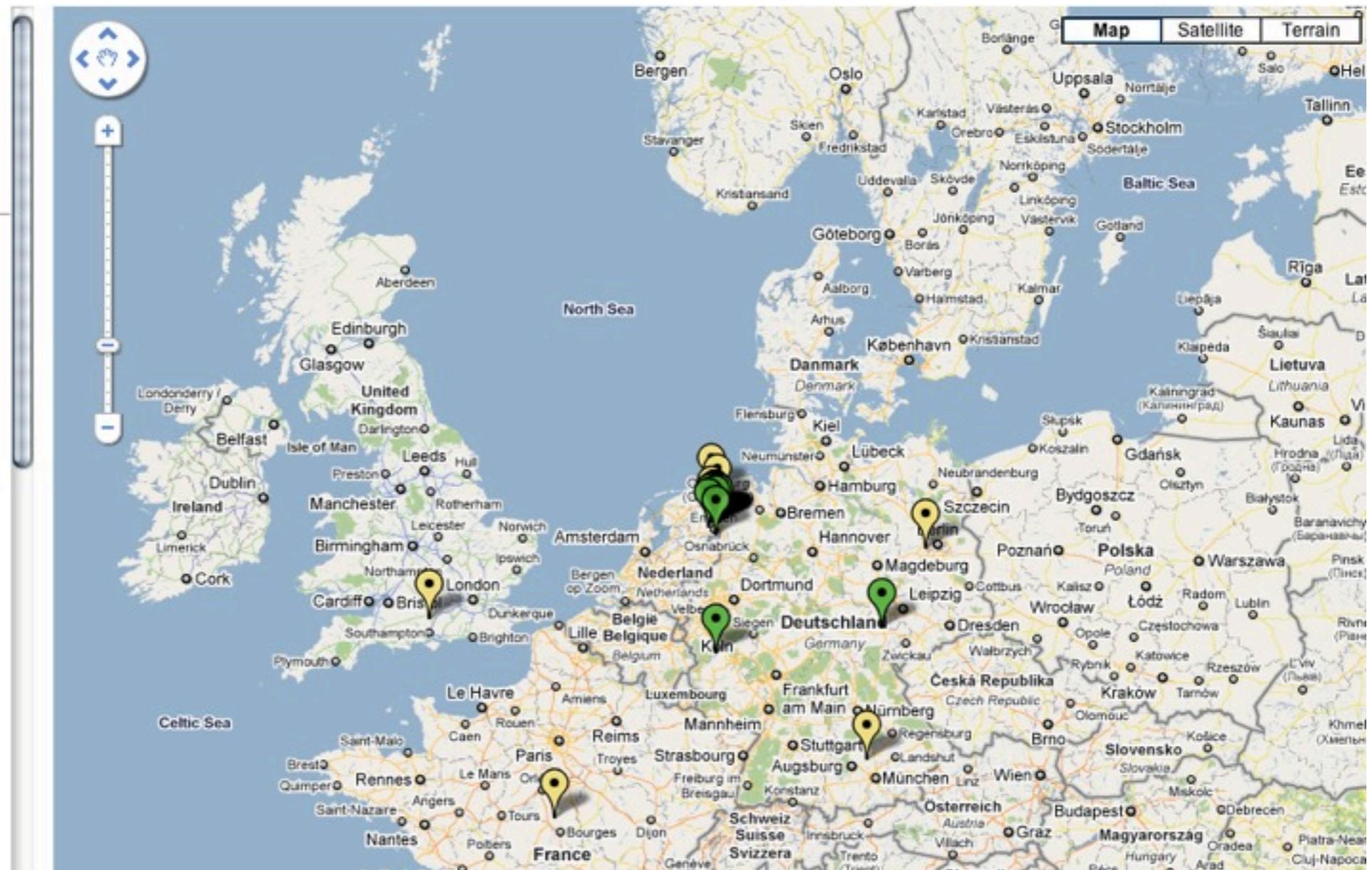
LOFAR status map

Last update 2010-07-22

Completed stations (validated by the Radio Observatory):

[Show all] / [Hide all]

DE601 [Hide]
DE603 [Hide]
CS103 [Hide]
RS106 [Hide]
RS205 [Hide]
RS208 [Hide]
CS302 [Hide]
RS306 [Hide]
RS307 [Hide]
RS503 [Hide]
CS001 [Hide]
CS002 [Hide]
CS003 [Hide]
CS004 [Hide]
CS005 [Hide]
CS006 [Hide]
CS007 [Hide]
CS021 [Hide]
CS024 [Hide]





- Asymmetry in polarized intensity in nearby galaxies caused by combination of toroidal and poloidal components
 - Minimum P/I on receding side: consequence of *trailing spiral arms*
 - Asymmetry expected to vanish at higher frequency
- New observational programs with LOFAR and other (higher frequency) new telescopes will allow us to learn much more about the full 3-D structure of galactic magnetic fields